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dr Tomasz Kawalec

Opracowanie utworu pod tytułem:

"Współczesne doświadczenia z zimnymi atomami" w ramach kursu zaawansowanego, organizowanego dniach 31.08 – 25.09.09 będącego kontynuacją szkoleń z zakresu eksploatacji i zarządzania dużą infrastrukturą badawczą organizowanego przez Narodowe Laboratorium Technologii Kwantowych



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Introduction

some criteria:

- cold and ultracold gases + some examples with atomic beams
- spectacular experiments that show the quantum nature of atoms
- experiments in the fields that are currently or in close future being developed in Poland
- just my subjective choice 🙂







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General table of contents

• part I – matter waves atom interferometry, coherence in BEC, atom laser

• part II – atoms close to surfaces atom chips, optical dipole traps, fundamental experiments

• part III – some properties and applications of cold atoms quantum degenerate gases, atomic clock







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Współczesne doświadczenia z zimnymi atomami część I – fale materii

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Table of contents

- why (ultra)cold atoms?
- atom optics
- atom interferometry
- atom laser milestones
- atom laser realizations
- prospects for atom interferometry











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Atom optics

Atom optics – coherent manipulation of atomic motion requires that they are treated as waves, so many techniques to control atom waves comes from light optics.

Atom interferometry comes from the development of coherent manipulation of the translational motion of atoms and molecules and started in 90'.

Atom interferometer components (in analogy to an optical interferometer):

 state selection to localize the initial state generally in momentum space: slits, atom cooling and trapping
coherent splitting, by e.g. diffraction to produce at least two localized maxima of the wave function with a well-defined relative phase: e.g. nanostructures, light gratings

$$\theta_n \approx \delta p_n / p_{\text{beam}} = n \lambda_{dB} / d$$

but transverse coherence length has to be \approx a few "d"

momentum uncertainty in units of photon momentum (590 nm):

optical molasses or MOT: 20 collimated beam (transverse): 1 Bose-Einstein condensate: 0.1

3. free propagation so that **interactions** can be applied to one arm; great sensitivity:

 $\Delta \phi = 1 \text{ mrad} \Rightarrow U/E = 10^{-14}$ (energy resolution)

4. coherent recombination so that phase information is converted back into state populations,

5. **detection** of a specific population, so the relative phase of the wave-function components can be determined from interference fringes.







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Atomic interferometry



[11]	3,	761	,721
[45]	Sept.	25,	1973

Primary Examiner—James W. Lawrence Assistant Examiner—B. C. Anderson Attorney—Daniel T. Anderson et al.

ABSTRACT

[57]

An apparatus is disclosed which makes use of interferometry of the matter waves accompanying particles such as neutral atoms, charged ions or electrons. The apparatus includes a particle source and a beam splitter for splitting the original beam of particles into two beams having accompanying matter waves which are coherent with each other. The two beams are recombined by a pair of beam reflectors, and the resulting interference fringes may be measured by a suitable particle detector. Such an apparatus may be used for mea-

rotation of the apparatus. In both cases the apparatus is capable of ultra precise measurement of acceleration, of the mass of an object or the rate of rotation. Alternatively, by utilizing charged particles it is possible to measure a magnetic field to obtain a magnetometer of great sensitivity. The apparatus may finally be used to carry out holography by matter waves. calculated accuracy of gravitational field gradient measurement: $\delta g/g = 5 \times 10^{-7}$







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Atomic interferometry



Phys. Lett. A 318, 184 (2003)

• trapped BEC \Rightarrow high spatial resolution, but phase diffusion, atomic density gradient (interaction induced decoherence)

- nondegenerate sample \Rightarrow lower spatial resolution
- fermions \Rightarrow collisions suppressed, but quantum pressure PRL **92**, 230402 (2004)
- Feschbach resonance \Rightarrow s-wave scattering length \rightarrow 0 PRL **100**, 080405 (2008)







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Atom laser – milestones $T=317~{\rm nK}$ $T=176~{\rm nK}$ $T=80~{\rm nK}$ $N_t = 0.8 \times 10^5, N_c = 0.9 \times 10^5$ $N_t = 4.2 \times 10^5, N_c = 0$ $N_t = 2.6 \times 10^5, N_c = 0.4 \times 10^5$ achievment of BEC • interference of condensates, showing first and second order coherence, long range correlations, temporal coherence, single particle coherence, many particle coherence F=1,m=1 a method of coherent F=1,m=0 outcoupling of atoms from BEC

F=1,m=-1







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Interference in BEC many particle coherence 30 BECs coherent splitting of BEC: BEC (a atom chip experiment 50 µr split independent BECs: (b) ASER 0 LASER d) 350 un $\Delta \phi$ (rad) splitting by RF-field phase difference, shot to shot 200 shots + number-phase uncertainty considerations Dalibard, PRL 93, 180403 (2004) (why relative phase exists?) Schmiedmayer, Nat. Phys. 2, 710 (2006) Schmiedmayer, Nat. Phys. 1, 57 (2005) + similar experiment on atom chip: Ketterle, PRA 72, 021604 (2005)







density profiles



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Atom laser – properties

		atom "laser"		laser	
output		coherent matter waves		coherent EM waves	
resonator		trap		mirrors	
active medium		thermal cloud of ultracold atoms		gain medium	
excitation of the active medium		evaporative cooling		pumping	
		stimulated emission of bosons into the same lasing mode			
thresh	nold	critical temperature		pumping threshold	
lim	it	Heisenberg uncertainty		diffraction limited	
	modes	single mode	m	many modes possible	
	modes	lowest mode	ł	high cavity modes	
	interactions	yes		no	
		atoms cannot be created	pho	otons can be created	

important

thermal equilibrium



gravity

beam quality:

not important

non-equilibrium

• optics:

$$M^2 = \frac{w_{0R}\theta_{0R}}{w_0\theta_0}$$

atom optics:

$$M^2 = \frac{2}{\hbar} \Delta x \Delta p_x$$







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• 3. Phillips, 1998, NIST







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Atom laser – realizations MT, weak RF field, 15 ms optical dipole trap, optical potential lowering 1 2 3 5 4 1 mm 2 mm (a) • 4. Esslinger, 1999, ETH • 1. Ketterle, 1997, MIT • 5. Weitz, 2003, Tübingen • 2. Kasevich, 1998, Yale • 3. Phillips, 1998, NIST







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Atom laser – realizations



- 7. Aspect, 2006, Orsay
- 8. Close, 2008, Canberra







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Atom laser – properties











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Atom laser – properties





symmetry of the wave function of the pair of bosonic particles

Acta. Phys. Pol. 29, 1839 (1998)







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Atom laser – properties

atom lasers - advantages and disadvantages...

BEC:

- relative atom velocity 0.1 mm/s
- macroscopic coherence
- atoms interact \Rightarrow mean field interactions \Rightarrow chemical potential
- mean field energy > ground-state energy of the trap
- mean field energy dominates in free expansion
- but still the velocity spread < photon recoil velocity
- it is easy to use in interferometers based on photon recoil paths separation

atom laser:

- bright source of atoms, but limited total flux (small cross sectional area)
- coherence length on the order of BEC size
- phase fluctuations < 700 Hz (Hänsch, PRL 87, 160404 2001)
- chemical potential changes during outcoupling







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Outlook

atom optics - a flexible and precise tool for atom interferometers

• accelerating and decelerating atoms and molecules in "light crystals" and higher-order beam splitters will enable coherence to be maintained between wave function components with relative velocities of m/s! => far greater precision with much greater separation of the arms and much greater enclosed area

bigger and better interferometers will be applied to fundamental problems in gravity and quantum mechanics, e.g.:

- gravitational potential in experiments analogous to the scalar Aharonov-Bohm effect,
- in orbit around the Earth: fundamental gravitational measurements

• better measurements of G, gravitational fields, gravitational gradients, and in gyroscopes - navigation, geodesy, fine structure value

increased fluxes and longer interaction times, but! reduction of the atom densities necessary to suppress atom-atom interactions

atomic and molecular physics - measurements with higher precision

measurements of fundamental atom-surface interactions:

• the van der Waals and Casimir potentials

• study of the temporal and spatial behavior of EM fields close to the surface => w new probes of surface structure







Outlook

applications in quantum information science:

• how to characterize, control, and use entanglement and correlations in atomic ensembles: preparation of the ensembles in complex quantum states with high fidelity, and their characterization - with decoherence greatly reduced or with error-correction methods

search for fundamental short-range interactions:

• finding limits on non-Newtonian gravitational potentials at the micrometer length scale

study of many-atom systems and of atoms in lattices that model condensed matter:

• e.g. atomic interference as an indication of tunneling

study of phase transitions in mesoscopic ensembles:

• they are too large to permit full quantum calculations, but too small for the thermodynamic description, detailed look at the thermodynamic border

nanolitography - surface manipulation







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Summary

atom lasers are at their early stage of development, however many interesting properties have been measured, like:

- long spatial correlations in BECs,
- first and second order coherence,
- temporal coherence

atom interferometers have been used and are a promissing tool in precise measurements of physical constants, acceleration, gravitational field







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Współczesne eksperymenty z zimnymi atomami część II – atomy przy powierzchniach

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- why surfaces? why (ultra)cold atoms?
- atom-wall interaction
- magnetic devices atom chips, permanent magnets, main achievments
- optical devices surface mirrors and traps, main achievments
- outlook surface devices: dead-end or promissing tool?
- cold atoms as a tool in a basic surface science Casimir-Polder force and quantum reflection











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Atom-surface interactions

- 1881: van der Waals predicts existence of the attractive force between atoms and between an atom and a conducting surface
- 1932: Lennard-Jones describes the interction in a quantitative way (r-3)
- 1948: Casimir and Polder calculate the interaction energy including retardation effects and QED (r⁻⁴)



relevant wavelengths in atom-atom and atom-wall interaction









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Atom-surface interactions









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Magnetic trapping and guiding

motivation: traps and guides for atoms in the micrometer scale



- ➤ high resolution and precision of surface structures → high resolution of trapping potentials
- ▶ high potential gradients → high energy separations between energy levels
- quantum engineering
- ➢ decoherence
- Iow-dimentional mesoscopic systems
- BEC beyond mean-field theory
- guides for matter waves
- quantum information technology







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Magnetic trapping and guiding

microtraps for neutral atoms

neutral atom manipulation via interactions with external fields:

- magnetic
- electric
- optical

 $V_{mag} = -\mu \cdot \mathbf{B} = -g_F \mu_B m_F B$

+ adiabatic approximation

 $U_{B} [\mu K] \sim 67B [Gs] @ \mu = \mu_{B}$

 $V_{el}(r) = -1/2 \alpha E^2(r)$ $U_{el} [\mu K] \sim 98E^2 [V/\mu m]$

atoms in magnetic field:

magnetic moment antiparallel to the B field direction $\rightarrow V_{mag} > 0$ \rightarrow weak- field seeking state

but: Majorana spin flips

magnetic moment parallel to the B field direction $\rightarrow V_{mag} < 0$ \rightarrow strong-field seeking state

but: no local maxima of B in free space







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Magnetic trapping and guiding









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atom guiding

Magnetic trapping and guiding



U and Z wires provide "endcaps"







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Magnetic trapping and guiding

 first experiments – beginning of 90' – focused on atom guiding along the wire and investigation of simple trap geometries

c)

- typical currents: up to 20 A
- loading efficiency from MOT: up to 40%

weak field seeking traps





bent wire trap \rightarrow



 $B_{h=} = 21G$ $B_{h=} = 36G$

 $B_{b=} = 5G$



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 $B_{h=}=52G$



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Magnetic trapping and guiding

experiments with free wires led to the construction of surface micro devices atom chips

Advantages over free wires:

- greater stiffness
- greater current densities
- better heat removal
- stronger atom confinement (< 10 nm)</p>



(electroplating)

close view at atom chips Hänsch, Phys. Rev. Lett. 86, 608 (2001)

Problems:

- non-linear current flows
- > van der Waals type forces
- roughness at nano-scale





(nanofabrication)







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Magnetic trapping and guiding



Aspect, Phys. Rev. A **70**, 043629 (2004) galvanic method (electroplating)







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Magnetic trapping and guiding

Exemplary values for F=2, mF=2 Rb atoms in single wire side guide with small loffe-Pritchard field (B_{IP}) along the wire to suppress spin flips and to get harmonic potential close to the bottom of the trap

Atom	Wire current [mA]	Bias fields		Potential		Ground state			
		<i>B_b</i> [G]	В _{ір} [G]	Depth [mK]	Distance [µm]	Gradient [kG/cm]	Frequency [kHz]	Size [nm]	Lifetime [ms]
Rb	1000	80	1	5.4	25	32	41	53	>1000
Rb	500	200	4	13	5	400	250	21	>1000
Rb	200	400	20	27	1	4000	1100	10	>1000
Rb	1000	2000	50	130	1	20000	3600	6	>1000

for comparison e.g.: 0.010 kG/cm in a MOT 2 kG/cm in a magnetic trap







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Magnetic trapping and guiding

Atom chip loading:

- \succ cold atoms transport to the μ trap
- \blacktriangleright further cooling and trapping close to $\mu trap$





sketch of a μ trap







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Magnetic trapping and guiding



10⁸⁷Li atoms, a few mm over the surface

switching off MOT coils switching on U field below the surface (up to 16 A) switching on bias field (8 Gs)

switching off laser beams increasing bias field (19 Gs)

switching on U fields on the surface (2 A) switching off U field below the surface atoms are several hundreds µm above the surface

switching on Z fields switching off U fields increasing bias field (40 Gs)

lifetime: several tens of ms height over surface: a few μ m transverse confinement: 100 nm trap frequency: $\omega = 2\pi 200$ kHz



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gradual field swiching:



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Magnetic trapping and guiding

atom chips - a toolbox for physicists:

- atom traps
- transport of atoms and atom guiding
- beam splitters
- interferometers

• BEC first groups:

on-chip condensation: Zimmermann, Phys. Rev. Lett. **87**, 230401 (2001) Hänsch, Reichel, Nature **413**, 498 (2001) Reichel, J. Appl. Phys. B **74**, 469 (2002)

external condensation + transport to the chip: Ketterle, Pritchard, Phys. Rev. Lett. **89**, 040401 (2002)

making BEC on a chip – somehow easier than in a free space because of very steep potentials leading to a high collision rate and short evaporative cooling time







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Magnetic trapping and guiding



FIG. 3. Interference pattern of (a) phase shift = $2n\pi$ and (b) phase shift = $(2n+1)\pi$. The absorption images are taken 10 ms after the recombining pulse.

Cornell, Phys. Rev. Lett. 94, 090405 (2005)







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Magnetic trapping and guiding

How to turn disadvantages to advantages? magnetic field sensing!



spatial resolution: 3 μm a few μm above the conductor surface nT sensitivity

BEC aspect ratio: a few thousands (1 mm long)



Schmiedmayer, Nature **435**, 440 (2005) Schmiedmayer, Appl. Phys. Lett. **88**, 264103 (2006)







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Magnetic trapping and guiding



PRL 82, 468 (1999)

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Magnetic trapping and guiding

destructive factors in tom chips:

- trapped atom losses
- heating of atomic clouds
- decoherence

- ✓ escape through the potential barrier
- ✓ Majorana spin flips
- ✓ noise induced spin flips
- ✓ collisional losses
- ✓ tunneling towards the surface
- thermal and technical fluctuations
- interactions with light

coupling between atomic cloud and atom chip







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Optical methods

evanescent wave mirror for atoms

first proposal: R.J. Cook i R.K. Hill, 1982 first experiments: Letokhov, Phys. Rev. Lett. 60, 2137 (1988) – for beam of thermal atoms Chu, Opt. Lett. 15, 607 (1990) – for atoms from MOT









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Optical methods

$$\begin{split} U(z) &= U_{dip}(z) + U_g(z) + U_{vdW}(z) = U_0 e^{-\frac{2z}{d}} + mgz - \frac{q}{z^3} \\ \text{for alkali atoms:} \\ U_{Fm}^{dip}(z) &= (2J'+1) \frac{3}{4} \frac{\Gamma \pi c^2}{\omega_0^3} I(z) \sum_{F'} \frac{|C_{Fm,F'm}|^2}{\delta_{FF'}} \\ \text{dipole potential depends on the quantum number m} \\ \end{split}$$







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Optical methods

$$U_{vdW} = -\frac{n^2 - 1}{n^2 + 1} \frac{1}{64\pi\epsilon_0} \frac{\frac{4}{3}e^2 a_0^2 \cdot 28.2}{z^3} \quad \text{ for J} \leq 3.2$$

for $J \leq \frac{1}{2}$ (no quadrupole moments)









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Optical methods









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Optical methods



single reflection



double reflection







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Optical methods

van der Waals force measurement



Aspect, PRL 77, 1464 (1996)







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Optical methods

decoherence - incoherent photon scattering

$$U^{dip}(\vec{r}) = \frac{3\pi c^2}{2\omega_0^3} \frac{\Gamma}{\delta} I(\vec{r}) \qquad \Gamma^{sp}(\vec{r}) = \frac{3\pi c^2}{2\hbar\omega_0^3} \left(\frac{\Gamma}{\delta}\right)^2 I(\vec{r})$$

$$p^{sp} = \int_{-\infty}^{\infty} \Gamma^{sp}(t)dt \qquad \qquad \frac{m}{2} \left(\frac{dz}{dt}\right)^2 + U^{dip}(z) = E_{\perp}$$

$$U_{dip}(z) = \frac{\hbar\delta}{2} \ln\left(1 + \frac{\frac{\Omega_1^2(z)}{2}}{\delta^2 + \frac{\Gamma^2}{4}}\right) \Gamma_{sp}(z) = \frac{\Gamma}{2} \frac{\frac{I(z)}{I_S}}{1 + \left(\frac{2\delta}{\Gamma}\right)^2 + \frac{I(z)}{I_S}} \quad \text{two-level atom} + \text{saturation}$$

$$p^{sp} = \frac{md}{\hbar} \frac{\Gamma}{\delta} v_{\perp}$$







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Optical methods

decoherence - incoherent photon scattering - radiation pressure









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Optical methods

photon scattering may be usefull – Sisyphus cooling

proposed by:



atoms climb up the high mountain but roll down the small hill...

 $\begin{array}{ll} \text{cooling efficiency} \\ \text{for single succesful} \\ \text{inelastic reflection:} \end{array} & \frac{\Delta E_{\perp}}{E_{\perp}} = \frac{2}{3} \frac{\Delta_{HFS}}{\delta + \Delta_{HFS}} \approx 0.47 \end{array}$







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- one of the ways of getting 2D degenerate gases
- 2D-BEC investigation of vortices and solitons (different properties than in 3D)
- investigation of atom-surface interactions







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Outlook

- further development of atom chips (including magnets) and multi-layer structures
- integration with other fields like micro-optics and photonics
- manipulation of single atoms Bose-Einstein condensates or Fermi gases as reservoirs and coherent sources for atoms, atoms extracted on demand, quantum information
- atom optics matter wave engineering
- investigation of quantum gases in periodic potentials, waveguide potentials with strong radial confinement, disordered potentials, 1D systems, continuous transformation from 3D to 1D with access to the dimensional crossover
- ultracold chemistry on a chip where reactions are controlled by incident matter waves
- a tool to search for fundamental short-range interactions: interferometric measurements of non-Newtonian gravitational potentials at the micrometer length scale
- on the other hand: many efforts to fight against atom-surface interactions and decoherence
- are "free space" devices like optical lattices better?







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Outlook

Atom chips with vacuum system seem to be produced commercially.



The company is proud of having: Dana Anderson, Theodor Hänsch and Jakob Reichel as members...







Dutlook possible ways of development (1): surfce plasmon polaritons Au and Ag layer – structured micropotentials prism with metalic layer

another way: standing wave surface plasmon polaritons

to be constructed in Cracow



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Casimir-Polder potential



FIG. 1. (Color online) (a) Diagram, to scale, illustrating the aspect ratio of the condensate and typical oscillation position relative to the surface. The coordinate axis orientation and the direction of gravity are also indicated. (b) Typical data showing the radial dipole oscillation after expansion away from the surface.

Cornell, Phys. Rev. A 72, 033610 (2005)

$$\gamma_x \equiv \frac{\omega_o - \omega_x}{\omega_o} \simeq \frac{1}{2m\omega_o^2} \left\langle \partial_x F_{CP} \right\rangle$$

other experiments: Aspect, Phys. Rev. Lett. **77**, 1464 (1996) – optical mirror

Shimizu, Phys. Rev. A **71**, 052901 (2005) – grazing angle reflection of Ne* (quantum reflection)

DeKieviet, Phys. Rev. Lett. **91**, 193202 (2003) – grazing angle reflection of 3 He (quantum reflection)

Vuletic, Phys. Rev. Lett. **92**, 050404 (2004) – BEC stability on atom chip

Ketterle, Phys. Rev. Lett. **93**, 223201 (2004) – BEC normal reflection (quantum reflection)







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Casimir-Polder potential

Casimir-Polder force measurement: temperature dependence

thermal fluctuations near the surface:



The strength of the C-P force increases by a factor of nearly 3 as the substrate temperature doubles (nonequilibrium conditions).

Cornell, Phys. Rev. Lett. 98, 063201 (2007)











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Quantum reflection

- reflection of ultraslow metastable neon on the silicon and BK7 surface
- 1 mm/s 3 cm/s
- reflectivity: 30% @ 1 mm/s









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Summary

- surfaces may be a convenient platform for atom trapping and manipulation
- there are magnetic, optical, electrical and hybrid methods of confining atoms close to surfaces
- all the methods have their physical and technical limitations

milestones (surfaces as a tool):

- BEC in an atom chip
- 2D BEC in optical surface trap
- atom optics on atom chips, including interferometry

milestones (basic science):

- quantum reflection
- measurement of the Casimir-Polder force







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Współczesne doświadczenia z zimnymi atomami część III – some properties and applications of cold atoms

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Some experiments

- basic property of bosonic and fermionic gas
- Josephson junction
- superfluidity, BCS-BEC crossover
- vortices, solitons
- applications of cold atoms atomic clock







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Josephson junction

bosonic Josephson junction



$$z = (N_l - N_r)/(N_l + N_r)$$
 relative population
 $\phi = \phi_r - \phi_l$ relative phase

$$\dot{z} = -\sqrt{1-z^2}\sin\phi$$

 $\phi =$

$$\Lambda z + \frac{z}{\sqrt{1-z^2}}\cos\phi$$

analogy: mechanical nonrigid pendulum: tilt angle ϕ and angular momentum z and length sqrt(1-z^2)

Oberthaler, PRL 95, 010402 (2005)

dynamics









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Josephson junction

bosonic Josephson junction











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Quantum pressure

quantum pressure



sympathetic cooling

Hulet, Science 291, 2570 (2001)







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Atomic clock



Allan deviation:

$$\sigma_y(\tau) \approx \left\langle \frac{\Delta \nu_{rms}}{\nu_0} \right\rangle_{\tau} \approx \frac{\Delta \nu}{\pi \nu_0} \sqrt{\frac{T}{\tau N}}$$

 Δv – spectral width of the transition

- N number of atoms
- T time for measuring the line frequency
- ν_0 transition frequency
- τ averaging time



