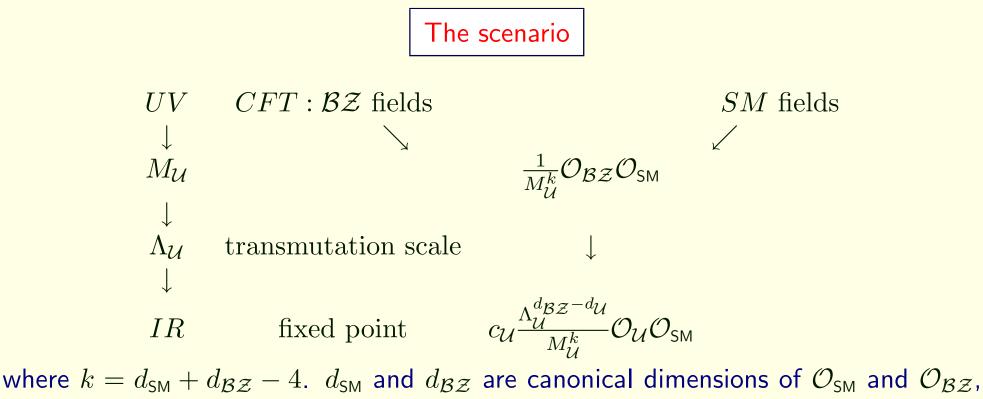
UnCosmology

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- The scenario H. Georgi, "Unparticle Physics", Phys. Rev. Lett. 98, 221601 (2007)
- Examples of the \mathcal{BZ} sector
- Couplings of unparticles to the SM
- Deconstruction of unparticles
- Spontaneous symmetry breaking with unparticles and Higgs boson physics
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 - The equation of state for unparticles
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respectively, while $d_{\mathcal{U}}$ is the scaling dimension (the same as the mass dimension in this case) of $\mathcal{O}_{\mathcal{U}}$:

 $\mathcal{O}_{\mathcal{U}}(x) \to \mathcal{O}'_{\mathcal{U}}(x') = s^{-d_{\mathcal{U}}} \mathcal{O}_{\mathcal{U}}(x) \quad \text{with} \quad 1 < d_{\mathcal{U}} < 2 \quad \text{for} \quad x \to x' = sx$

An example of matching between $\mathcal{O}_{\mathcal{BZ}}$ and $\mathcal{O}_{\mathcal{U}}$:

• $(\bar{q}q)$ in QCD $\iff M \propto (\bar{q}q)$ mesons in the chiral non-linear model

• Banks & Zaks (1982): SU(3) YM with n massless fermions in e.g. fundamental representation

$$\beta(g) = -\left(\beta_0 \frac{g^3}{16\pi^2} + \beta_1 \frac{g^5}{(16\pi^2)^2} + 3 \text{ loops} \cdots\right)$$

$$\beta_0 = 11 - \frac{2}{3}n \qquad \beta_0(n_0) = 0 \qquad n_0 = 16.5$$

$$\beta_1 = 102 - \frac{38}{3}n \qquad \beta_1(n_1) = 0 \qquad n_1 \simeq 8.05$$

If $n_1 < n < n_0$ (so $\beta_0 > 0$ & $\beta_1 < 0$) then keeping β_0 and β_1 one gets

$$\beta(g_{IR}) = 0$$
 for $\frac{g_{IR}^2}{16\pi^2} = -\frac{33-2n}{306-38n}$

Conclusions:

- If $g = g_{IR}$, then the low-energy theory is scale invariant with small anomalous scaling
- For $n \lesssim n_0$, the theory remains perturbative, so the continuous spectrum doesn't emerge.

Couplings of unparticles to the SM

Assumptions:

- $\mathcal{O}_{\mathcal{U}}$ in neutral under the SM gauge group
- $\dim(\mathcal{O}_{SM}) \leq 4$

$$\mathcal{L}_{\rm int} = c_{\mathcal{U}} \frac{\Lambda_{\mathcal{U}}^{d_{\mathcal{B}\mathcal{Z}} - d_{\mathcal{U}}}}{M_{\mathcal{U}}^{k}} \mathcal{O}_{\mathcal{U}} \mathcal{O}_{\mathsf{SM}} \propto \left(\frac{\Lambda_{\mathcal{U}}}{M_{\mathcal{U}}}\right)^{k} \Lambda_{\mathcal{U}}^{4 - d_{\mathsf{SM}} - d_{\mathcal{U}}} \mathcal{O}_{\mathcal{U}} \mathcal{O}_{\mathsf{SM}} \quad \text{for} \quad k = d_{\mathsf{SM}} + d_{\mathcal{B}\mathcal{Z}} - 4$$

- Scalar unparticles $\mathcal{O}_{\mathcal{U}}$: $\propto \Lambda_{\mathcal{U}}^{2-d_{\mathcal{U}}} H^{\dagger} H \mathcal{O}_{\mathcal{U}}$ for $d_{SM} = 2$
- Spinor unparticles $O^s_{\mathcal{U}} : \propto \Lambda^{5/2-d_{\mathcal{U}}}_{\mathcal{U}} \bar{\nu}_R O^s_{\mathcal{U}}$ for $d_{SM} = 3/2$

Deconstruction of unparticles

Källen-Lehman representation of the Feynman propagator:

$$i\Delta_F^{\mathcal{U}}(p^2) = \int d^4x e^{ipx} \langle 0|T\{\mathcal{O}_{\mathcal{U}}(x)\mathcal{O}_{\mathcal{U}}(0)\}|0\rangle = \int_0^\infty \frac{dm^2}{2\pi} \rho(m^2) \frac{i}{p^2 - m^2 + i\varepsilon}$$

with $\rho_{\mathcal{U}}(m^2) = A_{d_{\mathcal{U}}}\theta(m^2)(m^2)^{d_{\mathcal{U}}-2}$. Deconstruction (Stephanov'07):

$$\mathcal{O}_{\mathcal{U}} \to \sum_{n=0}^{\infty} F_n \varphi_n \quad \text{with} \quad m_n^2 = \Delta^2 n$$

Then

$$i\Delta_F^{\mathcal{U}}(p^2) = \int d^4x e^{ipx} \langle 0|T\{\mathcal{O}_{\mathcal{U}}(x)\mathcal{O}_{\mathcal{U}}(0)\}|0\rangle = \sum_{n=0}^{\infty} \frac{iF_n^2}{p^2 - m_n^2 + i\varepsilon}$$

if $F_n^2 = \frac{A_{d\mathcal{U}}}{2\pi} \Delta^2 (m_n^2)^{d\mathcal{U}-2}$ then

$$i\frac{A_{d_{\mathcal{U}}}}{2\pi}\sum_{n=0}^{\infty}\frac{(m_{n}^{2})^{d_{\mathcal{U}}-2}}{p^{2}-m_{n}^{2}+i\varepsilon}\Delta^{2} \xrightarrow{\to} 0 i\frac{A_{d_{\mathcal{U}}}}{2\pi}\int\frac{(m^{2})^{d_{\mathcal{U}}-2}dm^{2}}{p^{2}-m^{2}+i\varepsilon} = \int\frac{dm^{2}}{2\pi}\rho(m^{2})\frac{i}{p^{2}-m^{2}+i\varepsilon}$$

So, the undeconstructed result has been confirmed. Now, let's focus on the non-trivial phase:

$$\mathbf{Im}\left\{\sum_{n=0}^{\infty} \frac{F_n^2}{p^2 - m_n^2 + i\varepsilon}\right\} = -\sum_n F_n^2 \pi \delta(p^2 - m_n^2) \underset{\Delta \to 0}{\to} -\frac{A_{d_{\mathcal{U}}}}{2} \theta(p^2)(p^2)^{d_{\mathcal{U}}-2}$$

So, each peak becomes lower as $F_n^2 \sim \Delta^2 \rightarrow 0$, but their density increases.

- Each mode φ_n breaks the scale invariance.
- In the limit

$$\lim_{N \to \infty} \sum_{n=0}^{N}$$

the scale invariance is recovered.

The deconstruction for $t \to u \mathcal{O}_{\mathcal{U}}$ decay

Number of states $|\varphi_n\rangle$ in the interval $(E_u, E_u + dE_u)$: $dN = dE_u \frac{2m_t}{\Delta^2}$

$$\frac{d\Gamma}{dE_u} = \frac{2m_t}{\Delta^2} \Gamma(t \to u + \varphi_n) = \frac{\lambda^2}{\Lambda_u^{2d_u}} A_{d_u} \frac{m_t^2}{2\pi^2} E_u^2 (m_t^2 - 2m_t E_u)^{(d_u - 2)} \theta(m_t - 2E_u)$$

The same as the Georgi's result!

Γ

Spontaneous symmetry breaking with unparticles and Higgs boson physics

(Delgado, Espinosa, Quiros'07)

Deconstruction $(\mathcal{O}_{\mathcal{U}} \to \sum_n F_n \varphi_n, m_n^2 = \Delta^2 n) \Rightarrow$

$$V_{\text{tot}} = m^2 |H|^2 + \lambda |H|^4 + \delta V$$

for

So,

$$\delta V = \frac{1}{2} \sum_{n=0}^{\infty} m_n^2 \varphi^2 + \kappa_{\mathcal{U}} |H|^2 \sum_{n=0}^{\infty} F_n \varphi_n$$
$$\langle \varphi_n \rangle = -\frac{\kappa_{\mathcal{U}} v^2 F_n}{m_n^2} \quad \text{for} \quad \langle |H|^2 \rangle = v^2, \qquad F_n^2 = \frac{A_{d_{\mathcal{U}}}}{2\pi} \Delta^2 (m_n^2)^{d_{\mathcal{U}}-2}$$

$$\langle \mathcal{O}_{\mathcal{U}} \rangle = \sum_{n=0}^{\infty} F_n \langle \varphi_n \rangle \longrightarrow -\kappa_{\mathcal{U}} v^2 \frac{A_{d_{\mathcal{U}}}}{2\pi} \int_0^\infty \frac{dm^2}{(m^2)^{3-d_{\mathcal{U}}}} = -\infty$$

• The IR divergence!

• A possible regularization $\delta V' = \zeta |H|^2 \sum \varphi_n^2$ is not scale invariant.

Since the scaling invariance is anyway violated by the vacuum expectation value $\neq 0$ through $|H|^2 \mathcal{O}_{\mathcal{U}}$ so we adopt

$$\delta V' = \zeta |H|^2 \sum_n \varphi_n^2$$

as the IR regulator. Then

$$v_n = \langle \varphi_n \rangle = -\frac{\kappa_{\mathcal{U}} v^2}{2(m_n^2 + \zeta v^2)} F_n$$

The minimization for H reads:

$$m^2 + \lambda v^2 + \kappa_{\mathcal{U}} \sum_n F_n v_n + \zeta \sum_n v_n^2 = 0$$

Inserting v_n one gets in the continuum limit $(\Delta \rightarrow 0)$:

$$m^{2} + \lambda v^{2} - \lambda_{\mathcal{U}}(\mu^{2})^{2-d_{\mathcal{U}}} v^{2(d_{\mathcal{U}}-1)} = 0$$

for
$$\lambda_{\mathcal{U}} \equiv \frac{d_{\mathcal{U}}}{4} \zeta^{d_{\mathcal{U}}-2} \Gamma(d_{\mathcal{U}}-1) \Gamma(2-d_{\mathcal{U}})$$
 and $(\mu_{\mathcal{U}}^2)^{2-d_{\mathcal{U}}} \equiv \kappa_{\mathcal{U}}^2 \frac{A_{d_{\mathcal{U}}}}{2\pi}$
 $V_{\text{eff}} = m^2 |H|^2 - \frac{2^{d_{\mathcal{U}}-1}}{d_{\mathcal{U}}} \lambda_{\mathcal{U}} (\mu_{\mathcal{U}}^2)^{2-d_{\mathcal{U}}} |H|^{2d_{\mathcal{U}}} + \lambda |H|^4$

Even if $m^2 = 0$ one can get the vacuum expectation value $\neq 0$ (Λ_U provides the scale):

$$v^{2} = \left(\frac{\lambda_{\mathcal{U}}}{\lambda}\right)^{\frac{1}{2-d_{\mathcal{U}}}} \mu_{\mathcal{U}}^{2} \quad \text{for} \quad \mu_{\mathcal{U}}^{2} = \left(\frac{A_{d_{\mathcal{U}}}}{2\pi}\right)^{\frac{1}{2-d_{\mathcal{U}}}} \left(\frac{\Lambda_{\mathcal{U}}^{2}}{M_{\mathcal{U}}^{2}}\right)^{\frac{d_{\mathsf{SM}}-2}{2-d_{\mathcal{U}}}} \Lambda_{\mathcal{U}}^{2}$$

UnCosmology

B. G. and Jose Wudka, "UnCosmology," arXiv:0809.0977

• The equation of state for unparticles

The trace anomaly of the energy momentum tensor for a gauge theory with massless fermions:

$$\theta^{\mu}_{\mu} = \frac{\beta}{2g} N \left[F^{\mu\nu}_{a} F_{a \ \mu\nu} \right] \tag{1}$$

where β denotes the beta function and N stands for the normal product. Non-trivial IR fixed point at $g = g_{\star}$, so in the IR we assume

$$\beta = \gamma(g - g_\star), \quad \gamma > 0$$

in which case the running coupling reads

$$g(\mu) = g_{\star} + c\mu^{\gamma}; \qquad \beta[g(\mu)] = \gamma c\mu^{\gamma}$$

where c is an integration constant and μ is the renormalization scale.

From the thermal average of (1) choosing the renormalization scale $\mu = T$ and using $\langle \theta^{\mu}_{\mu} \rangle = \rho_{\mathcal{U}} - 3p_{\mathcal{U}}$, we get

$$\rho_{\mathcal{U}} - 3p_{\mathcal{U}} = \frac{\beta}{2g_{\star}} \langle N \left[F_a^{\mu\nu} F_a_{\mu\nu} \right] \rangle = AT^{4+\gamma}$$

$$\rho_{\mathcal{U}} - 3p_{\mathcal{U}} = AT^{4+\gamma}$$

$$\Downarrow$$

$$\rho_{\mathcal{U}} = \sigma T^{4} + A\left(1 + \frac{3}{\gamma}\right)T^{4+\gamma} \quad \text{and} \quad p_{\mathcal{U}} = \sigma \frac{T^{4}}{3} + \frac{A}{\gamma}T^{4+\gamma}$$

where σ is an integration constant.

$$p_{\mathcal{U}} = \frac{1}{3} \rho_{\mathcal{U}} \left(1 - B \rho_{\mathcal{U}}^{\gamma/4} \right) \quad \text{for} \quad B \equiv \frac{A}{\sigma^{1+\gamma/4}}$$

 \downarrow

One can expect that $A\propto \Lambda_{\mathcal{U}}^{-\gamma}$, therefore we obtain

$$\rho_{\rm NP} = \frac{\pi^2}{30} T^4 \times \begin{cases} g_{\rm IR} + f\left(\frac{T}{\Lambda_{\mathcal{U}}}\right)^{\gamma} & \text{for} \quad T \lesssim \Lambda_{\mathcal{U}} \\ g_{\mathcal{B}\mathcal{Z}} & \text{for} \quad T \gtrsim \Lambda_{\mathcal{U}} \end{cases}$$

where $g_{\mathcal{BZ}} = 2(n_c^2 - 1 + \frac{7}{8}n_cn_f)$ for $SU(n_c)$ with n_f flavours in the \mathcal{BZ} sector.

- From the continuity at $T = \Lambda_{\mathcal{U}}$, the constant f could be determined: $f = g_{\mathcal{BZ}} g_{\mathrm{IR}}$.
- We will assume $g_{\mathcal{BZ}} \sim g_{\mathrm{IR}}$.

$$\rho_{\rm NP} = \frac{\pi^2}{30} T^4 \times \begin{cases} g_{\rm IR} + f \left(\frac{T}{\Lambda_{\mathcal{U}}}\right)^{\gamma} & \text{for} \quad T \lesssim \Lambda_{\mathcal{U}} \\ g_{\mathcal{B}\mathcal{Z}} & \text{for} \quad T \gtrsim \Lambda_{\mathcal{U}} \end{cases}$$

Deconstruction (Stephanov'07):

$$\mathcal{O}_{\mathcal{U}} \to \sum_{n=0}^{\infty} F_n \varphi_n \quad \text{with} \quad m_n^2 = \Delta^2 n$$

The above result fits the following guess for the effective number of degrees of freedom:

$$g_{\mathcal{U}}(T) \propto \frac{\int_0^{T^2} dM^2 \rho(M^2) \theta(\Lambda_{\mathcal{U}}^2 - M^2)}{\int_0^{\Lambda_{\mathcal{U}}^2} dM^2 \rho(M^2)}$$

where $\rho(M^2) \propto (M^2)^{(d_U-2)}$. Then

$$g_{\mathcal{U}}(T) \propto \left(\frac{T}{\Lambda_{\mathcal{U}}}\right)^{2(d_{\mathcal{U}}-1)}$$

 \implies In the presence of just one unparticle operator one can argue that $\gamma = 2(d_{\mathcal{U}} - 1)$.

• Freeze-out and thaw-in

Brief history of the Universe in the presence of unparticles (no mass-gap).

• $T \gg M_{\mathcal{U}}$: the \mathcal{BZ} sector in form of massless particles (no unparticles yet), thermal equilibrium with the SM is maintained (assumption), so $T = T_{\mathcal{BZ}} = T_{SM}$

• $T \lesssim M_{\mathcal{U}}$:

- The \mathcal{BZ} sector starts to decouple, as the average energy is no longer sufficient to create mediators.
- However, the thermal equilibrium may still be maintained $(T = T_{\mathcal{BZ}} = T_{SM})$ depending on the strength of effective couplings between the SM and the extra sector (which at higher temperature, $T \gtrsim \Lambda_{\mathcal{U}}$, is made of the \mathcal{BZ} matter, while below $\Lambda_{\mathcal{U}}$ of unparticles).

Let's denote by T_f the decoupling temperature at which

$$\Gamma(SM \leftrightarrow NP) \simeq H$$

where H is the Hubble parameter

$$H^{2} = \frac{8\pi}{3M_{Pl}^{2}}\rho_{\rm tot}(T) \quad \text{ for } \quad \rho_{\rm tot} = \rho_{\rm SM} + \rho_{\rm NP}$$

There are 2 interesting cases:

• $M_{\mathcal{U}} > T_f > \Lambda_{\mathcal{U}}$:

 $-T_f$ is determined by the condition

 $\Gamma(SM \leftrightarrow \mathcal{BZ}) \simeq H$

- For $T > T_f$ the SM and the \mathcal{BZ} sectors evolve in thermal equilibrium, but even for $T < T_f$ their temperatures remain equal $(T = T_{\mathcal{BZ}} = T_{SM})$ since $\Lambda_{\mathcal{U}} > v$.
- $\Lambda_{\mathcal{U}} > T_f$:
 - Till $T = \Lambda_{\mathcal{U}}$ the SM and unparticles still have the same temperature.
 - For $\Lambda_{\mathcal{U}} \gtrsim T \gtrsim T_f$ still the equilibrium is maintained (assumption, in general this depends on $d_{\mathcal{U}}$). The decoupling temperature T_f must be now determined by

$$\Gamma(SM \leftrightarrow \mathcal{O}_{\mathcal{U}}) \simeq H$$

- Till $T \sim v$ temperatures of SM and unparticles remain equal, at $T \sim v$ they split.
- \implies The unparticle cosmic background should be there.

♣ The Banks-Zaks phase.

$$\mathcal{L}_{\mathcal{B}\mathcal{Z}} = \frac{1}{M_{\mathcal{U}}} \left(H^{\dagger} H \right) \left(\bar{q}_{\mathcal{B}\mathcal{Z}} q_{\mathcal{B}\mathcal{Z}} \right)$$

Then

$$\Gamma_{\mathcal{B}\mathcal{Z}} \propto \frac{T^3}{M_{\mathcal{U}}^2}$$
 and $H \propto \frac{T^2}{M_{Pl}} \implies$ decoupling for $T \lesssim T_{f-\mathcal{B}\mathcal{Z}}$

♣ The unparticle phase.

$$\mathcal{L}_{\mathcal{U}} = c_{\mathcal{U}} \frac{\Lambda_{\mathcal{U}}^{d_{\mathcal{B}Z} - d_{\mathcal{U}}}}{M_{\mathcal{U}}^{k}} \mathcal{O}_{\mathcal{U}} \mathcal{O}_{\mathsf{SM}} \quad \text{for} \quad k = d_{\mathsf{SM}} + d_{\mathcal{B}Z} - 4$$

The most relevant operators for scalar unparticles are

$$\mathcal{L}_{s} = c_{\mathcal{U}}^{(s)} \frac{\Lambda^{1-d_{\mathcal{U}}}}{M_{\mathcal{U}}} \left(H^{\dagger}H \right) \mathcal{O}_{\mathcal{U}}, \ \mathcal{L}_{f} = c_{\mathcal{U}}^{(f)} \frac{\Lambda^{3-d_{\mathcal{U}}}}{M_{\mathcal{U}}^{3}} \left(\bar{\ell}He \right) \mathcal{O}_{\mathcal{U}}, \ \mathcal{L}_{v} = c_{\mathcal{U}}^{(v)} \frac{\Lambda^{3-d_{\mathcal{U}}}}{M_{\mathcal{U}}^{3}} \left(B_{\mu\nu}B^{\mu\nu} \right) \mathcal{O}_{\mathcal{U}},$$
$$\mathcal{L}_{s} \implies \Gamma_{\mathcal{U}} \propto \frac{\Lambda_{\mathcal{U}}^{3}}{M_{\mathcal{U}}^{2}} \left(\frac{T}{\Lambda_{\mathcal{U}}} \right)^{2d_{\mathcal{U}}-3} \quad \text{and} \quad H \propto \frac{T^{2}}{M_{Pl}} \implies T_{f-\mathcal{U}}$$

$$\frac{\Gamma_{\mathcal{U}}}{H} \propto T^{2d_{\mathcal{U}}-5} \qquad \Longrightarrow \qquad \left\{ \begin{array}{c} d_{\mathcal{U}} > \frac{5}{2} \\ d_{\mathcal{U}} < \frac{5}{2} \end{array} \right.$$

 $\begin{array}{ll} \mbox{decoupling for} & T < T_{f-\mathcal{U}} & \mbox{freeze-out} \\ \mbox{decoupling for} & T > T_{f-\mathcal{U}} & \mbox{thaw-in} \end{array}$

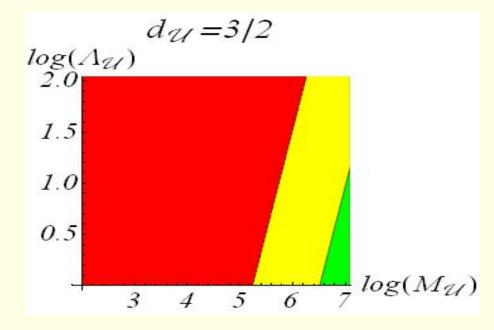


Figure 1: Regions of $(M_{\mathcal{U}}, \Lambda_{\mathcal{U}})$ for various scenarios of decoupling for $d_{\mathcal{U}} = 3/2$.

 $d_{\mathcal{U}} = 3$ $log(A_{\mathcal{U}})$ 1.5 1.0 0.5 $3 \ 4 \ 5 \ 6 \ 7 \ log(M_{\mathcal{U}})$

Figure 2: Regions of $(M_{\mathcal{U}}, \Lambda_{\mathcal{U}})$ for various scenarios of decoupling for $d_{\mathcal{U}} = 3$.

	decoupling in \mathcal{BZ} phase	decoupling in the unparticle phase
green	+	+
blue	—	+
yellow	+	—
red	—	_

• BBN constraints

Big-Bang Nucleosynthesis $\implies \Delta N_{\nu} = -0.37^{+0.10}_{-0.11} \implies$ upper limit for $g_{\rm IR}$

• Assume freeze-out above the EW scale $(T_f > v = 246 \text{ GeV}, \mathcal{L} \propto H^{\dagger} H \mathcal{O}_{\mathcal{U}})$

• Assume freeze-out below T_{BBN} ($T_{f-U} < T_{BBN}$, $\mathcal{L} \propto B_{\mu\nu}B^{\mu\nu}\mathcal{O}_{\mathcal{U}}$)

$$g_{\rm IR} = \frac{7}{4} \Delta N_{\nu} \implies g_{\rm IR} \lesssim 0.05 \text{ at } 4\sigma$$

Summary

- Intensive activity on unparticles (~ 200 citations of the first Georgi's paper)
- Interesting and exotic phenomenology
- Unparticles could be deconstructed
- Troubles with IR divergences
- Cosmological consequences
 - Rough arguments for the equation of state for unparticles: $p_{\mathcal{U}} = \frac{1}{3}\rho_{\mathcal{U}} \left| 1 B\rho_{\mathcal{U}}^{\delta/4} \right|$
 - Rough arguments for the energy density for unparticles "derived":

$$\rho_{\rm NP} = \frac{\pi^2}{30} T^4 \times \begin{cases} \left[g_{\rm IR} + \left(g_{\mathcal{B}\mathcal{Z}} - g_{\rm IR} \right) \left(\frac{T}{\Lambda_{\mathcal{U}}} \right)^{\gamma} \right] & \text{for} \quad T \lesssim \Lambda_{\mathcal{U}} \\ g_{\mathcal{B}\mathcal{Z}} & \text{for} \quad T \gtrsim \Lambda_{\mathcal{U}} \end{cases}$$

- Unparticles in equilibrium: freeze-out and thaw-in.
- BNN bounds on the number of degrees of freedom for unparticles.

Experimental constraints

From A. Freitas and D. Wyler, "Astro Unparticle Physics", arXiv:0708.4339.

$$\mathcal{L}_{\mathcal{U}ff} = \frac{c_{\mathrm{V}}}{M_{\mathrm{Z}}^{d_{\mathcal{U}}-1}} \bar{f}\gamma_{\mu}f O_{\mathcal{U}}^{\mu} + \frac{c_{\mathrm{A}}}{M_{\mathrm{Z}}^{d_{\mathcal{U}}-1}} \bar{f}\gamma_{\mu}\gamma_{5}f O_{\mathcal{U}}^{\mu} + \frac{c_{\mathrm{S1}}}{M_{\mathrm{Z}}^{d_{\mathcal{U}}}} \bar{f}\mathcal{D}f O_{\mathcal{U}} + \frac{c_{\mathrm{S2}}}{M_{\mathrm{Z}}^{d_{\mathcal{U}}}} \bar{f}\gamma_{\mu}f \partial^{\mu}O_{\mathcal{U}} + \frac{c_{\mathrm{S1}}}{M_{\mathrm{Z}}^{d_{\mathcal{U}}}} \bar{f}\gamma_{\mu}\gamma_{5}f \partial^{\mu}O_{\mathcal{U}}.$$

Here the coefficients have been scaled to a common mass, chosen as the Z-boson mass M_Z , so that the only unknown quantities are the dimensionless coupling constants c_i .

Coupling	c_{V}				c_{A}			
$d_{\mathcal{U}}$	1	4/3	5/3	2	1	4/3	5/3	2
5th force	$7 \cdot 10^{-24}$	$1.4 \cdot 10^{-15}$	$1.8 \cdot 10^{-10}$	$2 \cdot 10^{-5}$	$4 \cdot 10^{-24}$	$8 \cdot 10^{-16}$	$1 \cdot 10^{-10}$	$1.1 \cdot 10^{-5}$
Star cooling	$5 \cdot 10^{-15}$	$2.5\cdot 10^{-12}$	$1 \cdot 10^{-9}$	$3.5 \cdot 10^{-7}$	$6.3 \cdot 10^{-15}$	$2 \cdot 10^{-12}$	$7.3 \cdot 10^{-10}$	$3 \cdot 10^{-7}$
SN 1987A	$1 \cdot 10^{-9}$	$3.5 \cdot 10^{-8}$	$1 \cdot 10^{-6}$	$3 \cdot 10^{-5}$	$2 \cdot 10^{-11}$	$5.5 \cdot 10^{-10}$	$1.5 \cdot 10^{-8}$	$4.1 \cdot 10^{-7}$
LEP	0.005	0.045	0.04	0.01	0.1	0.045	0.04	0.008
Tevatron		0.4	0.05					
ILC	$1.6 \cdot 10^{-4}$	$1.4 \cdot 10^{-3}$	$1.3 \cdot 10^{-3}$	$3.2 \cdot 10^{-4}$	$3.2 \cdot 10^{-3}$	$1.4 \cdot 10^{-3}$	$1.3 \cdot 10^{-3}$	$2.5 \cdot 10^{-4}$
LHC		0.25	0.02					
Precision	1	0.2	0.025		1	0.15	0.01	
Quarkonia		0.01	0.1	0.45				
Positronium		0.25				$2 \cdot 10^{-13}$	$2 \cdot 10^{-8}$	0.03
·	•	•	•	•	•		•	

Coupling	$c_{\rm S1}$				c_{P1} , $2c_{\mathrm{P2}}$			
$d_{\mathcal{U}}$	1	4/3	5/3	2	1	4/3	5/3	2
5th force	$6.5 \cdot 10^{-22}$	$1.2 \cdot 10^{-13}$	$1.6 \cdot 10^{-8}$	$1.7 \cdot 10^{-3}$	—	—	—	—
Star cooling	$1.3 \cdot 10^{-9}$	$7 \cdot 10^{-7}$	$3 \cdot 10^{-4}$	0.13	$4 \cdot 10^{-8}$	$1.1 \cdot 10^{-5}$	$3.3 \cdot 10^{-3}$	1
SN 1987A	$8 \cdot 10^{-8}$	$2.4 \cdot 10^{-6}$	$6.6 \cdot 10^{-5}$	$2 \cdot 10^{-3}$	$5.5 \cdot 10^{-8}$	$1.3 \cdot 10^{-6}$	$3.5 \cdot 10^{-5}$	$9 \cdot 10^{-4}$
LEP	> 1	> 1	> 1	> 1	> 1	> 1	> 1	> 1
ILC	> 1	> 1	> 1	> 1	> 1	> 1	> 1	> 1

From A. Freitas and D. Wyler, "Astro Unparticle Physics", arXiv:0708.4339 [hep-ph].

HEIDI

Jochum van der Bij and S. Dilcher:

- 1. J. J. van der Bij and S. Dilcher, "HEIDI and the unparticle," Phys. Lett. B 655, 183 (2007) [arXiv:0707.1817 [hep-ph]].
- J. J. van der Bij and S. Dilcher, "A higher dimensional explanation of the excess of Higgs-like events at CERN LEP," Phys. Lett. B 638, 234 (2006) [arXiv:hep-ph/0605008].
- 3. J. J. van der Bij, "The minimal non-minimal standard model," Phys. Lett. B 636, 56 (2006) [arXiv:hep-ph/0603082].

The model:

• Extra-dimensional (δ) scalars neutral under the SM gauge group

$$\phi(x,y) = \frac{1}{\sqrt{2}L^{\delta/2}} \sum_{\vec{k}} \phi_{\vec{k}}(x) e^{i\frac{2\pi}{L}\vec{k}\vec{y}}$$

• Extra terms in the scalar potential

$$V(H,\phi) = \dots - \frac{\lambda_1}{8} (2f_1\phi - |H|^2)$$

Similarities:

• The continuous mass spectrum e.g. for $s \to \infty: \ \rho(s) \sim s^{-3+\delta/2}$

Differences

- In HEIDI only scalars, while unparticles could have any spin
- Van der Bij and Dilcher don't assume scale invariance of the extra sector
- In HEIDI interactions between the SM and the extra scalars assumed to be renormalizable
- Van der Bij and Dilcher claim that only for $0 < \delta < 1$ there is no tachyons in the scalar spectrum, so the potential is stable $(1 < d_{\mathcal{U}} < 2)$