

# Reevaluating the WIMP Miracle

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Scott Watson

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and **Syracuse University**

## Acknowledgments:

Bobby Acharya (ICTP)

Piyush Kumar (Berkeley)

Phill Grajek, Gordy Kane, Dan Phalen, and Aaron Pierce (Michigan)

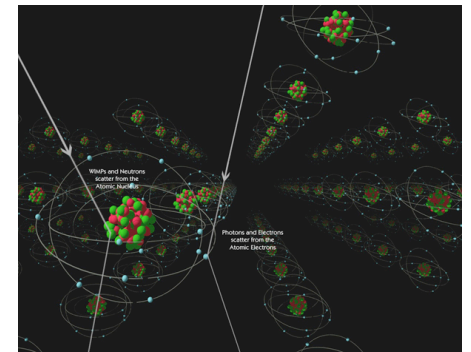
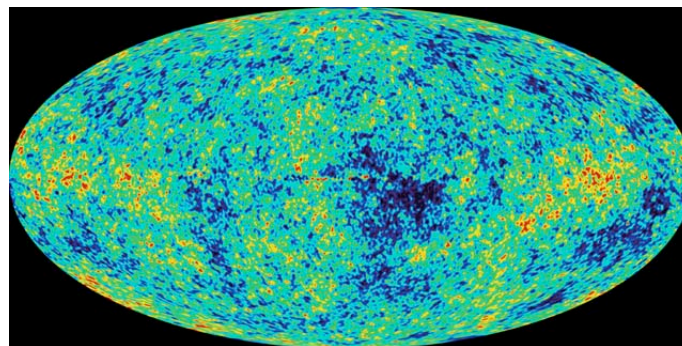
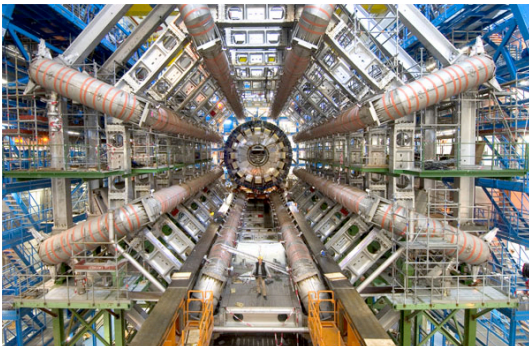
# Conclusion

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Thermal dark matter from “realistic” models of string phenomenology could prove challenging.

This is good news, because non-thermal dark matter (in contrast to thermal production) could provide a new window on probing string based models.

A complete understanding of dark matter requires a concordance approach (cosmology, particle experiment, and fundamental theory)

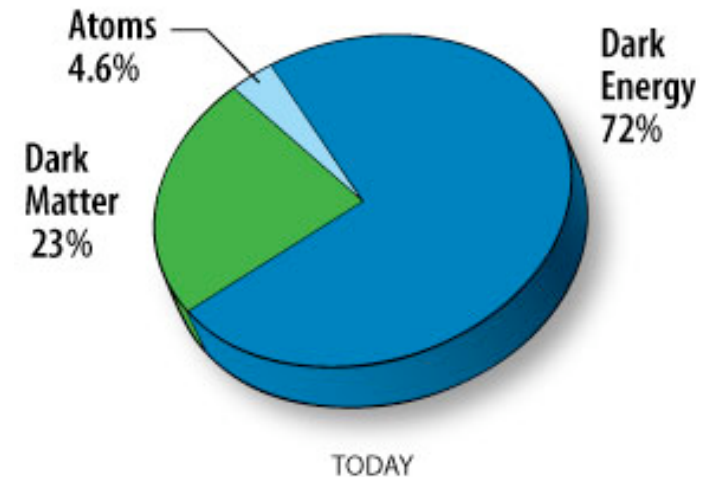


# Precision Cosmology

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## Cosmic Energy Budget

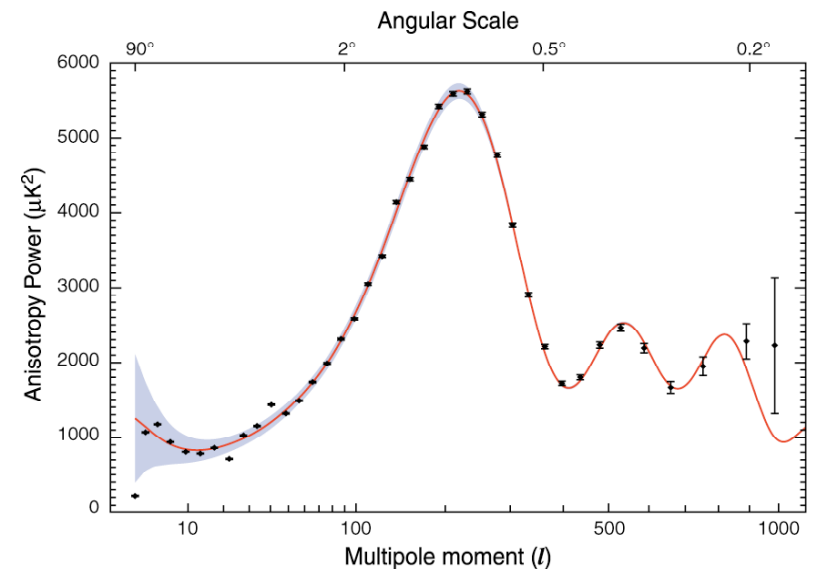
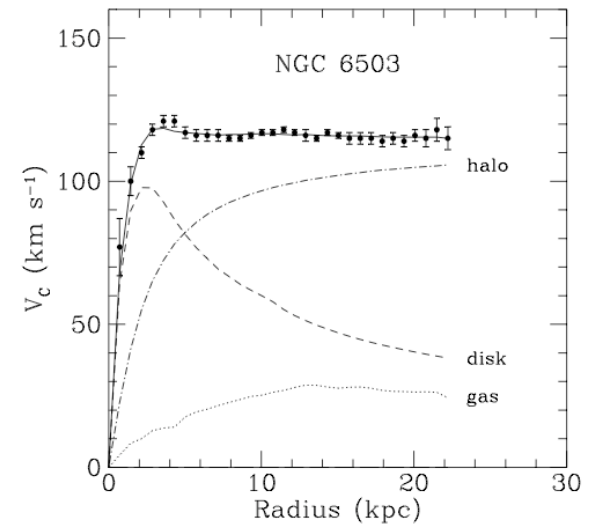
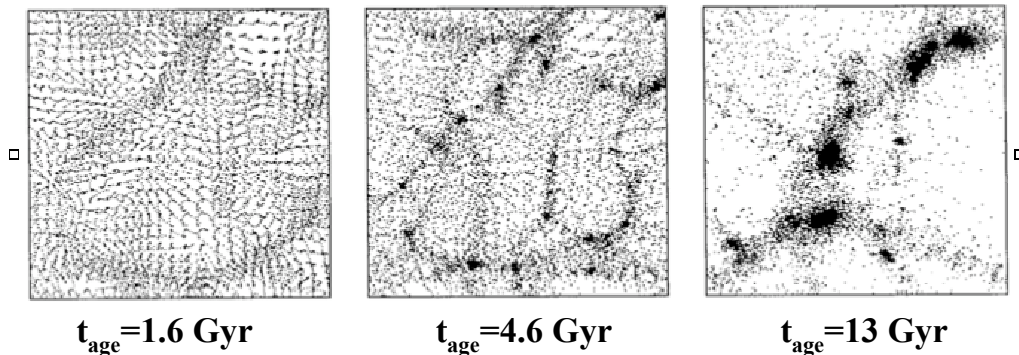
- Dark Energy 72%
- Dark Matter 23%
- Baryons 5%
- Early universe remarkably homogeneous
- Very small density contrast (1:100,000) at time of decoupling of CMB



All suggest physics beyond the standard model.

# Cosmological Dark Matter

- Rotation curves
- CMB / LSS / Supernovae
- Evolution of LSS
- Gravitational Lensing





# Cosmological Dark Matter

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## Cosmological Properties:

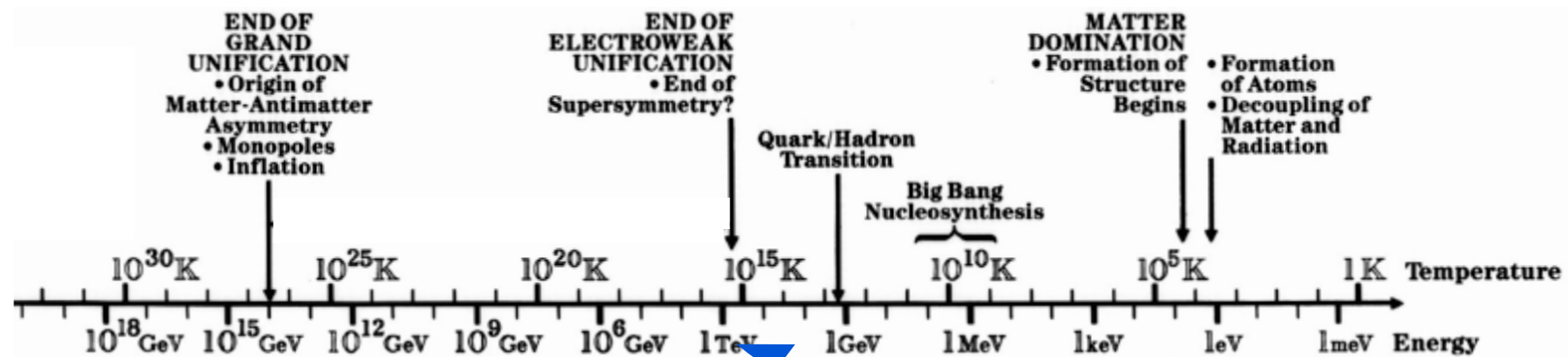
- **Cold** ( Non-relativistic when structure forms )
- **Dark** (electrically neutral)
- **Stable** (or very long-lived)
- **Weakly interacting with SM particles**

“WIMPs”

$$\Omega_{dm} \equiv \frac{\rho_{dm}}{\rho_{total}} = 0.233 \pm 0.013$$

How is dark matter produced?

# The “WIMP” Miracle

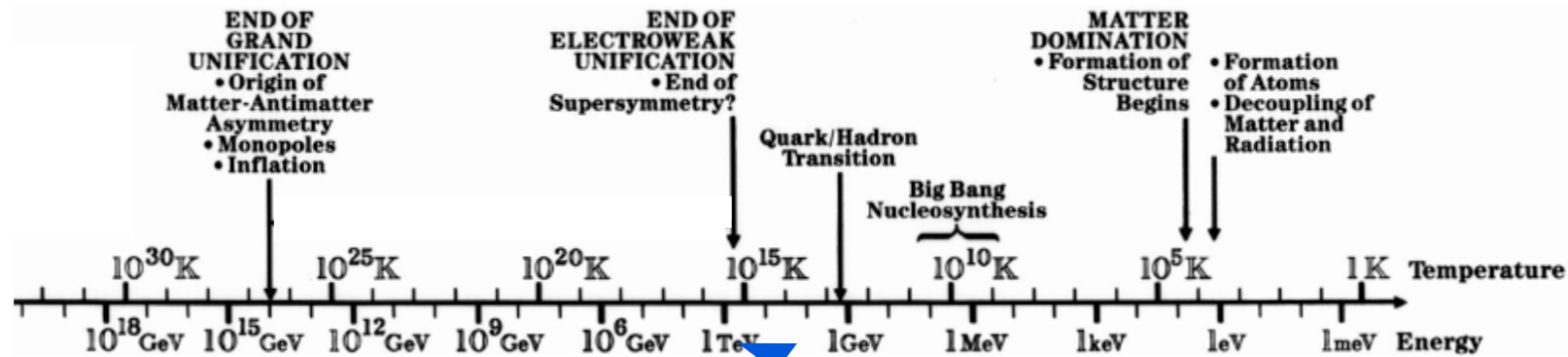


Dark Matter  
“freezes out”

## Dark Matter Abundance from Thermal Production

$$\Omega_{dm} = 0.23 \times \left( \frac{10^{-26} \text{ cm}^3 \cdot \text{s}^{-1}}{\langle \sigma v \rangle} \right)$$

# The “WIMP” Miracle



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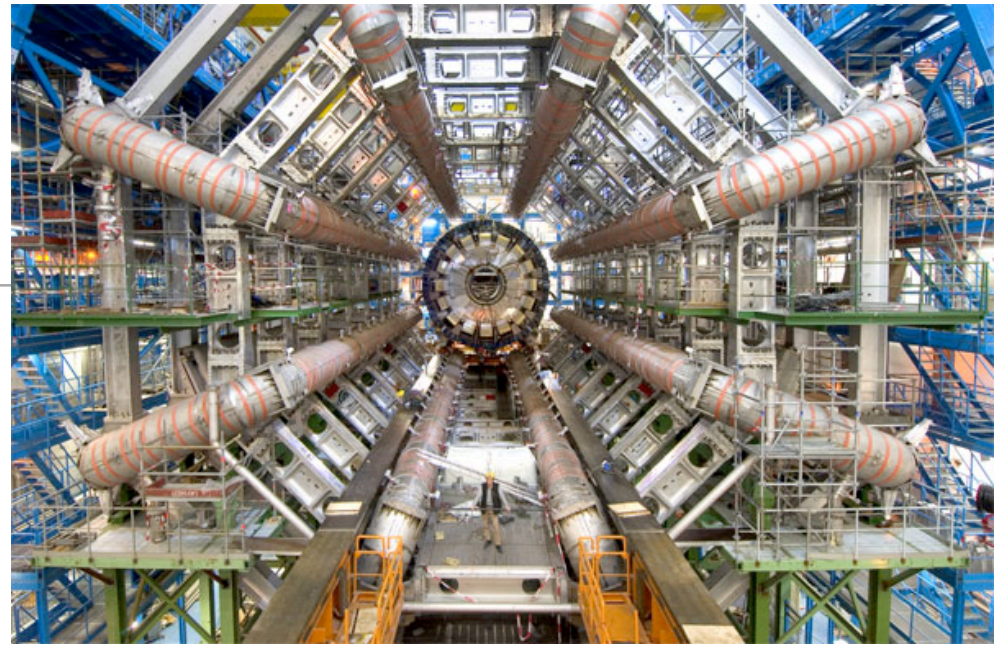
Cosmological Measurement

Weak Scale Physics

As anticipated from particle theory

# LHC and Dark Matter

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LHC will probe our theories of EWSB.

$$\Omega_{dm} = 0.23 \times \left( \frac{10^{-26} \text{ cm}^3 \cdot \text{s}^{-1}}{\langle \sigma v \rangle} \right)$$

Measure dark matter mass/interaction

--> **End game?**

Other probes of Dark Matter

# Indirect Detection -- An Overview

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## Prior to BBN

$$\Gamma_{ann} \sim n^2 \langle \sigma v \rangle \quad \Gamma_{ann} < H$$

Inside our galaxy the density can again reach levels that lead to annihilations

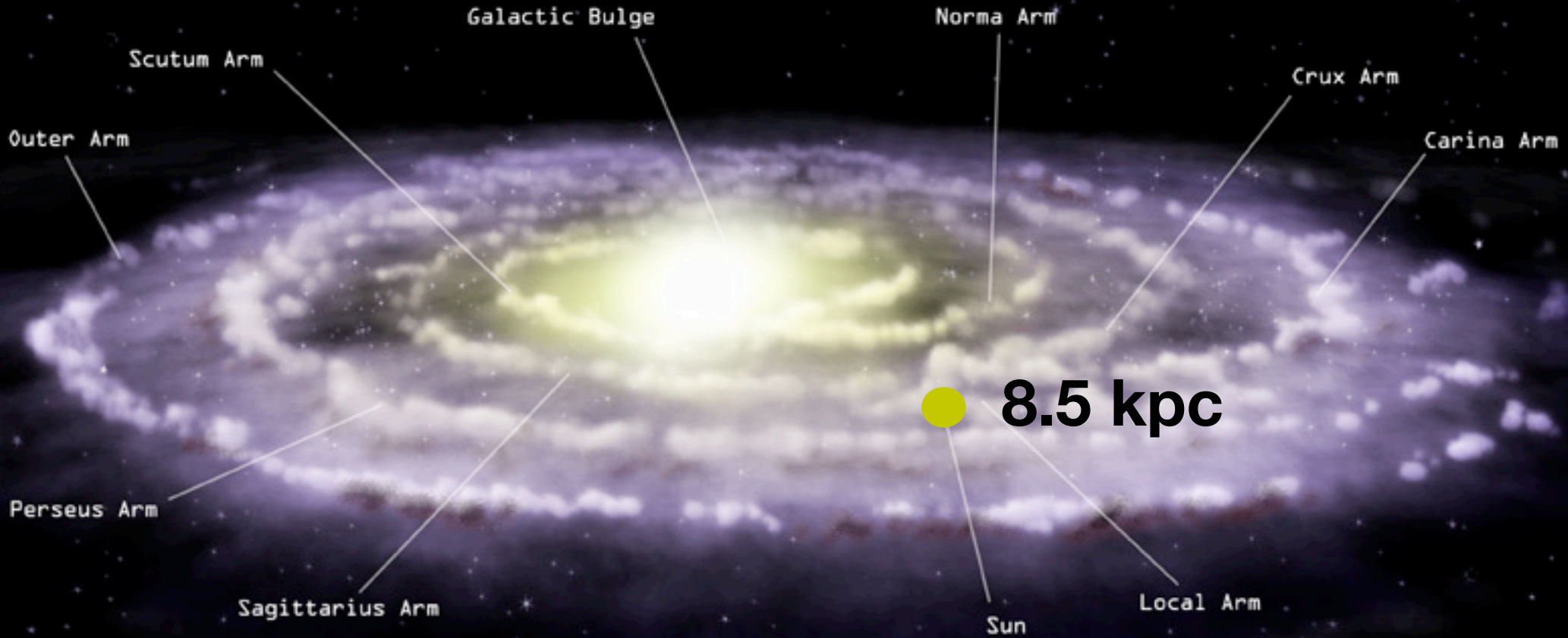
Many cosmic rays -- focus on anti-matter (rare)

$$e^+ \quad \bar{p} \quad \gamma \quad \nu$$



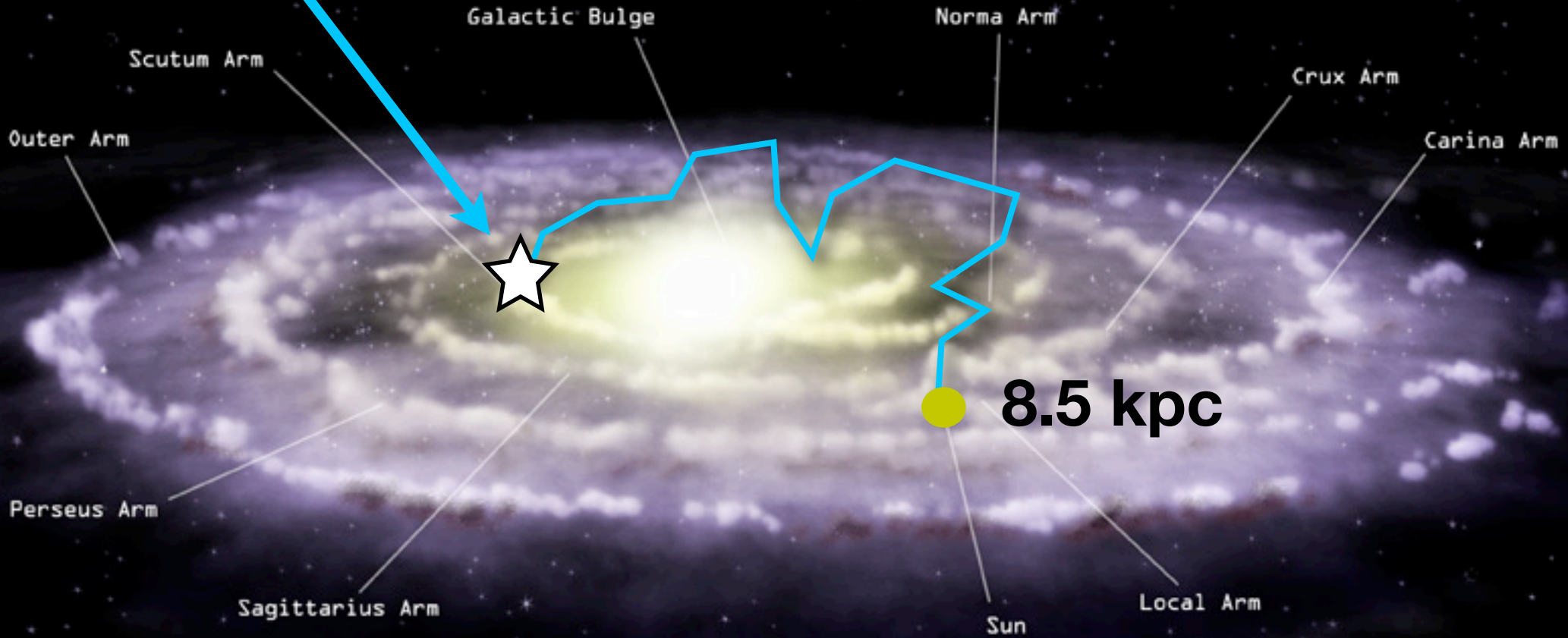
# Indirect Detection of Dark Matter

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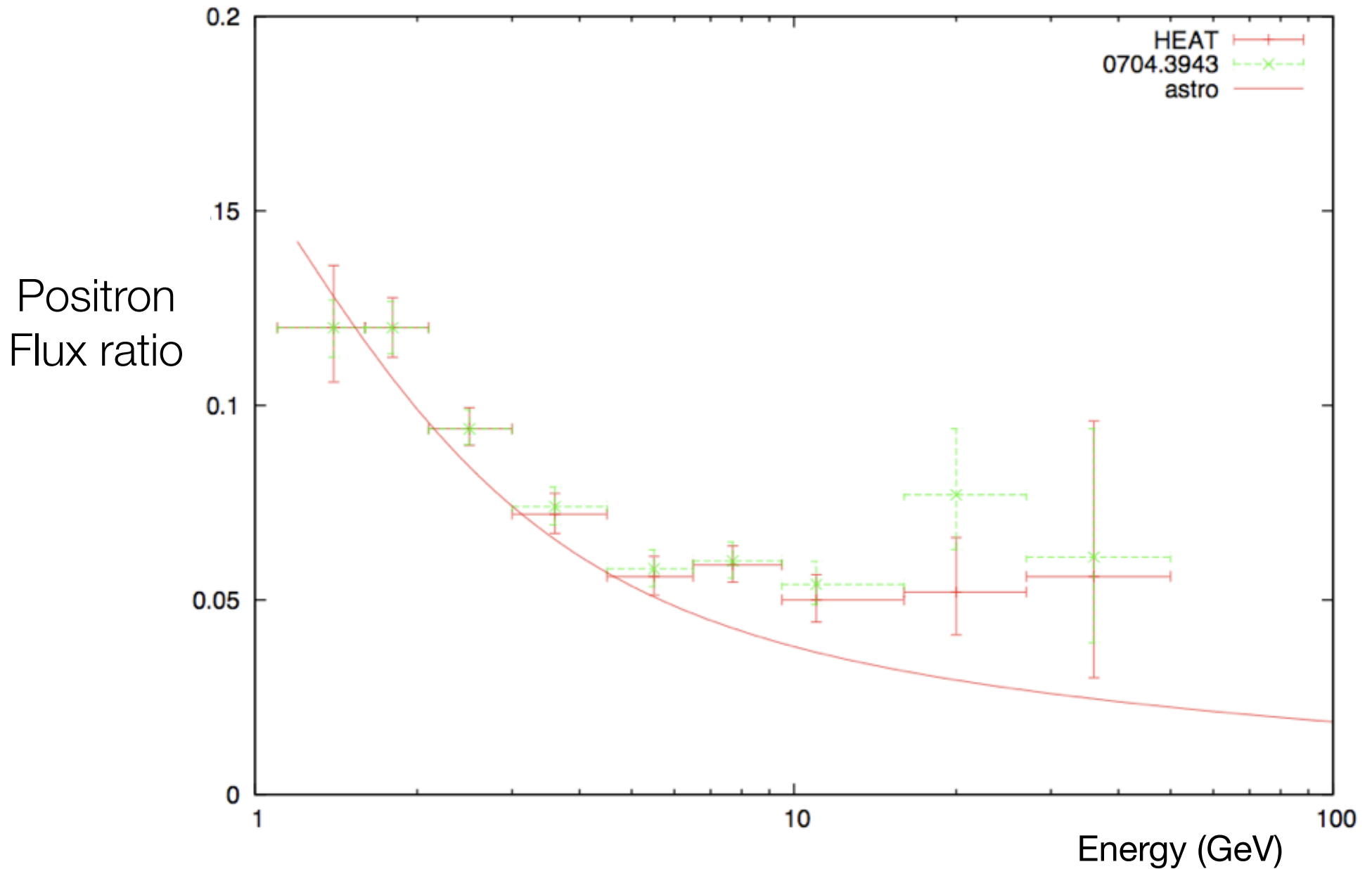


# Indirect Detection of Dark Matter

Dark Matter  
Annihilates



# Cosmic-ray Flux in Positrons



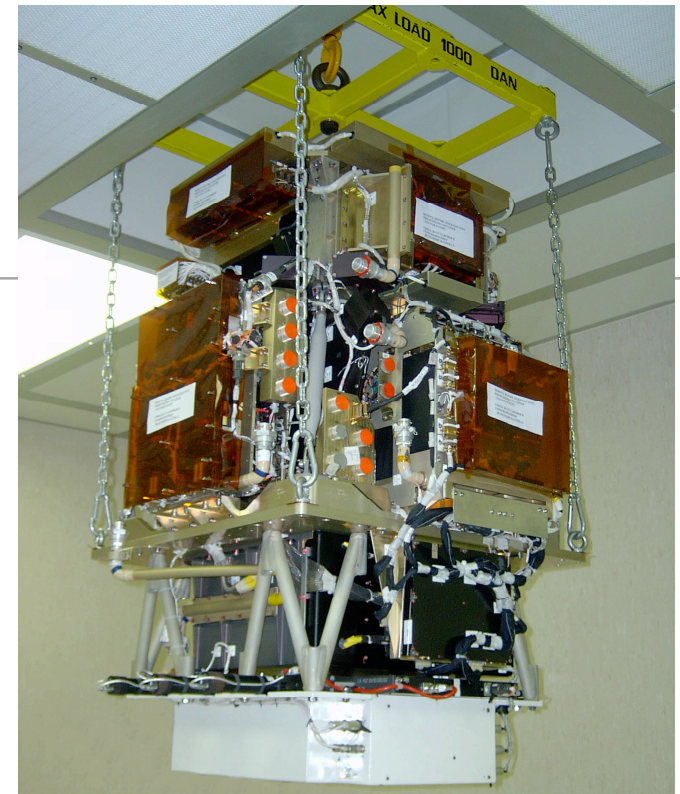


# PAMELA

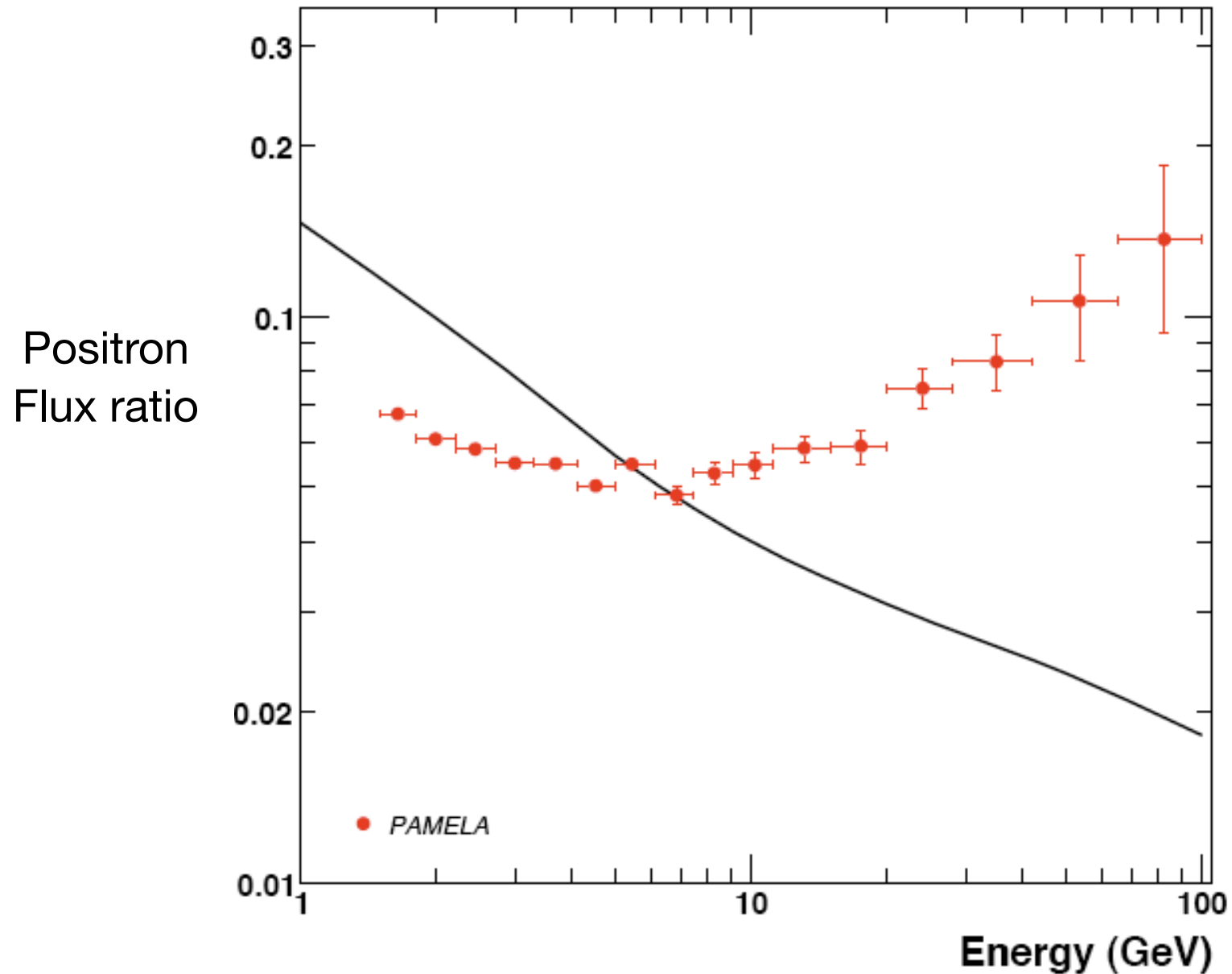
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## Payload for Antimatter Matter Exploration and Light Nuclei Astrophysics

- Satellite mission -- online as June 2008
- Positron data reported from 50 MeV - 100 GeV (will go to 270 GeV max)
- Anti-proton data from 80 MeV up to 190 GeV (consistent with existing data, e.g. BESS)

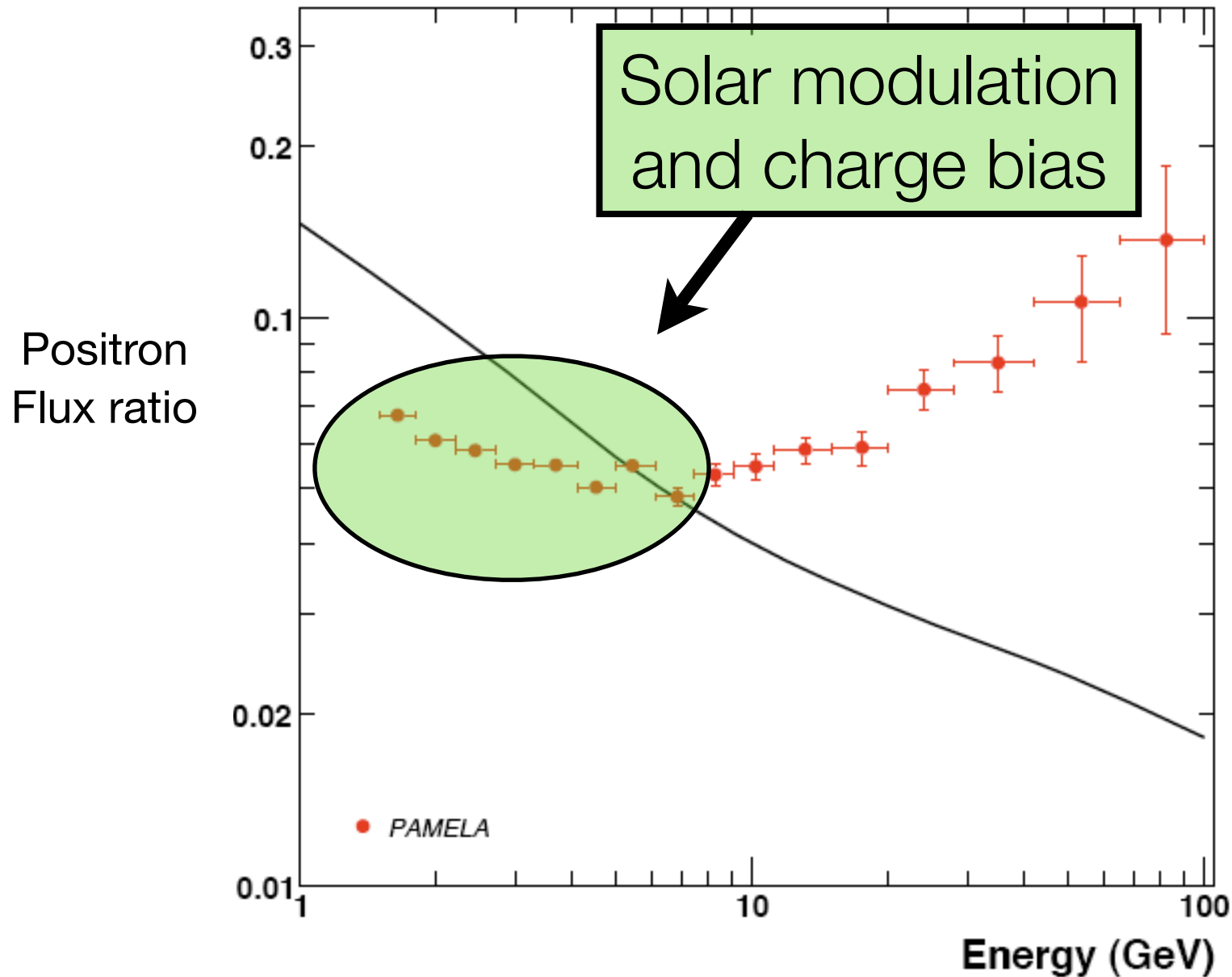


# A Possible Positron Excess



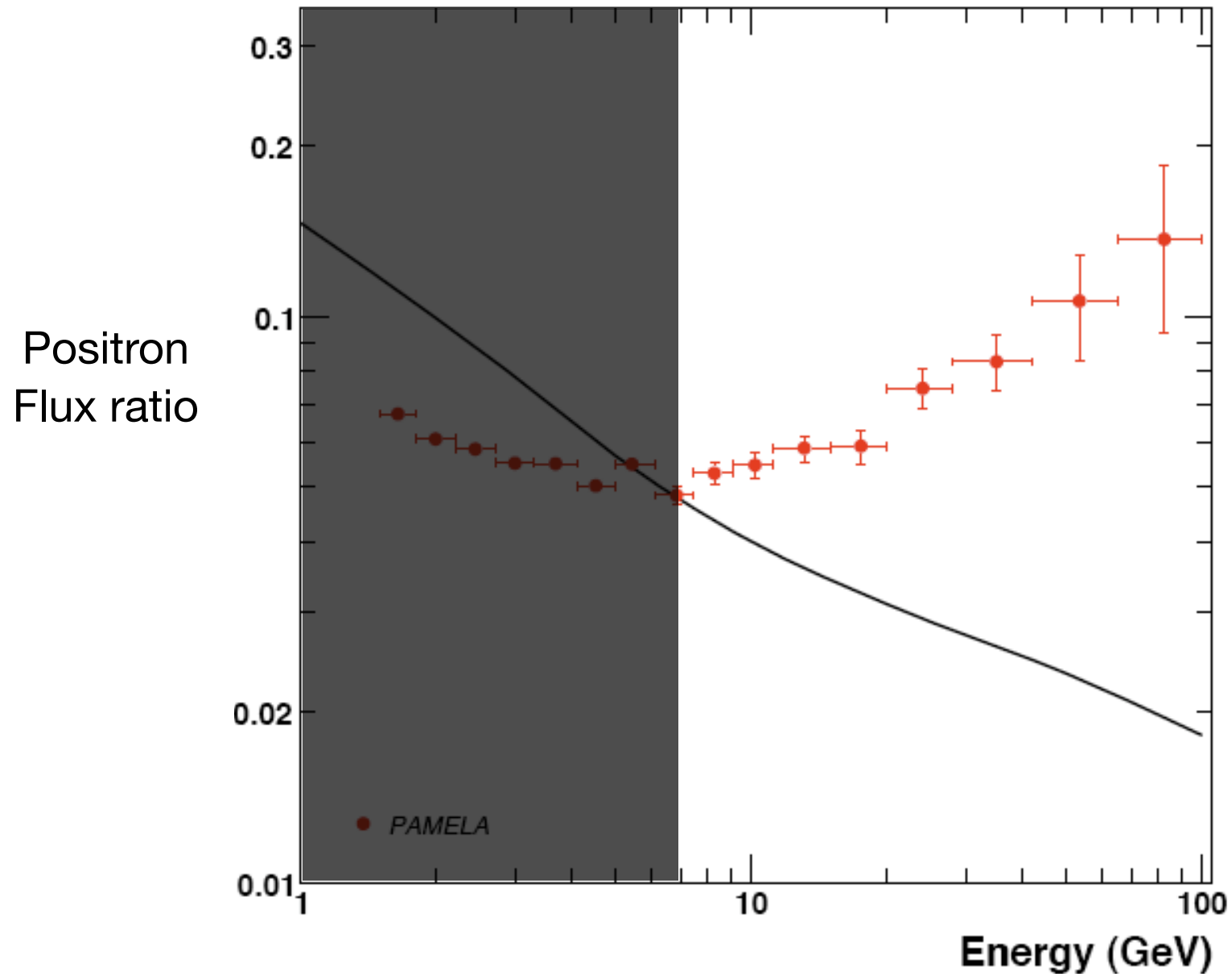


# A Possible Positron Excess





# A Possible Positron Excess



# PAMELA -- Indirect Evidence for WIMPs?

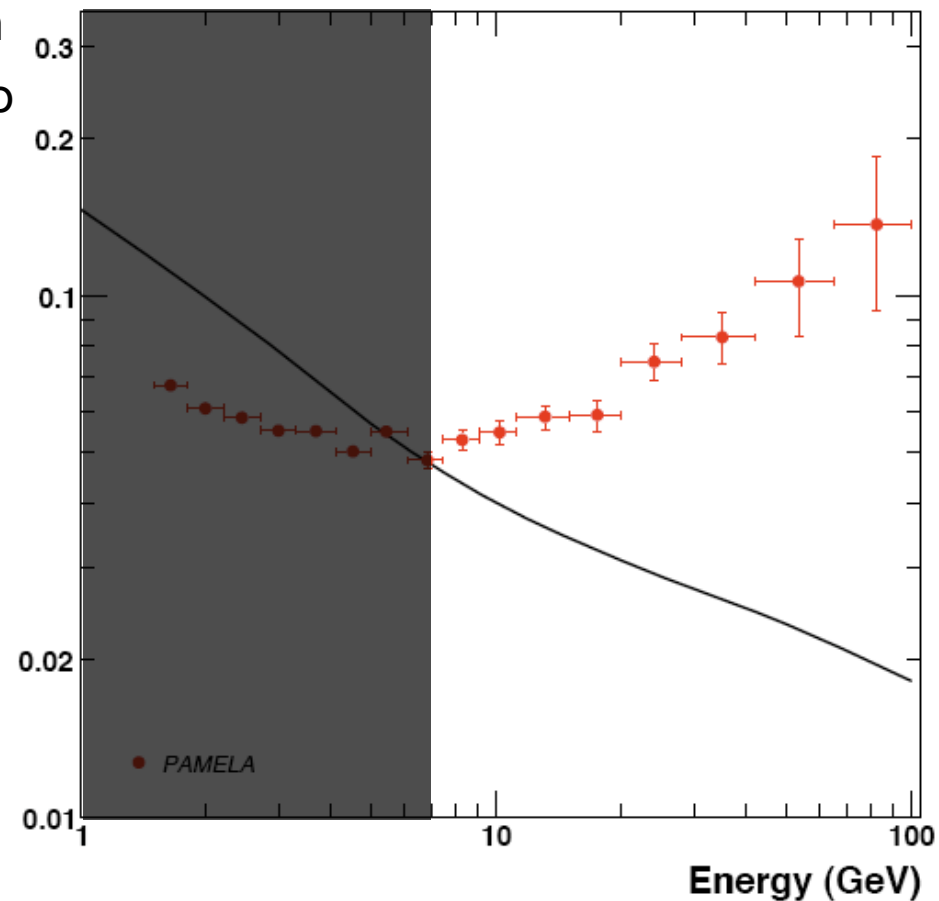
Expected Positron Flux

$$\Phi \sim \underbrace{\frac{\langle \sigma v \rangle}{m_X^2}}_{\text{Microphysics}} \times \underbrace{\rho^2(r)}_{\text{Astrophysics}}$$

Cosmological Constraint

$$\Omega_{dm} = 0.23 \times \left( \frac{10^{-26} \text{ cm}^3 \cdot \text{s}^{-1}}{\langle \sigma v \rangle} \right)$$

Positron  
Flux ratio



**Flux many orders of magnitude too low**

# PAMELA -- Indirect Evidence for WIMPs?

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Expected Positron Flux

$$\Phi \sim \underbrace{\frac{\langle \sigma v \rangle}{m_X^2}}_{\text{Microphysics}} \times \underbrace{\rho^2(r)}_{\text{Astrophysics}}$$

## Important Considerations

- Astrophysical uncertainties: Halo profile, propagation, backgrounds
- Unknown astrophysical sources, e.g. Pulsars
- Proton contamination (10,000/1)

**Taken alone probably not a compelling case for dark matter**

Could another surprise be coming?

# The New York Times

April 1, 2010 Last Update: 6:38 PM ET

New York Partly Cloudy 42°F

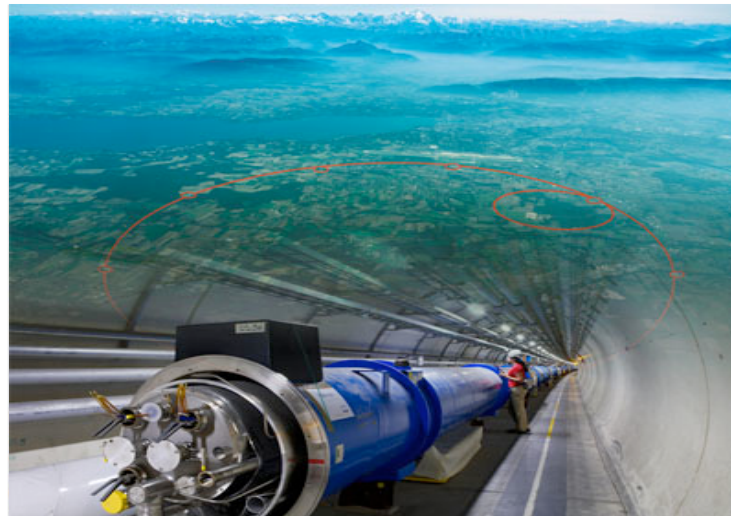
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[REAL ESTATE](#)  
[AUTOS](#)  
[ALL CLASSIFIEDS](#)

[WORLD](#)  
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## Obama Solves Global Financial Crisis and Brings World Peace

by Paul Krugman

President Obama addressed the nation today acknowledging that although his administration has successfully resolved the global financial crisis, restored the confidence of the American housing market, and brought world peace, that there is still much left to be accomplished. The president has promised to turn to more mundane issues such as establishing a legitimate college football playoff,



## Experimental Result Leads to Excitement and Controversy

by Dennis Overbye

$$\Omega_{cdm} = 0.002$$

To the physicist, the above expression succinctly summarizes the recent surprising results coming from the Large Hadron Collider (LHC) located in Geneva, Switzerland. The equation symbolically represents the amount of dark matter in the universe, which from the initial findings of the experiment seem to fall short of expectations coming from cosmological observation.

### OPINION »

#### Op-Ed: Restore the Senate's Treaty Power

America needs to maintain its sovereignty, write John R. Bolton and John Yoo.



- Krugman: Stimulus Plan  
[Comments \(418\)](#)
- Kristol: Why Israel Fights  
[Comments \(368\)](#)
- Cohen: Penn's Dangers  
[Comments \(130\)](#)
- [Editorial: Drug Money](#)  
[Comments \(69\)](#)

### ARTS »

#### A Leitmotif of Love, Memories and Secrets

Jayne Anne Phillips's novel fuses disparate influences into something utterly original.

#### Protecting Borders and Other Pursuits

A reality series about policing the borders is more homage than reportage.



### MARKETS » At close 01/05/2009

S.&P. 500	Dow	Nasdaq
9927.45	19927.45	8927.45
-4.35	-81.80	-4.18
-0.47%	-0.91%	-0.26%

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[nytimes.com/dealbook](http://nytimes.com/dealbook)

# Particle v.s. Cosmological Dark Matter

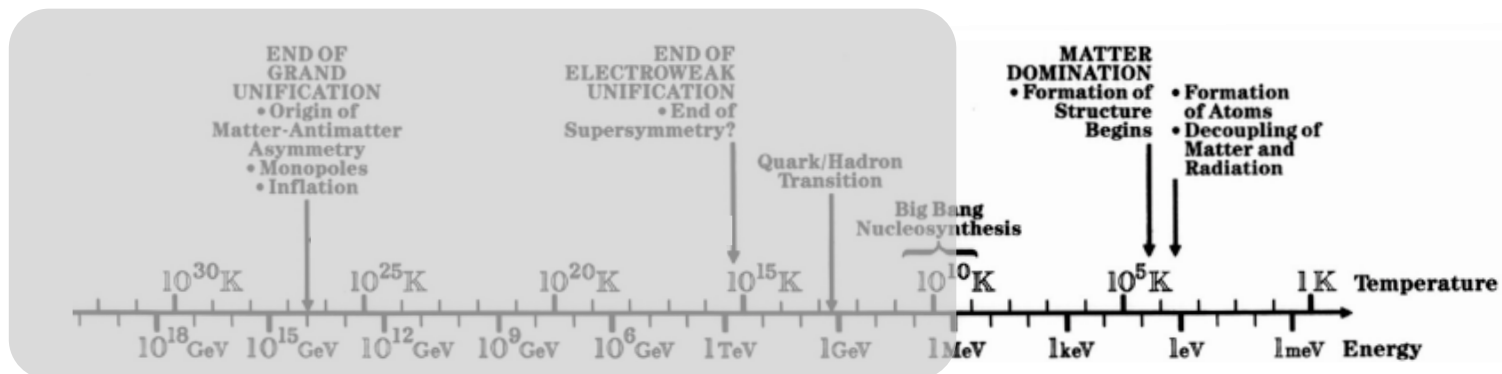
Review: G. Kane, S.W. arXiv:0807.2244

## Many explanations for a low relic density:

- Many additional dark matter particles possible in addition to WIMPs ( e.g. neutrinos / axions )

$$\Omega_{cdm}^{Total} = \sum_i \Omega_{cdm}^{(i)}$$

- Other light particles can result in a lower relic density (coannihilations)
- [Thermal origin](#) of dark matter may be [too simplistic](#)

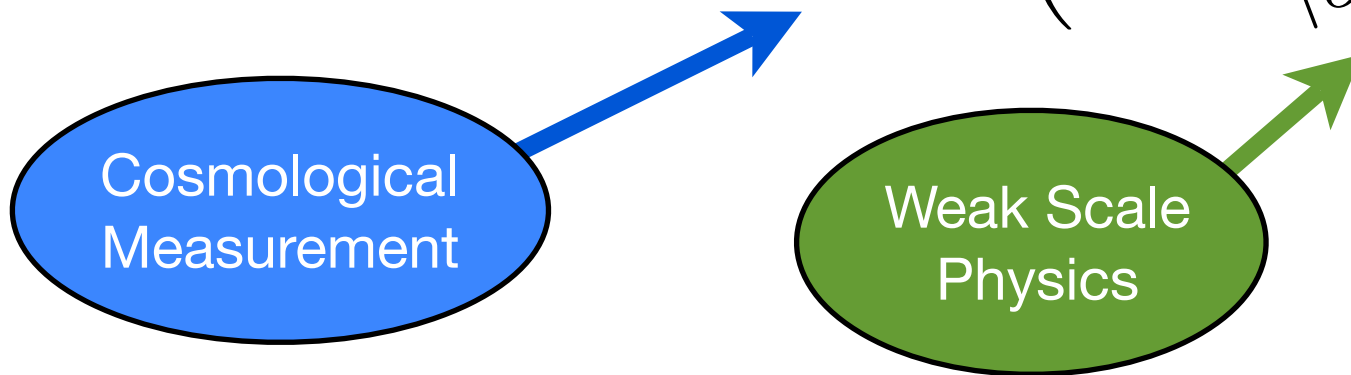


# Revisiting the WIMP Miracle

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## Dark Matter Abundance from Thermal Production

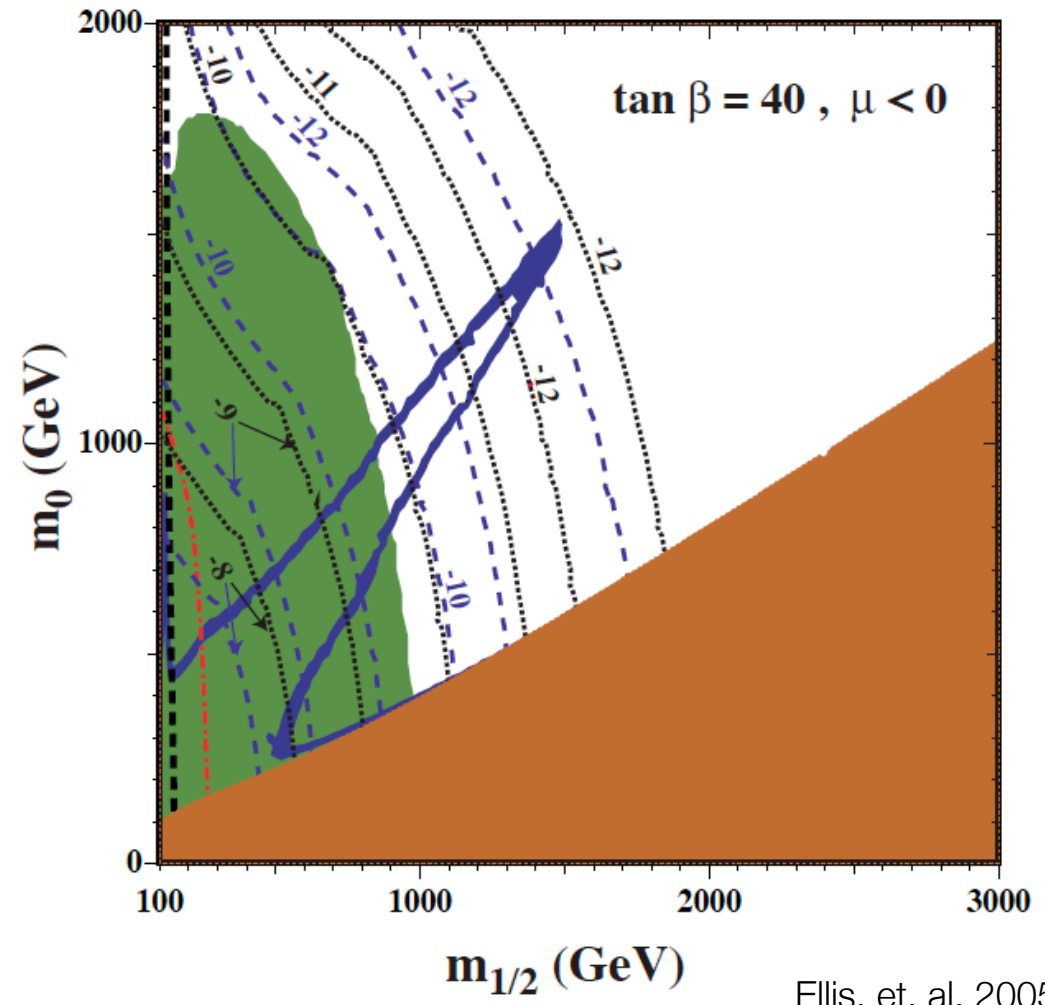
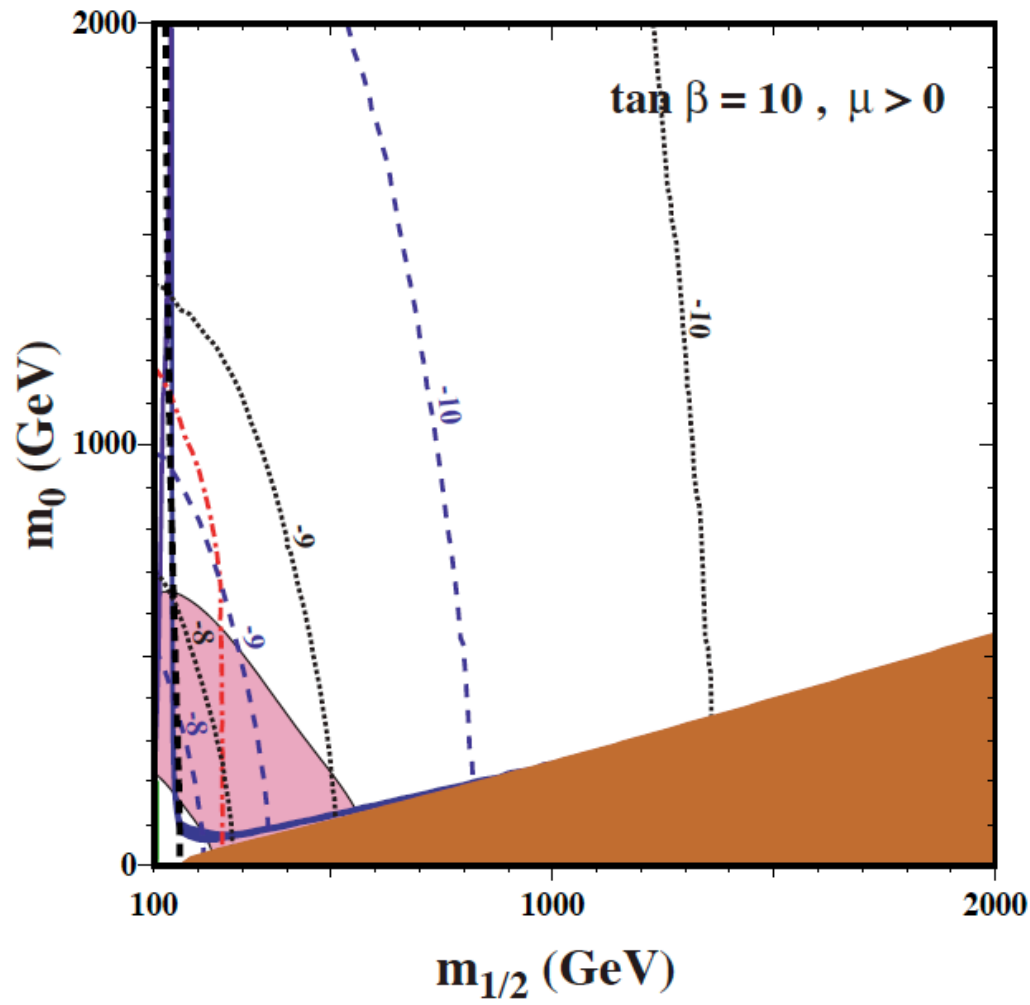
$$\Omega_{dm} = 0.23 \times \left( \frac{10^{-26} \text{ cm}^3 \cdot \text{s}^{-1}}{\langle \sigma v \rangle} \right)$$



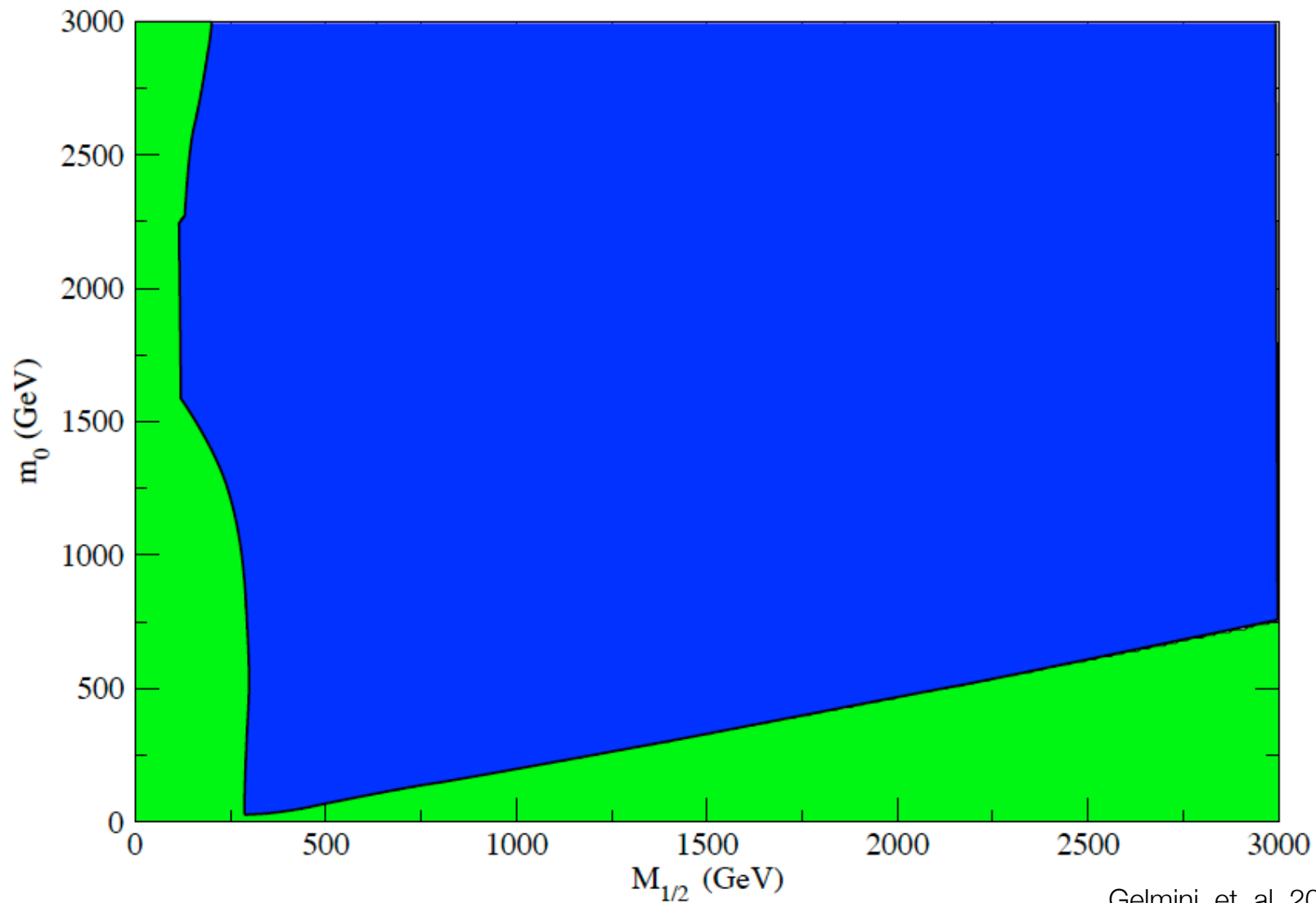
A larger cross-section would account for PAMELA and a surprise at LHC



# SUSY Model Constraints Enforcing WMAP (blue)



# SUSY Model Constraints Without Enforcing WMAP (blue)



If dark matter is not produced thermally,  
how is it produced?

# Example: Non-thermal Dark Matter from Light Scalars

Moroi and Randall -- hep-ph/9906527

## Dark Matter from Scalar Decay:

- Moduli generically displaced in early universe
- Energy stored in scalar condensate

$$\Delta\Phi \rightarrow \Delta E$$

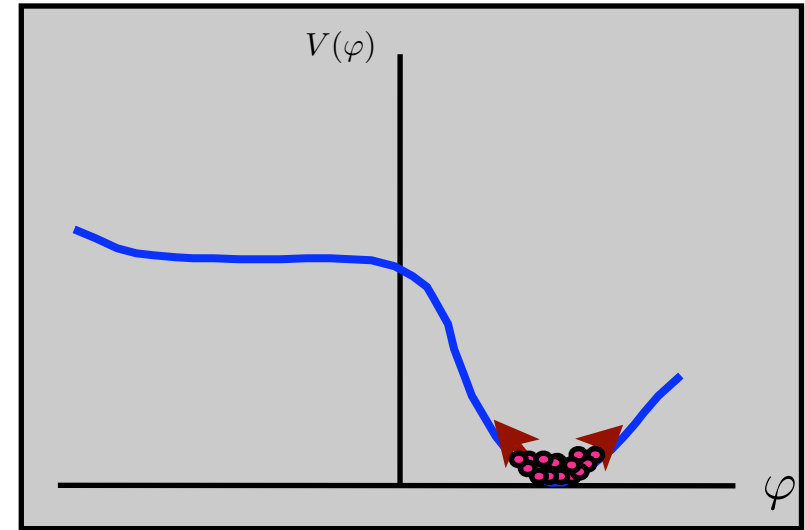
- Typically decays through gravitational coupling

$$T_r \simeq \left( \frac{m_\phi}{10 \text{ TeV}} \right)^{3/2} \text{ MeV}$$

- Large entropy production dilutes existing dark matter of thermal origin

$$\Omega_{cdm} \rightarrow \Omega_{cdm} \left( \frac{T_r}{T_f} \right)^3$$

Thermal abundance diluted



## Non-thermal Dark Matter

Given  $T_r < T_f$  then dark matter populated non-thermally

$$\Omega_{cdm} \sim \frac{m_x}{T} \left( \frac{H}{T^2 \langle \sigma v \rangle} \right)_{T=T_f}$$

$$\Omega_{cdm}^{NT} = \Omega_{cdm} \left( \frac{T_f}{T_r} \right)$$

← Freeze-out temp  
← Reheat temp

$$T_f \sim \text{GeV} \quad T_r \sim \text{MeV}$$

Can vary over 3 orders of magnitude -- Allowed values still imply weak-scale physics “WIMP Miracle” survives

What do we expect from top-down model building?

# What were the key ingredients?

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1

“Light” Scalar

$$m_\phi \approx 10 \text{ TeV}$$

2

Gravitationally coupled

$$\Gamma_\phi \sim \frac{m_\phi^3}{M_p^2}$$

3

Stable dark matter particle

$$m_x \approx 100 \text{ GeV}$$



What were the key ingredients?

---

1

“Light” Scalar

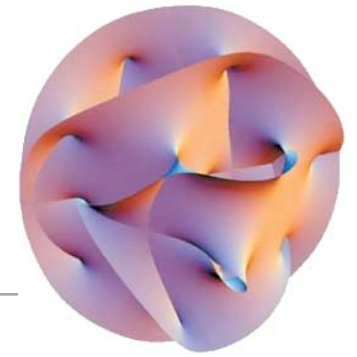
$$m_\phi \approx 10 \text{ TeV}$$

Light enough for decay after freeze-out,  
Heavy enough to evade BBN bounds

3

Stable dark matter particle

$$m_x \approx 100 \text{ GeV}$$



# Guidance from Fundamental Theory

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What is needed from a top-down approach:

- 4D Effective theory (under parametric control)
- Spontaneously broken SUSY (or alternative)
- Explanation for how  $M_{EWSB} \ll M_p$
- Small and Positive Vacuum Energy

In String theory, all [these problems are related](#) and are essentially a problem of [stabilizing scalars](#).

String Models that adequately meet these goals

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String Models that adequately meet these goals

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(joke)

# The Cosmological Moduli Problem

Coughlan, Fischler, Kolb, Raby, and Ross -- Phys. Lett. B131, 1983  
Banks, Kaplan, and Nelson -- Phys. Rev. D49, 1994

---

“ **Model Independent** properties and cosmological implications of the dilaton and moduli sectors of 4-d strings ”

Carlos, Casas, and Quevedo -- Phys. Lett. B318, 1993

$$V = e^{\frac{K}{m_p^2}} |DW|^2 - 3m_{3/2}^2 m_p^2$$

Shift symmetry

$$\Phi = \phi + ia \quad \longrightarrow \quad W \neq W(\Phi)$$

Zero vacuum energy, stabilize scalar, break SUSY (spontaneously)

$$\Delta V(\Phi) = m_{3/2}^2 m_p^2 f\left(\frac{\Phi}{m_p}\right)$$

$$m_\phi \sim m_{3/2} \sim \text{TeV}$$

## Ex: Type IIB -- KKLT

$$W = W_0 + m_p^3 e^{-X} \quad K = -n m_p^2 \log (X + \bar{X})$$

$$V = e^{\frac{K}{m_p^2}} (|DW|^2 - 3m_{3/2}^2 m_p^2)$$

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### SUSY Minimum

$$D_X W = 0 \rightarrow \langle X \rangle = \log \left( \frac{m_p}{n m_{3/2}} \right)$$

$$V_{AdS} = -3m_{3/2}^2 m_p^2$$

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## Uplift and Break SUSY

$$\Delta V \sim m_{3/2}^2 m_p^2 \quad \delta X \rightarrow \delta X_c = \frac{\sqrt{n}}{\langle \text{Re} X \rangle} \delta X$$



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## Uplift and Break SUSY

$$\Delta V \sim m_{3/2}^2 m_p^2 \quad \delta X \rightarrow \delta X_c = \frac{\sqrt{n}}{\langle \text{Re} X \rangle} \delta X$$

$$m_X = n^{-\frac{1}{2}} \log \left( \frac{m_p}{n m_{3/2}} \right) m_{3/2} \sim 4\pi^2 m_{3/2}$$

(Loaiza-Brito, Martin, Nilles , and Ratz)

# Other models with possible non-thermal contribution:

- Large Volume Compactifications  
e.g. Conlon and Quevedo -- [arXiv:0705.3460](#)
- F-theory (Jonathan's talk)  
Heckman, Tavanfar, and Vafa-- [arXiv:0812.3155](#)
- M-theory on G2 manifolds (Gordy's talk)  
Acharya, et. al. -- [arXiv:0804.0863](#)

$$W = \cancel{W_0} + c_1 f(\phi) e^{-aX} + c_2 e^{-bX}$$

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## Remarks

- Many open questions:  
Embedding visible sector, uplifting, path to 4d, SUSY breaking
- Scalar may be too light (then perhaps thermal inflation)
- Gaugino (dark matter ) has three robust patterns  
[“The Gaugino Code”, Choi and Nilles -- arXiv:hep-ph/0702146](#)
- Light scalar may be robust prediction  
(a.k.a. cosmological moduli “problem”)

# Moduli Stabilization Basics

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If scalars stabilized without reintroducing [electroweak hierarchy](#) and accounting for [small and positive vacuum energy](#) this typically implies:

$$m_\phi \approx m_{3/2} \approx \text{TeV} \quad \text{A new "WIMP" miracle}$$

Scalars are gravitationally coupled giving

$$T_r \simeq \left( \frac{m_\phi}{10 \text{ TeV}} \right)^{3/2} \text{ MeV}$$

**Non-thermal dark matter!!!!**

Given hints from LHC (April 1, 2010)  
and motivation from [fundamental theory](#):

Can the [well-motivated](#) neutralino account for PAMELA?

# Non-thermal SUSY Dark Matter

P. Grajek, G. Kane, D. Phalen, A. Pierce, S.W. arXiv:0812.4555 and arXiv:0807.1508

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Neutralino WIMPs ( light, stable (R-parity), neutral )

$$\tilde{\chi} = N_{i1} \tilde{B} + N_{i2} \tilde{W}^3 + N_{i3} \tilde{H}_1^0 + N_{i4} \tilde{H}_2^0$$

Bino-like cross-section ( P-wave suppression )

$$\langle \sigma v \rangle \sim 10^{-26} \text{cm}^3 \text{s}^{-1} \quad \Omega_{lsp} \approx 0.23$$

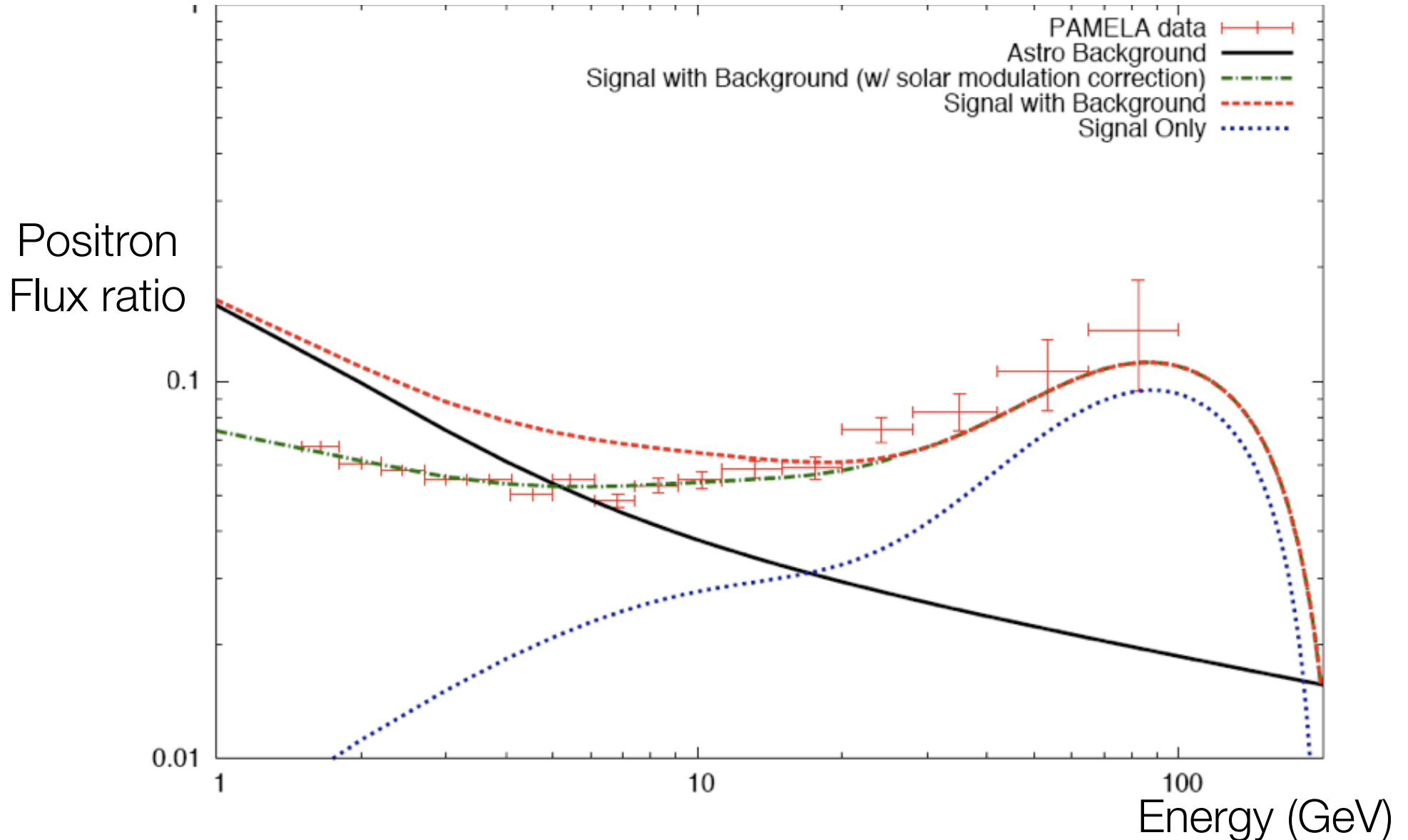
Wino-like cross-section ( S-wave suppression )

$$\langle \sigma v \rangle \sim 10^{-24} \text{cm}^3 \text{s}^{-1} \quad \Omega_{lsp} \approx 0.002$$

# The PAMELA Excess from SUSY Dark Matter

P. Grajek, G. Kane, D. Phalen, A. Pierce, S.W. arXiv:0812.4555 and arXiv:0807.1508

## Positron Flux for 200 GeV SUSY Dark Matter



# PAMELA from Non-thermal SUSY Dark Matter

P. Grajek, G. Kane, D. Phalen, A. Pierce, S.W. arXiv:0812.4555 and arXiv:0807.1508

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Light enough to explain PAMELA

$$m_{\mathbf{X}} \lesssim 300 \text{ GeV}$$

Heavy enough to avoid other indirect detection

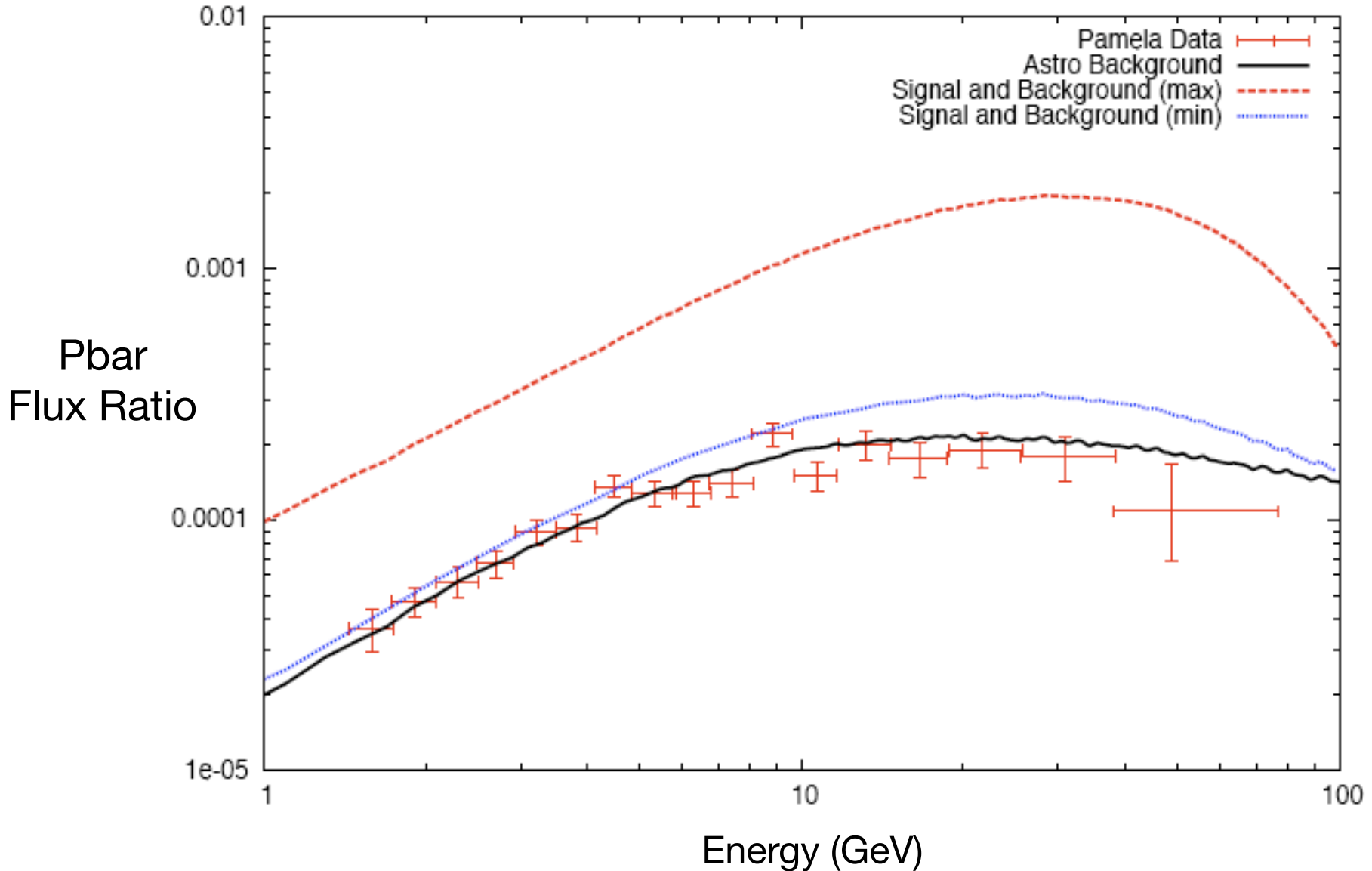
$$m_{\mathbf{X}} \gtrsim 200 \text{ GeV}$$



# Anti-Proton Bounds and Uncertainties

P. Grajek, G. Kane, D. Phalen, A. Pierce, S.W. arXiv:0812.4555 and arXiv:0807.1508

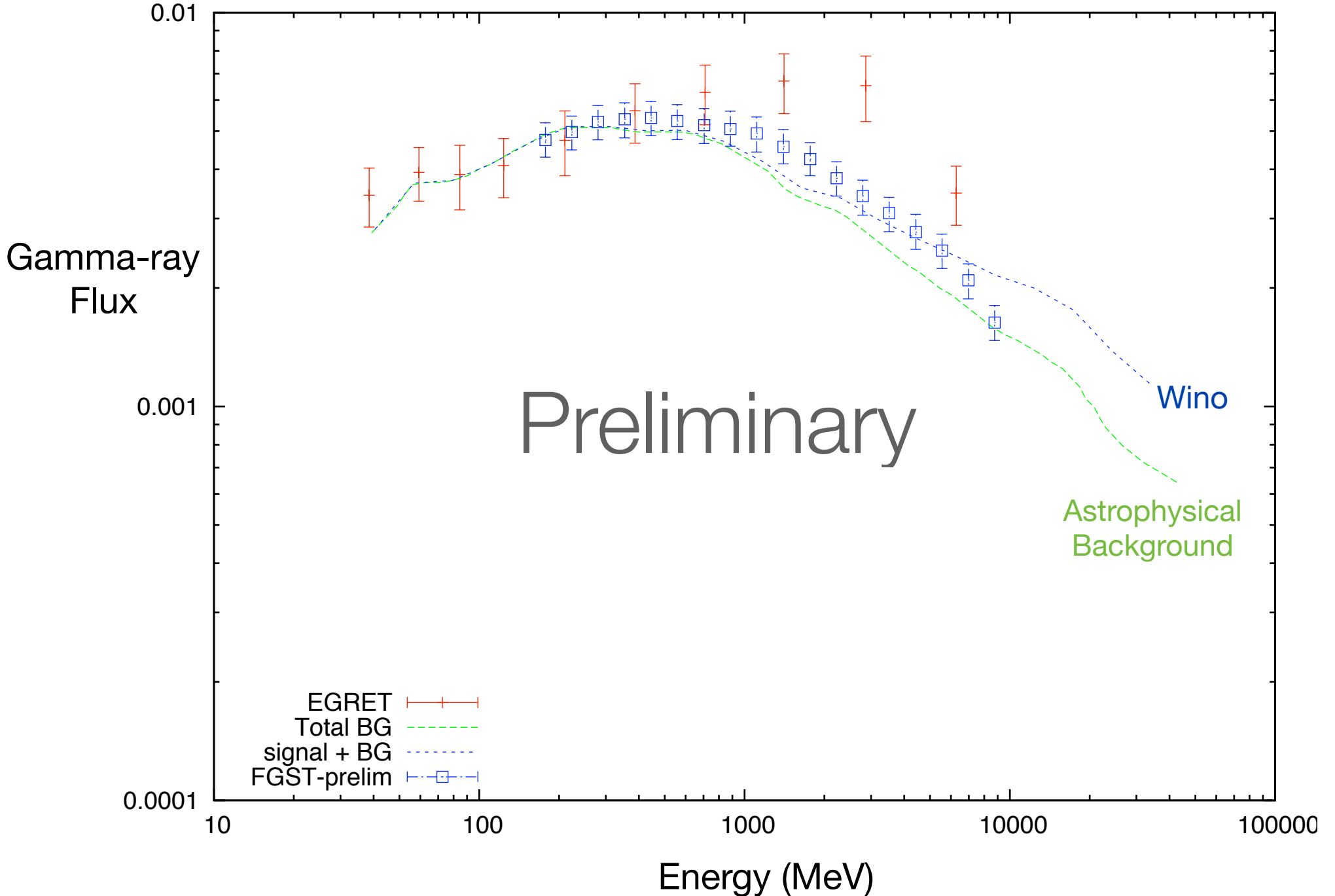
Anti-Proton Flux for 200 GeV Wino-like Neutralino



What about Gamma-rays and FERMI?

# Gamma-ray fluxes and FERMI

Data taken from talk at Michigan workshop (MCTP) on LHC/CDM



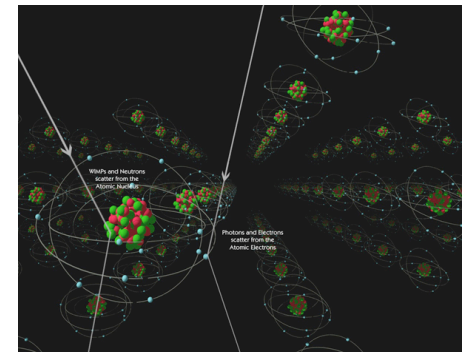
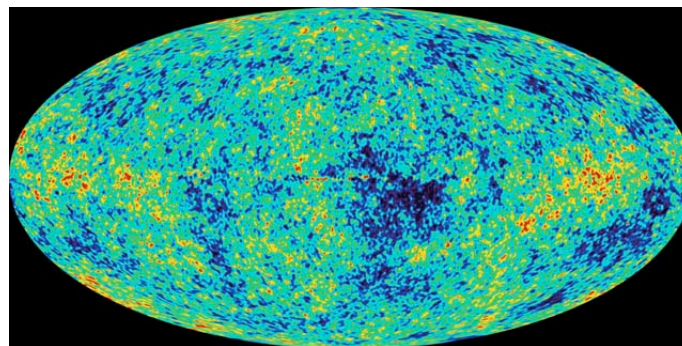
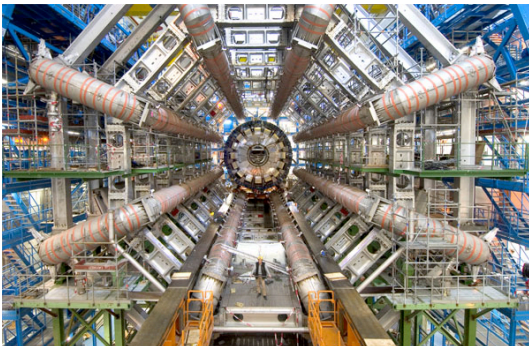
# Conclusion

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Thermal dark matter from “realistic” models of string phenomenology could prove challenging.

This is good news, because non-thermal dark matter (in contrast to thermal production) could provide a new window on probing string based models.

A complete understanding of dark matter requires a concordance approach (cosmology, particle experiment, and fundamental theory)



Thank You

Backups

# Wino-like Neutralinos - Positron Excess

P. Grajek, G. Kane, D. Phalen, A. Pierce, S.W. arXiv:0812.4555 ( PRD )

P. Grajek, G. Kane, D. Phalen, A. Pierce, S.W. arXiv:0807.1508 ( PRD )

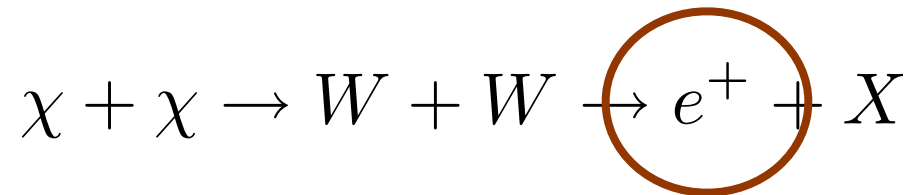
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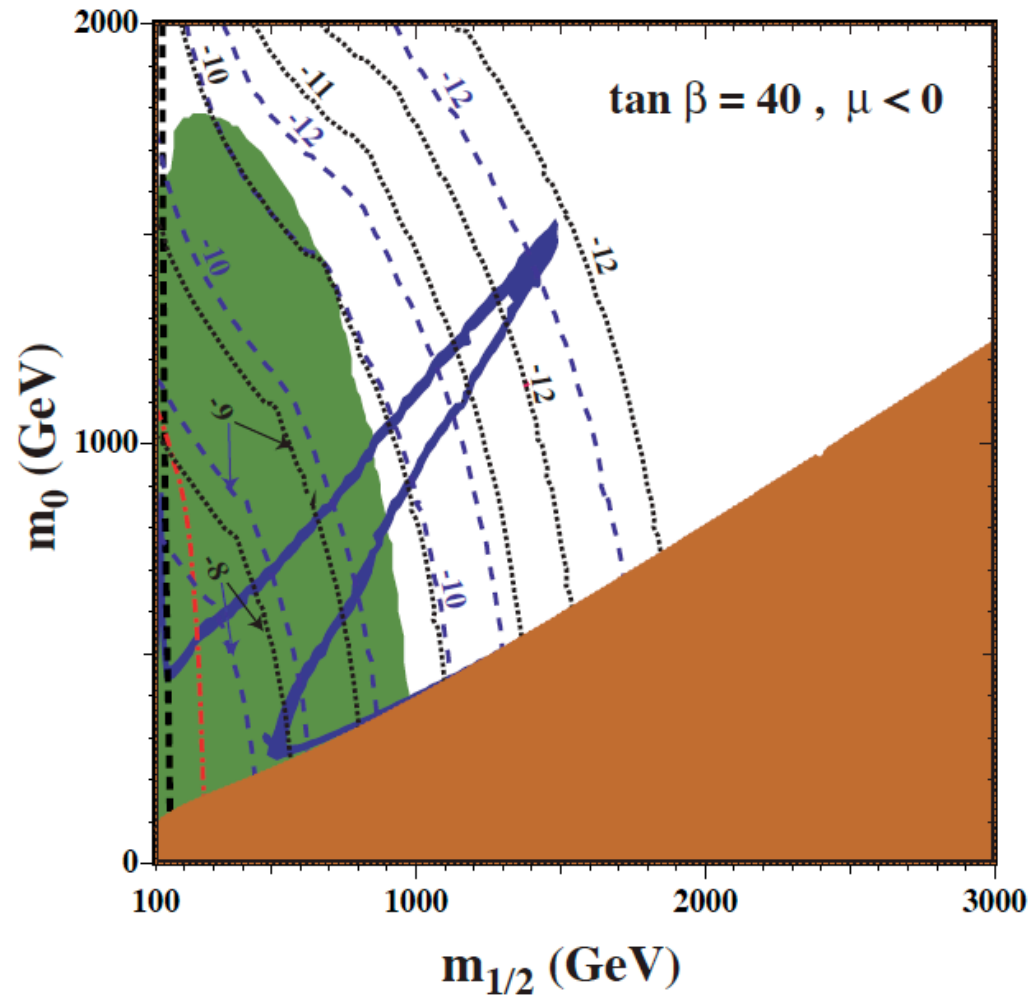
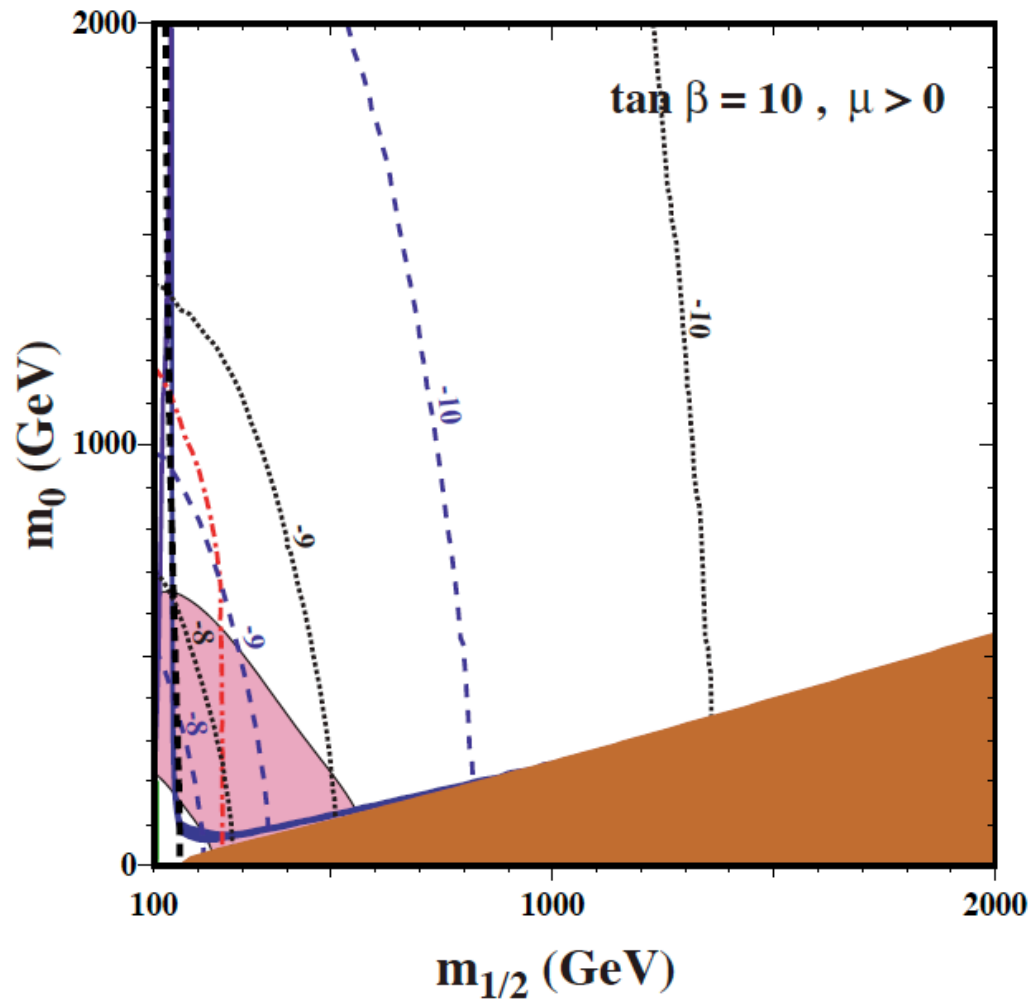
Could excess be due to annihilating SUSY dark matter?

Bino-like requires large “boost” factor

$$Flux \sim \langle \sigma v \rangle \times \left( \frac{\rho_{\chi}^{halo}}{m_{\chi}} \right)^2$$

Wino leading decay channel:

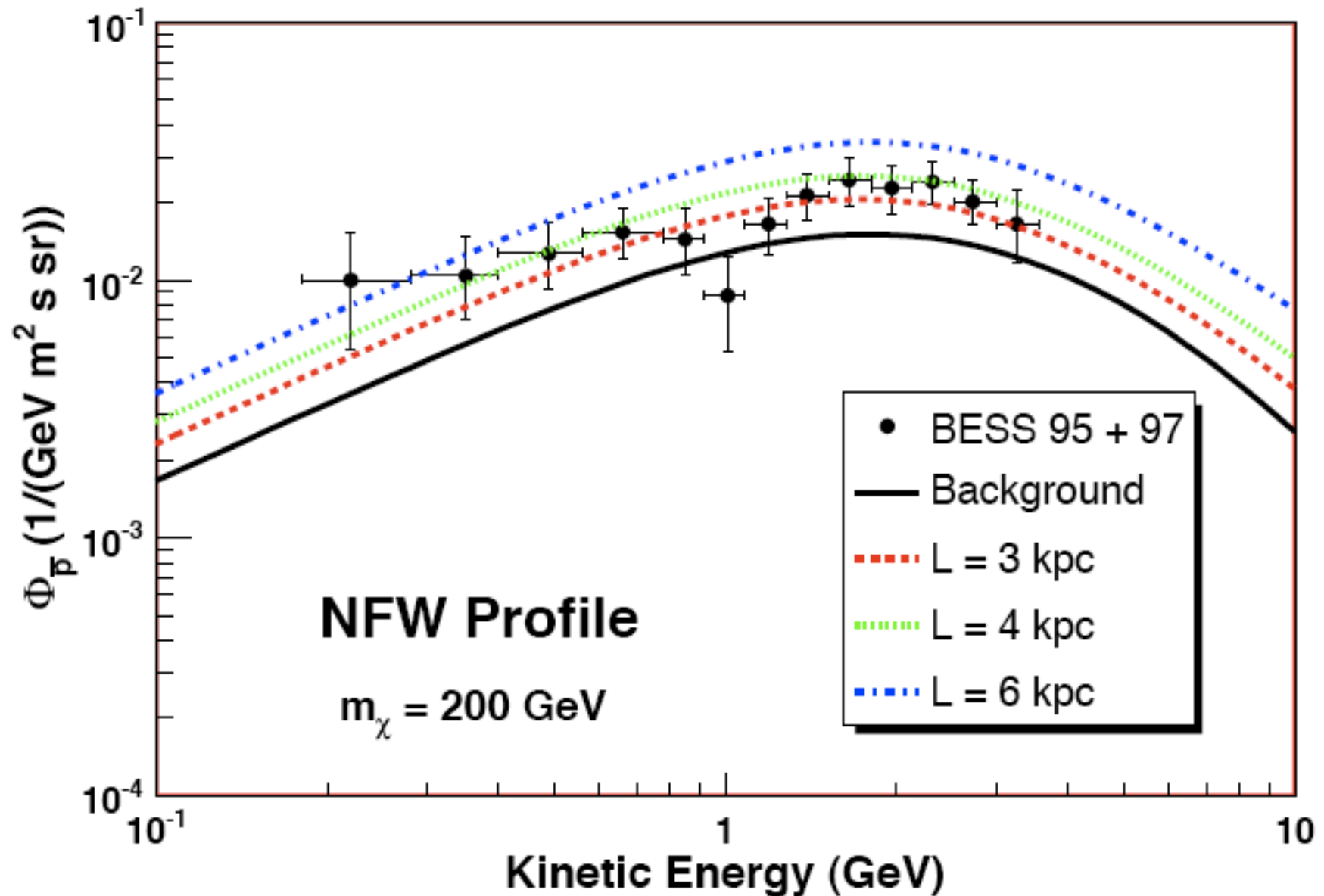




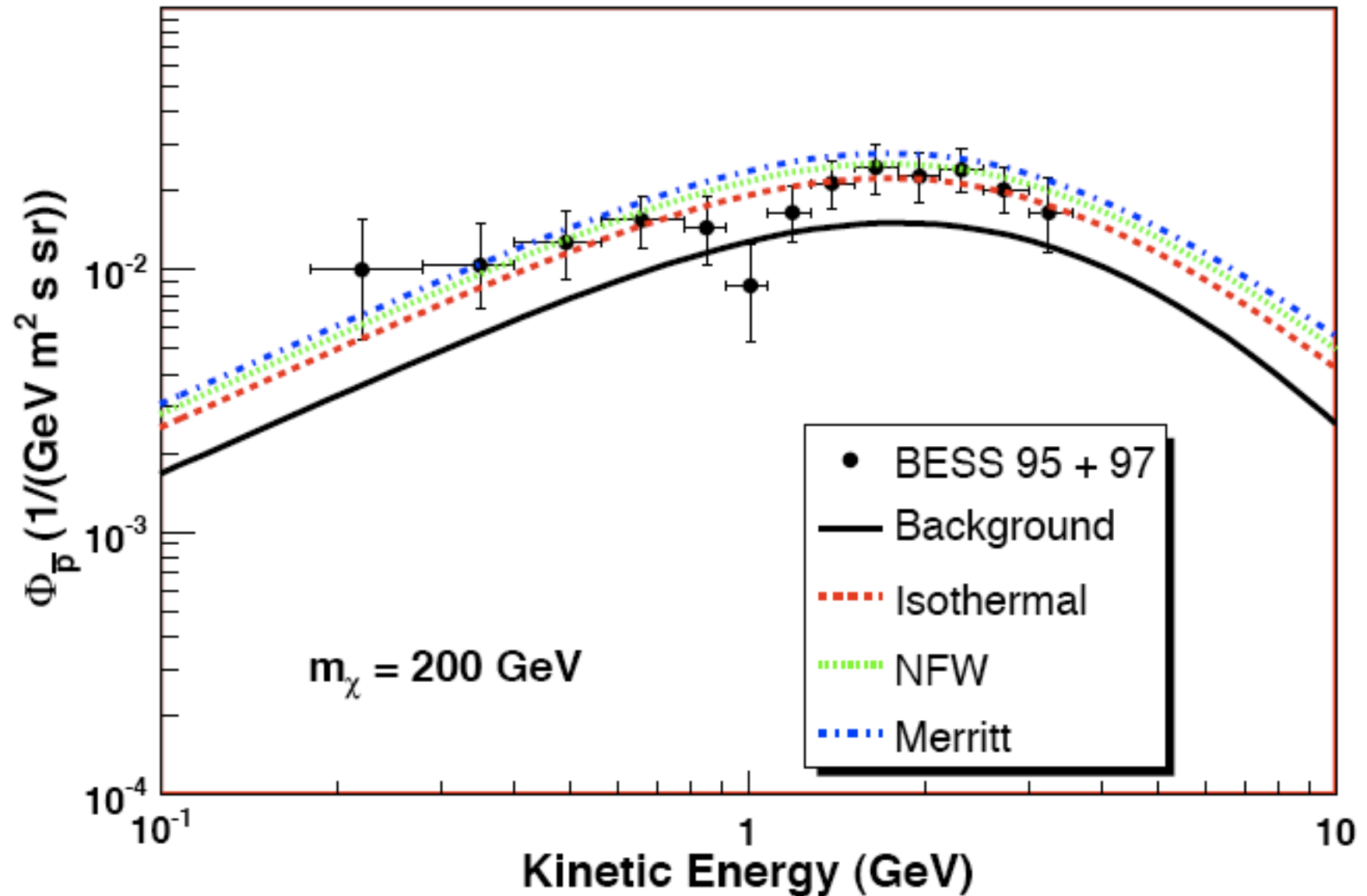
The  $(m_{1/2}, m_0)$  planes in the CMSSM for (a)  $\tan \beta = 10, \mu < 0$ , (b)  $\tan \beta = 10, \mu > 0$ , (c)  $\tan \beta = 40, \mu < 0$  and (d)  $\tan \beta = 57, \mu > 0$ , all assuming  $A_0 = 0$ . We display the WMAP relic-density constraint, the experimental constraints due to  $m_h, m_{\chi^\pm}, b \rightarrow s$  and  $g\mu - 2$ , and contours of the spin-independent elastic-scattering cross section calculated for  $\sigma = 45$  and  $64$  MeV (lighter, blue and black dotted contours, respectively), labelled by their exponents in units of picobarns.



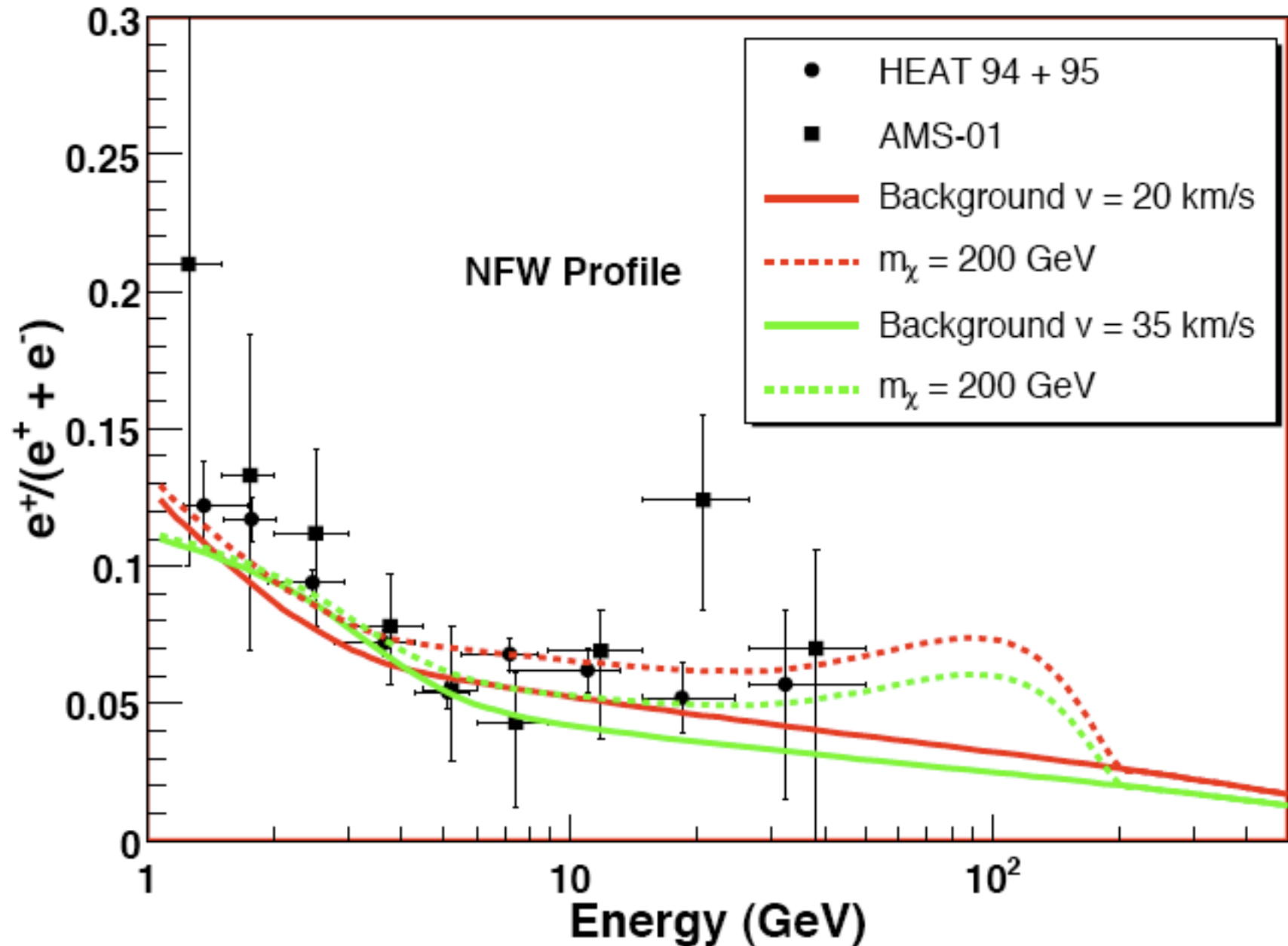
# Anti-proton flux for changing cylinder height

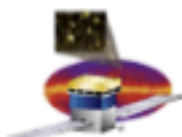


# Anti-proton flux for changing halo profile



# Anti-proton flux for changing Alfvén Velocity





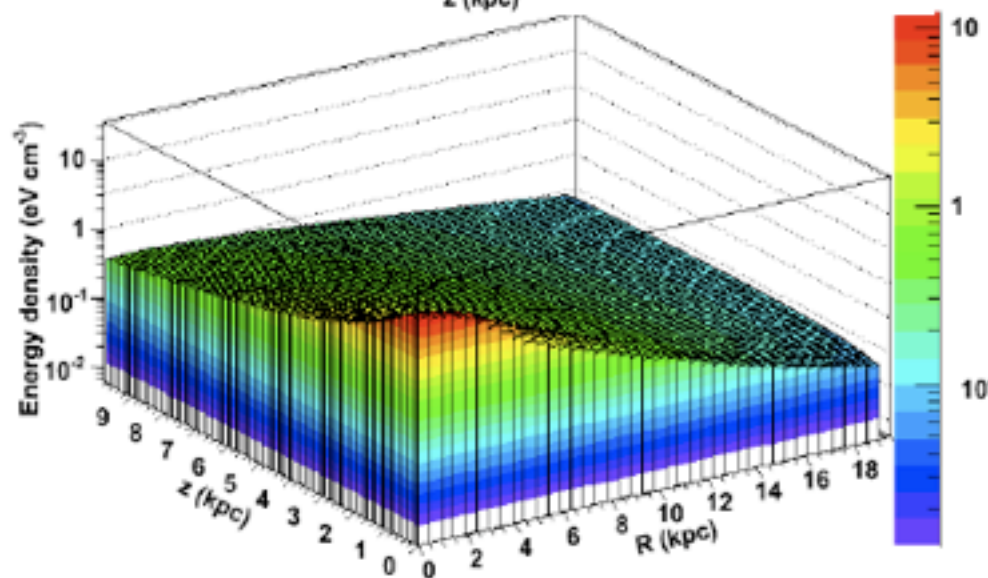
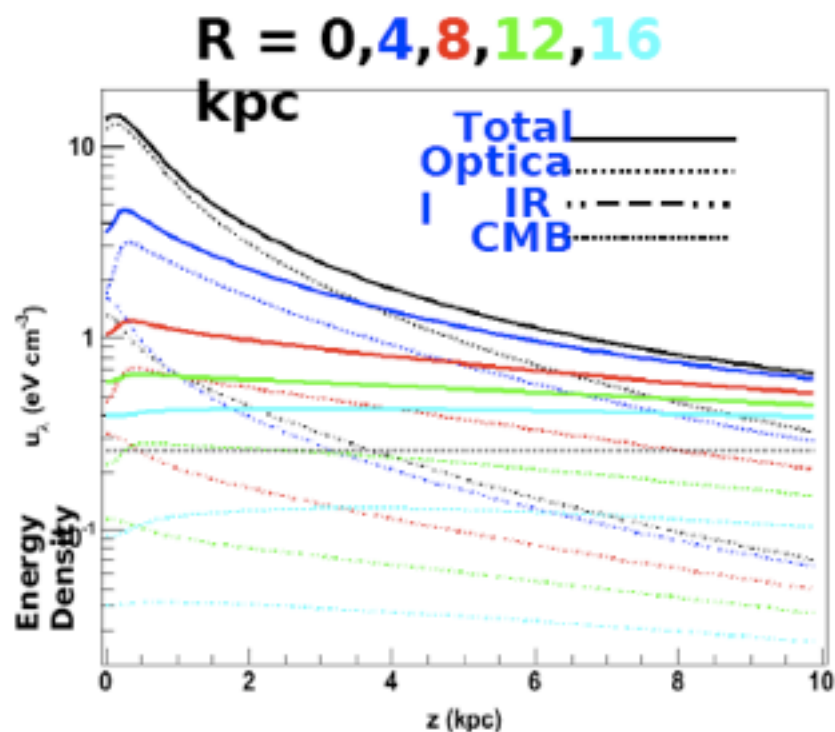
# Large Scale Distribution

ISRF extends for significant distance above GP

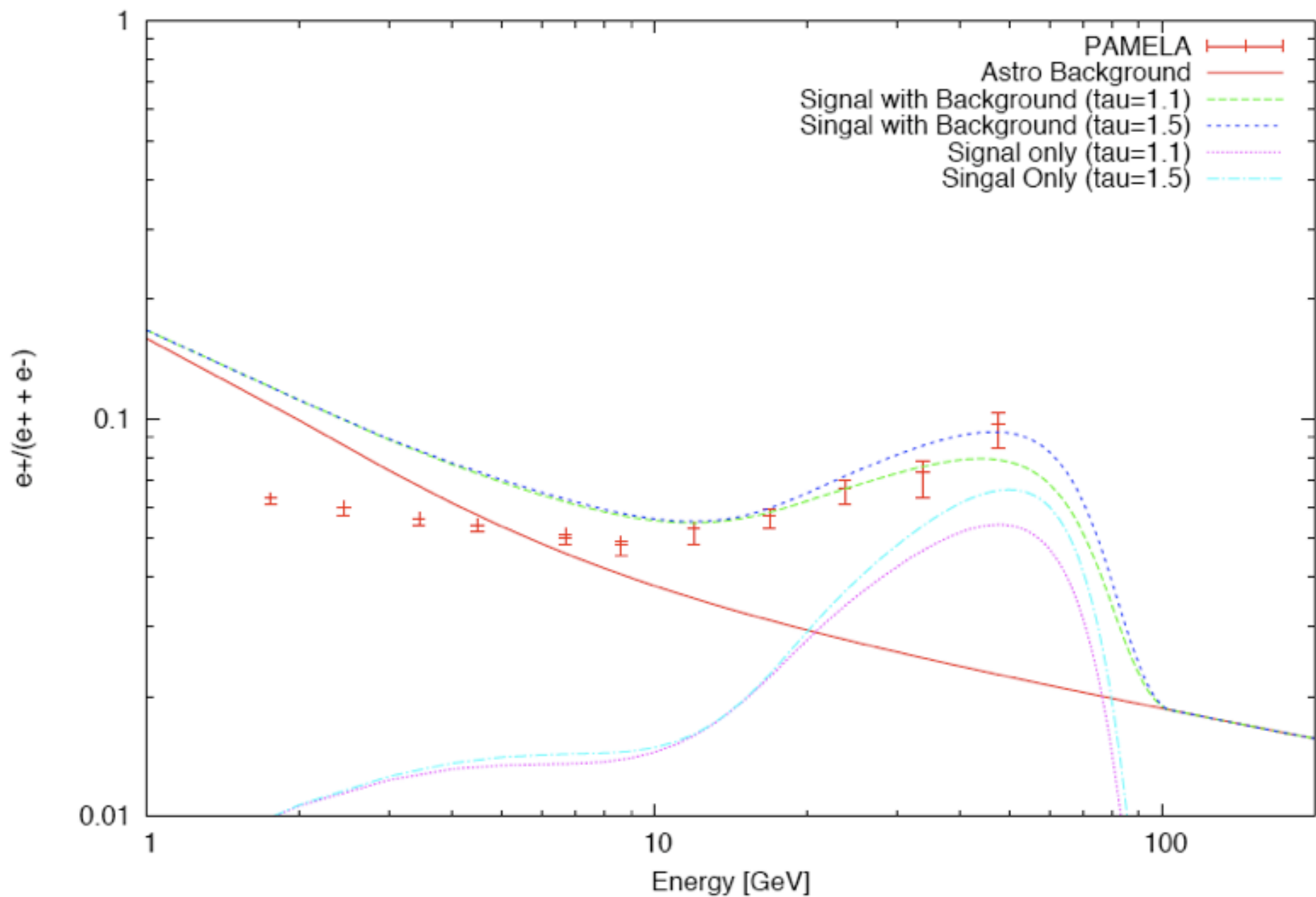


Significant ICS at high lats.

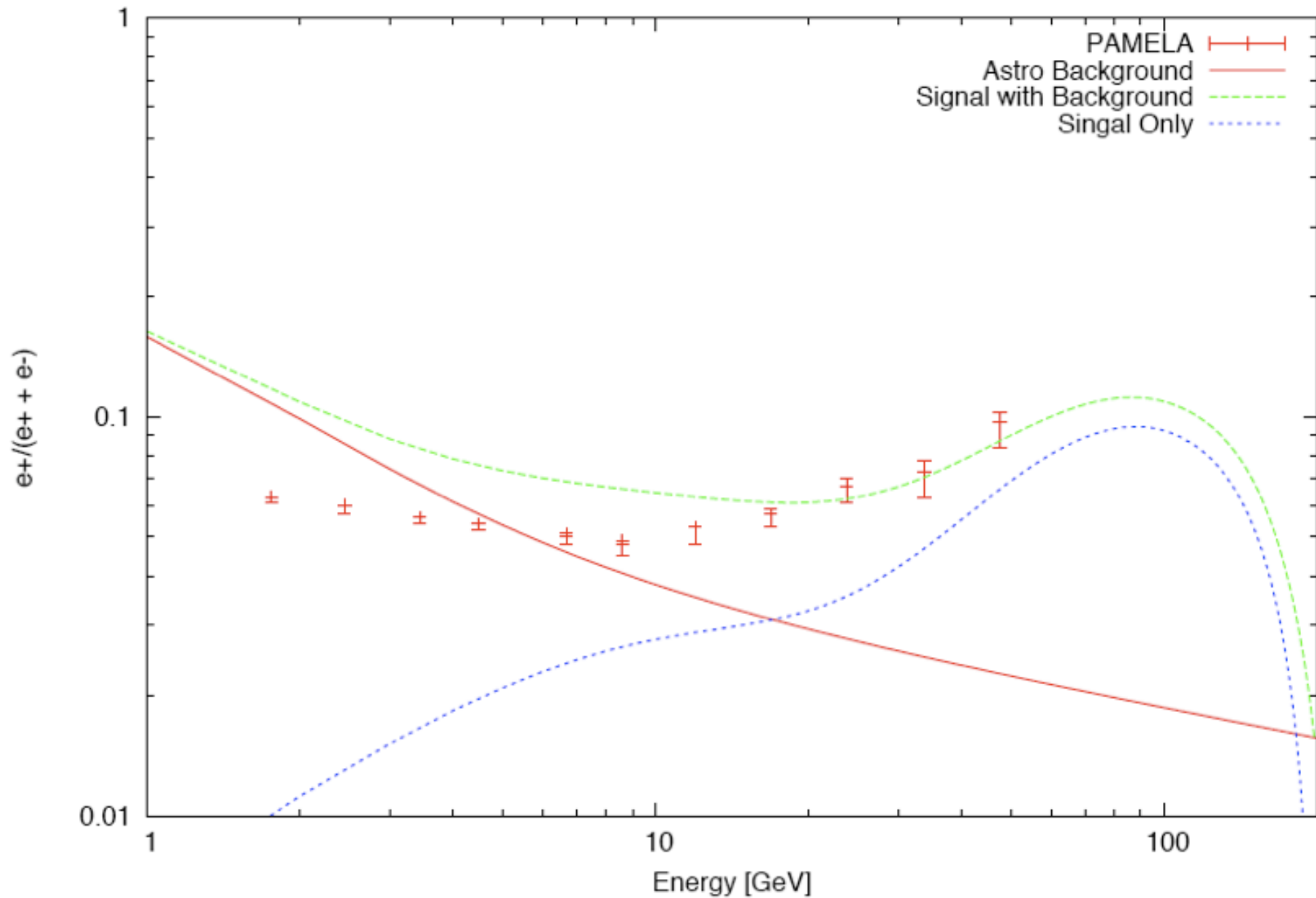
Not so much in plane because of dust and star density decreases with R

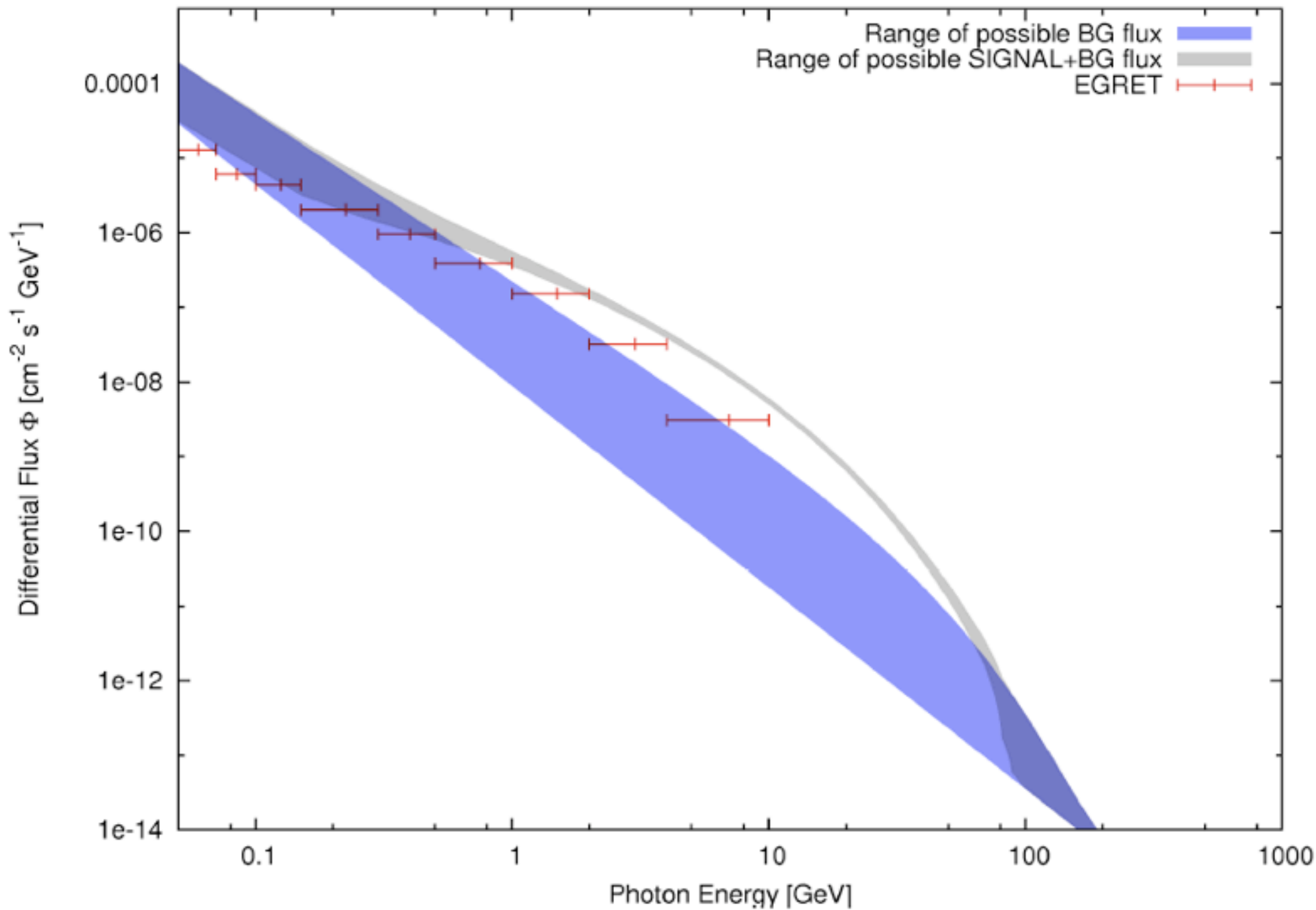


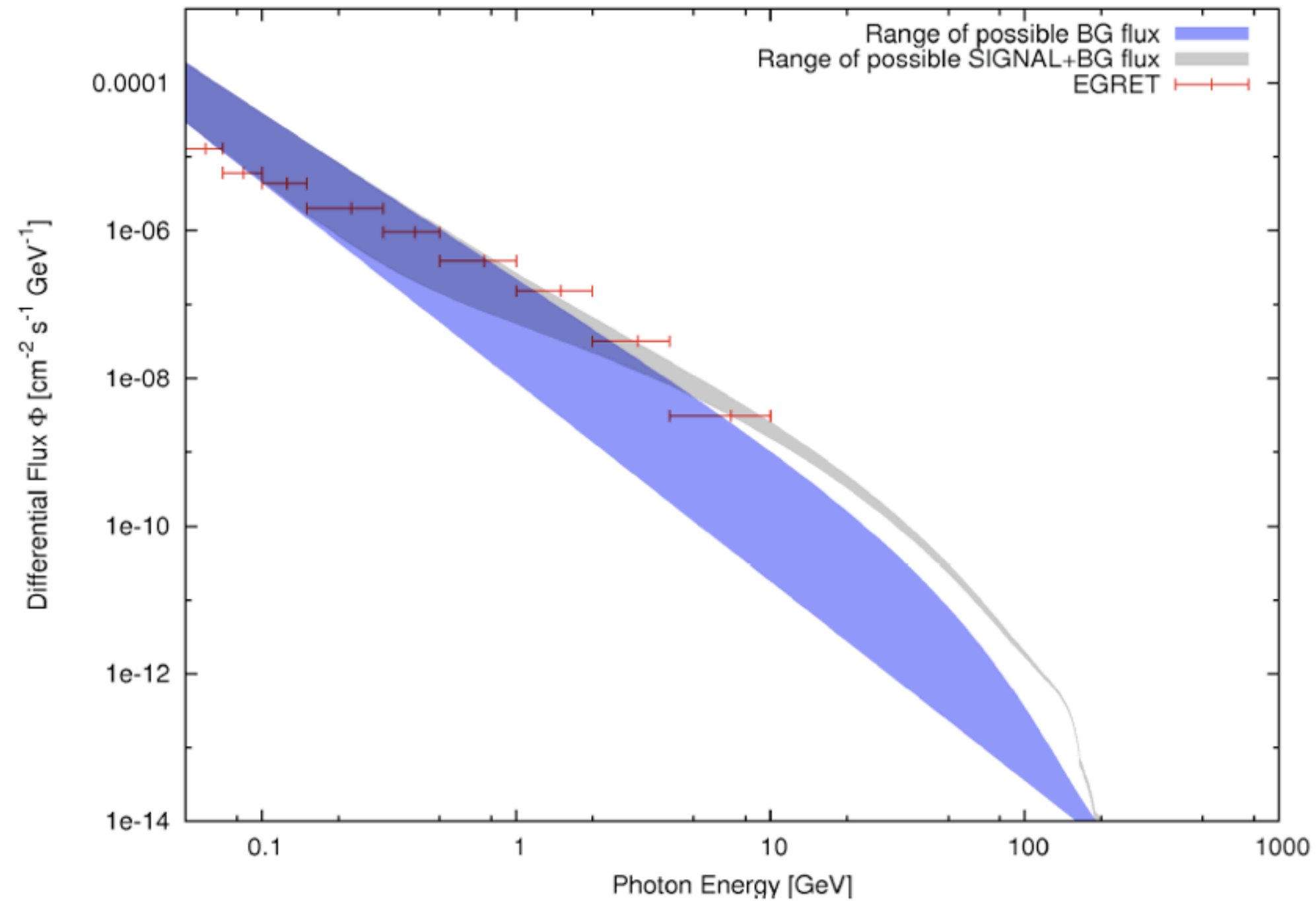
Positron Flux for Changing Energy Loss



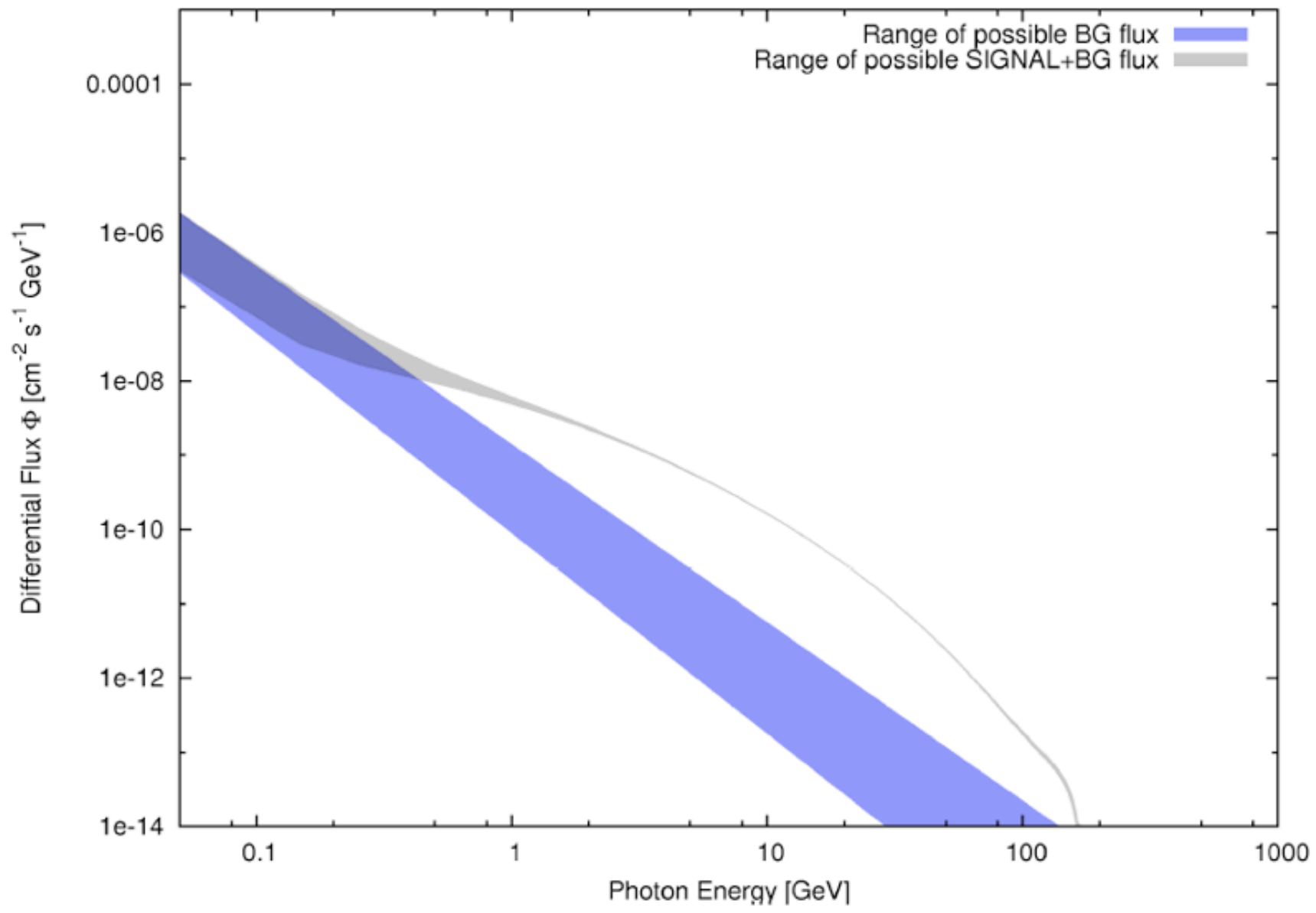
Positron Flux for 198 GeV Wino-like Neutralino











# Dark Matter Self Annihilations

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Source term for dark matter annihilations

$$Q = \frac{1}{2} \left[ \frac{\langle \sigma v \rangle}{m_{\chi}^2} \sum_i \frac{dN_i}{dE} B_i(\chi\chi \rightarrow i) \right] \times \rho(\vec{r})^2$$

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