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# STRINGY INSTANTONS ON RIGID MAGNETISED BRANES

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work in collaboration with  
Cezar Condeescu, Emilian Dudas and Michael Lennek

NPB 818 (2009) 52 [arXiv:0902.1694]

## $T^6 / \mathbb{Z}_2 \times \mathbb{Z}'_2$ orientifolds with discrete torsion

- O-plane geography
- Non-Supersymmetric BSB vacua
- Supersymmetric vacua with magnetised branes  
(or, alternatively, branes at angles)
- Rigid instantons
- Examples
- Conclusions & speculations

*related talks: Bianchi, Uranga, Weigand, Richter, Cvetič, ...*

Why are stringy instantons interesting?

If they exist in a given theory, they will play a role!  
Therefore, their role is worth to be studied.

## Why are stringy instantons interesting?

### Phenomenologically

they may induce non-perturbative corrections to low-energy couplings. Although these corrections are typically negligible in a perturbative framework, they may nevertheless represent leading contributions to given quantities if symmetries forbid classical and quantum operators.

$$\mathcal{W} = e^{-S_{\text{inst}}} \prod_i \Phi_i$$

where, chiral fields have charges  $Q_i$  wrt anomalous  $U(1)$ 's, and

$$S_{\text{inst}} \rightarrow S_{\text{inst}} + \Lambda \sum_i Q_i$$

# Why are stringy instantons interesting?

## Phenomenologically

- Generation of perturbatively forbidden couplings
  - generation of Majorana neutrino masses;
  - Higgs term in *MSSM*;
  - top Yukawa couplings in *SU(5) GUT's*;
- Moduli stabilisation
- Supersymmetry breaking;
- ....

[Ibanez, Uranga, Blumenhagen, Cvetič, Weigand, Richter, Bianchi, Fucito, Morales, Lerda, Frau, Billò, Pesando, Ferro, Gallot, Dudas, Camara, Argurio, Ferretti, Bertolini, Kachru, Maillard, Pradisi, Schmidt-Sommerfeld, Akerblom, Petersson, Halverson, Garcia-Extebarria, ....]

# Why are stringy instantons interesting?

## Theoretically

test of heterotic  $SO(32)$  - type I duality

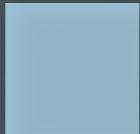
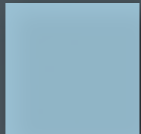
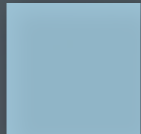
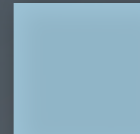




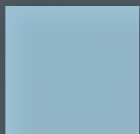
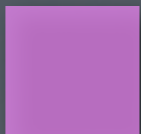
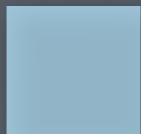
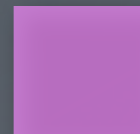




heterotic	type I
$\alpha'$ corrections	E1 branes
NS5 branes	E5 branes

[Camara, Dudas, Maillard, Pradisi]

$T^6 / \mathbb{Z}_2 \times \mathbb{Z}'_2$  IIB orientifolds

$\mathbb{Z}_2 \ni g : (z_1, z_2, z_3) \rightarrow (z_1, -z_2, -z_3)$

$\mathbb{Z}'_2 \ni h : (z_1, z_2, z_3) \rightarrow (-z_1, -z_2, z_3)$

0		g		h		gh	
	0		0		0		0
0		g		h		gh	
	g		g		g		g
0		g		h		gh	
	h		h		h		h
0		g		h		gh	
	gh		gh		gh		gh

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$$\mathcal{L} = \sum_{\alpha, \beta} \alpha \begin{array}{c} \blacksquare \\ \beta \end{array} + \epsilon \sum_{\gamma, \delta} \gamma \begin{array}{c} \blacksquare \\ \delta \end{array}$$

$\epsilon = \pm 1$  is related to discrete torsion and, clearly, affects massless and massive spectra



# $T^6 / \mathbb{Z}_2 \times \mathbb{Z}'_2$ IIB orientifolds


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$\epsilon = \pm 1$  is related to discrete torsion and, clearly, affects massless and massive spectra

1. changing the GSO projection of the oriented IIB string ( $h_{1,1} \leftrightarrow h_{2,1}$ )
2. determining the type of orientifold planes introduced


In fact, in the presence of discrete torsion ( $\epsilon = -1$ ) ....

	space time	$Z_1$	$Z_2$	$Z_3$
O9 <sub>-</sub> planes				
O5 <sup>1</sup> <sub>-</sub> planes				
O5 <sup>2</sup> <sub>-</sub> planes				
O5 <sup>3</sup> <sub>+</sub> planes				






In fact, in the presence of discrete torsion ( $\epsilon = -1$ ) ....


	tension	charge
O <sub>-</sub> planes	-	-
O <sub>+</sub> planes	+	+

In fact, in the presence of discrete torsion ( $\epsilon = -1$ ) ....

	space time	$Z_1$	$Z_2$	$Z_3$
O9 <sub>-</sub> planes				
O5 <sup>1</sup> <sub>-</sub> planes				
O5 <sup>2</sup> <sub>-</sub> planes				
O5 <sup>3</sup> <sub>+</sub> planes				


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O5 <sup>3+</sup> <sub>+</sub> planes				

	space time	$Z_1$	$Z_2$	$Z_3$
D9 branes				
D5 <sup>1</sup> branes				
D5 <sup>2</sup> branes				
$\overline{D5^3}$ branes				

Stable Brane Supersymmetry Breaking Vacuum Configuration

In fact, in the presence of discrete torsion ( $\epsilon = -1$ ) ....

	space time	$Z_1$	$Z_2$	$Z_3$
O9 <sub>-</sub> planes				
O5 <sup>1</sup> <sub>-</sub> planes				
O5 <sup>2</sup> <sub>-</sub> planes				
O5 <sup>3</sup> <sub>+</sub> planes				

	space time	$Z_1$	$Z_2$	$Z_3$
D9 branes		$H_1$	$H_2$	$H_3$

Supersymmetry condition:  $H_1 + H_2 + H_3 = H_1 H_2 H_3$

$$T_{\text{eff}} = T_{\text{D9}} \int (1 - H_2 H_3 - H_3 H_1 - H_1 H_2)$$

$H_1, H_2 > 0, H_3 < 0$  Stable Supersymmetry Vacuum Configuration

[Dudas, Timirgaziu; Blumenhagen, Cvetič, Marchesano, Shiu]

Using standard techniques one can compute the spectrum of open-string excitations on the magnetised D9 branes

$$G_{\text{CP}} = \prod_a U(p_a) \times \prod_\alpha U(q_\alpha)$$

together with varying families of chiral matter in bi-fundamental and rank-2 (anti)symmetric representations **but NO adjoint chiral multiplets**

$\mathbf{Z}_2 \times \mathbf{Z}_2'$  orbifold with discrete torsion have Hodge numbers  $(h_{11}, h_{21}) = (3, 51)$

Eight 3-cycles are inherited from the covering six-torus. The remaining 3-cycles originate from the twisted sectors and have the topology of  $S^1 \times S^2$  where  $S^1$  is a 1-cycle of the fixed torus while  $S^2$  corresponds to the 2-cycle of the blown-up orbifold singularities.

The twisted 3-cycles (*aka rigid cycles*) are localised on orbifold singularities and thus cannot be deformed

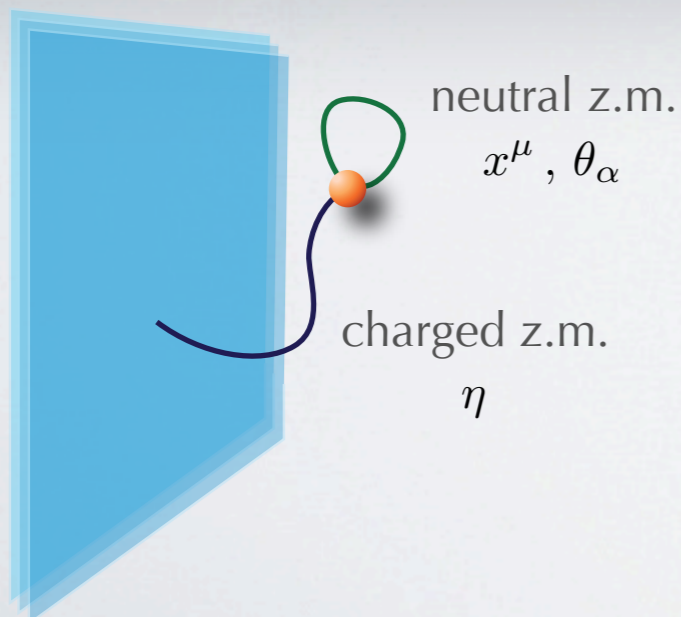
# Euclidean-brane instantons

	s.t.	$z_1$	$z_2$	$z_3$	$G_{CP}$	minimal z.m.
E5	•	■	■	■	U(n)	4
E1 <sub>1</sub>	•	■	•	•	U(n)	4
E1 <sub>2</sub>	•	•	■	•	U(n)	4
E1 <sub>3</sub>	•	•	•	■	SO(n)	2



# Euclidean-brane instantons

	s.t.	z <sub>1</sub>	z <sub>2</sub>	z <sub>3</sub>	G <sub>CP</sub>	minimal z.m.
E5	•	■	■	■	U(n)	4
E1 <sub>1</sub>	•	■	•	•	U(n)	4
E1 <sub>2</sub>	•	•	■	•	U(n)	4
E1 <sub>3</sub>	•	•	•	■	SO(n)	2



$$\mathcal{S}_{\text{inst}} = \mathcal{S}_{\text{neutral}}(\text{vol}) + \mathcal{S}_{\text{charged}}(\eta, \Phi_o)$$

$$\int [d\eta] e^{-\mathcal{S}_{\text{inst}}} \Rightarrow \mathcal{W}_{\text{np}} \sim e^{-\mathcal{S}_{\text{neutral}}} \prod_i \Phi_o^i$$

## Example ①

4 stacks of magnetised branes			
	"wrapping" numbers		
stack 1	(2,1)	(1,1)	(-1,1)
stack 2	(-2,1)	(-1,1)	(1,1)
stack 3	(0,1)	(0,1)	(0,1)
stack 4	(0,1)	(1,0)	(-1,0)

# Example 1

$$G_{CP} = U(2)^2 \times U(2)^2 \times USp(4)^2 \times USp(4)^2$$

mult	reps	field
1	$(\mathbf{2}, \mathbf{2}^*, 1, 1; 1, 1, 1, 1)$	$\Phi_{1\bar{2}}$
1	$(\mathbf{2}^*, \mathbf{2}, 1, 1; 1, 1, 1, 1)$	$\Phi_{\bar{1}2}$
12	$(\mathbf{1}^*, 1, 1, 1; 1, 1, 1, 1)$	$A^1$
12	$(1, \mathbf{1}^*, 1, 1; 1, 1, 1, 1)$	$A^2$
4	$(\mathbf{2}^*, \mathbf{2}^*, 1, 1; 1, 1, 1, 1)$	$\Phi_{\bar{1}\bar{2}}$
1	$(1, 1, \mathbf{2}, \mathbf{2}^*; 1, 1, 1, 1)$	$\Phi_{3\bar{4}}$
1	$(1, 1, \mathbf{2}^*, \mathbf{2}; 1, 1, 1, 1)$	$\Phi_{\bar{3}4}$
12	$(1, 1, \mathbf{1}, \mathbf{1}; 1, 1, 1, 1)$	$A^3$
12	$(1, 1, \mathbf{1}, \mathbf{1}; 1, 1, 1, 1)$	$A^4$
4	$(1, 1, \mathbf{2}, \mathbf{2}; 1, 1, 1, 1)$	$\Phi_{34}$
2	$(\mathbf{2}^*, 1, 1, 1; \mathbf{4}, 1, 1, 1)$	
2	$(1, \mathbf{2}^*, 1, 1; 1, \mathbf{4}, 1, 1)$	

.....

# Example 1

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.....

Euclidean instantons with 2 neutral z.m.

	reps	field
E1 <sub>o</sub>	$(\mathbf{1}, \mathbf{2}, 1, 1; 1, 1, 1, 1)$	$\eta_i^o$
E1 <sub>g</sub>	$(\mathbf{2}, 1, 1, 1; 1, 1, 1, 1)$	$\eta_i^g$
E1 <sub>f</sub>	$(1, 1, \mathbf{2}^*, 1; 1, 1, 1, 1)$	$\eta_i^f$
E1 <sub>h</sub>	$(1, 1, 1, \mathbf{2}^*; 1, 1, 1, 1)$	$\eta_i^h$

# Example 1

$$\mathcal{I}_{\text{neutral}} = T_3 + \sum_{a=1}^3 \alpha_a M_a$$

volume of the third  $T^2$

twisted moduli

$$\mathcal{I}_{\text{charged}} = \sum_{i,j} \eta_i^o A_{ij}^2 \eta_j^o + \sum_{i,j,k=1}^2 \eta_i^o \Phi_{12}^{ki} \Phi_{12}^{kj} \eta_j^o$$

Upon integration over charged zero modes

$$\mathcal{W}_{\text{np}} = e^{-\mathcal{I}_{\text{neutral}}} \sum_{i,j=1,2} \epsilon_{ij} \left[ A_{ij}^2 + \sum_{k=1,2} \Phi_{12}^{ki} \Phi_{12}^{kj} \right]$$

Linear terms in the superpotential may induce O’Raifeartaigh/Polony supersymmetry breaking, gauge mediation supersymmetry breaking, moduli stabilisation, ...

$$G_{\text{CP}} = U(2)^2 \times U(2)^2 \times USp(4)^2 \times USp(4)^2$$

mult	reps	field
1	( <b>2</b> , <b>2</b> <sup>*</sup> , 1, 1; 1, 1, 1, 1)	$\Phi_{1\bar{2}}$
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12	( <b>1</b> <sup>*</sup> , 1, 1, 1; 1, 1, 1, 1)	$A^1$
12	(1, <b>1</b> <sup>*</sup> , 1, 1; 1, 1, 1, 1)	$A^2$
4	( <b>2</b> <sup>*</sup> , <b>2</b> <sup>*</sup> , 1, 1; 1, 1, 1, 1)	$\Phi_{\bar{1}\bar{2}}$
1	(1, 1, <b>2</b> , <b>2</b> <sup>*</sup> ; 1, 1, 1, 1)	$\Phi_{3\bar{4}}$
1	(1, 1, <b>2</b> <sup>*</sup> , <b>2</b> ; 1, 1, 1, 1)	$\Phi_{\bar{3}4}$
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.....

Euclidean instantons with 2 neutral z.m.

	reps	field
E1 <sub>o</sub>	( <b>1</b> , <b>2</b> , 1, 1; 1, 1, 1, 1)	$\eta_i^o$
E1 <sub>g</sub>	( <b>2</b> , 1, 1, 1; 1, 1, 1, 1)	$\eta_i^g$
E1 <sub>f</sub>	(1, 1, <b>2</b> <sup>*</sup> , 1; 1, 1, 1, 1)	$\eta_i^f$
E1 <sub>h</sub>	(1, 1, 1, <b>2</b> <sup>*</sup> ; 1, 1, 1, 1)	$\eta_i^h$

# Example 1

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volume of the third  $T^2$

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Upon integration over charged zero modes

$$\delta \mathcal{S}_{\text{neutral}} = 2\Lambda_2$$

$$\mathcal{W}_{\text{np}} = e^{-\mathcal{S}_{\text{neutral}}} \sum_{i,j=1,2} \epsilon_{ij} \left[ A_{ij}^2 + \sum_{k=1,2} \Phi_{12}^{ki} \Phi_{12}^{kj} \right]$$

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E1 <sub>h</sub>	(1, 1, 1, <b>2</b> <sup>*</sup> ; 1, 1, 1, 1)	$\eta_i^h$

## Example ②

2 stacks of magnetised branes			
	"wrapping" numbers		
stack 1	(1,1)	(1,1)	(-1,1)
stack 2	(-1,1)	(-1,1)	(1,1)

$\eta_i^o$

$\eta_i^g$

$\eta_i^f$

$\eta_i^h$



## Example ②

$G_{CP} = U(4)^2 \times U(4)^2$		
mult	reps	field
1	$(\mathbf{4}^*, \mathbf{4}, 1, 1)$	
1	$(\mathbf{4}, \mathbf{4}^*, 1, 1)$	
1	$(1, 1, \mathbf{4}^*, \mathbf{4})$	
1	$(1, 1, \mathbf{4}, \mathbf{4}^*)$	
8	$(\mathbf{6}^*, 1, 1, 1)$	$A^1$
8	$(1, \mathbf{6}^*, 1, 1)$	$A^2$
8	$(1, 1, \mathbf{6}, 1)$	$A^3$
8	$(1, 1, 1, \mathbf{6})$	$A^4$

$\eta_i^o$

$\eta_i^g$

$\eta_i^f$

$\eta_i^h$

## Example ②

$G_{CP} = U(4)^2 \times U(4)^2$		
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8	$(1, 1, \mathbf{6}, 1)$	$A^3$
8	$(1, 1, 1, \mathbf{6})$	$A^4$

Euclidean instantons with 2 neutral z.m.		
	reps	field
E1 <sub>o</sub>	$(1, \mathbf{4}, 1, 1)$	$\eta_i^o$
E1 <sub>g</sub>	$(\mathbf{4}, 1, 1, 1)$	$\eta_i^g$
E1 <sub>f</sub>	$(1, 1, \mathbf{4}^*, 1)$	$\eta_i^f$
E1 <sub>h</sub>	$(1, 1, 1, \mathbf{4}^*)$	$\eta_i^h$

## Example ②

$$\mathcal{I}_{\text{neutral}} = T_3 + \sum_{a=1}^3 \alpha_a M_a$$

volume of the third  $T^2$

twisted moduli

$$\mathcal{I}_{\text{charged}} = \sum_{i,j=1}^4 \eta_i^o A_{ij}^2 \eta_j^o$$

Upon integration over charged zero modes

$$\mathcal{W}_{\text{np}} = e^{-\mathcal{I}_{\text{neutral}}} \sum_{i,j,k,l=1}^4 \epsilon_{ijkl} A_{ij}^2 A_{kl}^2$$

non-perturbative mass term for the  $A$ 's

$$G_{\text{CP}} = U(4)^2 \times U(4)^2$$

mult	reps	field
1	$(\mathbf{4}^*, \mathbf{4}, 1, 1)$	
1	$(\mathbf{4}, \mathbf{4}^*, 1, 1)$	
1	$(1, 1, \mathbf{4}^*, \mathbf{4})$	
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8	$(1, 1, 1, \mathbf{6})$	$A^4$

Euclidean instantons with 2 neutral z.m.

	reps	field
E1 <sub>o</sub>	$(1, \mathbf{4}, 1, 1)$	$\eta_i^o$
E1 <sub>g</sub>	$(\mathbf{4}, 1, 1, 1)$	$\eta_i^g$
E1 <sub>f</sub>	$(1, 1, \mathbf{4}^*, 1)$	$\eta_i^f$
E1 <sub>h</sub>	$(1, 1, 1, \mathbf{4}^*)$	$\eta_i^h$

## Example ②

The gauge theory on the D9 branes, actually divides into two non-interacting sectors.

The beta functions for the non-Abelian couplings are vanishing at one loop and it is tempting to speculate about the existence of an IR conformal fixed point.

[Leigh, Strassler]

Conformal invariance would then be broken by non-perturbative effects  $mAA$  at a hierarchically small energy scale, thus offering an alternative solution to the hierarchy problem.

[Frampton, Vafa]

$G_{CP} = U(4)^2 \times U(4)^2$		
mult	reps	field
1	$(\mathbf{4}^*, \mathbf{4}, 1, 1)$	
1	$(\mathbf{4}, \mathbf{4}^*, 1, 1)$	
1	$(1, 1, \mathbf{4}^*, \mathbf{4})$	
1	$(1, 1, \mathbf{4}, \mathbf{4}^*)$	
8	$(\mathbf{6}^*, 1, 1, 1)$	$A^1$
8	$(1, \mathbf{6}^*, 1, 1)$	$A^2$
8	$(1, 1, \mathbf{6}, 1)$	$A^3$
8	$(1, 1, 1, \mathbf{6})$	$A^4$

# CONCLUSIONS

Stringy instantons play a crucial role in generating  
hierarchically small masses,  
low-energy supersymmetry breaking,  
conformal symmetry breaking,

.....

They are also crucial for testing string dualities,

.....

# SPECULATIONS

Our driving motivation was trying to connect non-tachyonic non-supersymmetric vacua with  $N=1$  supersymmetric vacua with magnetised D9 branes. In fact, both configurations share the same supersymmetric closed-string spectrum, with identical O-plane structure.

It is reasonable to believe that, though classically stable, the non-supersymmetric vacuum is actually metastable and will quantum mechanically decay to the supersymmetric solution.

This is actually what happens in similar  $N=2$  set-ups

[C.A., Dudas]

# SPECULATIONS

The non-supersymmetric model contains stacks of  $D5_{1,2}$  branes and  $D5_3$  branes in addition to  $D9$  ones. All  $D5$  branes can actually be seen as zero-size gauge instantons on the  $D9$  branes.

[Witten]

Instantons would energetically prefer to expand to their maximal size within the  $D9$  branes, and because of conservation of topological charges, the original  $D5$  (anti)branes are actually converted into diluted magnetic fluxes on the  $D9$ 's.

***It is tempting to believe that this (highly non-trivial) dynamical process is triggered by E-brane instantons***