

# How masses have been generated in the early Universe

J.Iliopoulos

Ecole Normale Supérieure, Paris

Warsaw, June 3 2013



▶ **Where**

▶ **Where**

▶ **What**

- ▶ **Where**
- ▶ **What**
- ▶ **Why**



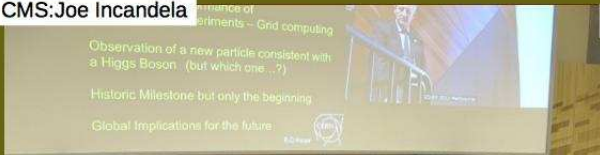


CMS: Joe Incandela

# Journée historique : 4 Juillet 2012



ATLAS: Fabiola Gianotti



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- ▶ **The discovery itself was a triumph of technology and ingeniouity**
- ▶ **But the excitement was mainly due to its potential theoretical significance**

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- A problem of mass
- Brief Historical Remarks
- The next Steps
- Do we understand the Physics?

# A problem of mass

or, why are we not pure spirits!

- ▶ **Why most, but not all, particles are massive?**

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- ▶ The most **natural** solution would be to have  $m = 0$  for all elementary particles

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- ▶ **The most **natural** solution would be to have  $m = 0$  for all elementary particles**
- ▶ **For the constituents of matter**  
Spin 1/2 fermions
- ▶ **For the intermediaries of the interactions**  
The gauge bosons

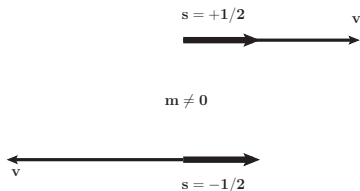
# A problem of mass

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## For the fermions because of chirality

We need both chiralities in order to build a massive fermion

But weak interactions use only one





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- ▶ **For the gauge bosons  $m = 0$  is a geometrical property**
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- ▶ Under gauge transformations, *i.e.*  $\theta(x) \Rightarrow \theta_i$ , the term:

$\bar{\Psi}_i\Psi_{i+1}$  transforms in  $e^{-i\theta_i}\bar{\Psi}_i\Psi_{i+1}e^{i\theta_{i+1}}$

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- ▶ The gauge potentials live on the oriented lattice links
- ▶ On the lattice gauge invariance establishes a long range order.
- ▶ The gauge bosons are massless.

# Brief Historical Remarks

- **I. Spontaneous Symmetry Breaking**
- **II. Spontaneous Br. of Chiral Symmetry**
- **III. Spontaneous Br. of a gauge Symmetry**

# Brief Historical Remarks I.

- **Spontaneous Symmetry Breaking** (Euler??)
  - ▶ A critical point

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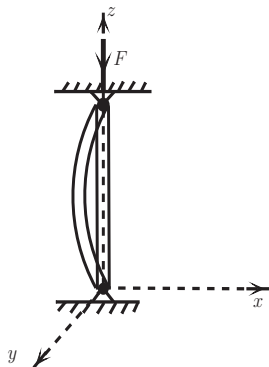
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  - ▶ A critical point
  - ▶ Instability of the symmetric solution
  - ▶ The ground state is degenerate  $\Rightarrow$  Massless excitations

# Brief Historical Remarks I.

- An example from Classical Mechanics



$$IE \frac{d^4 X}{dz^4} + F \frac{d^2 X}{dz^2} = 0 \quad ; \quad IE \frac{d^4 Y}{dz^4} + F \frac{d^2 Y}{dz^2} = 0$$

$$X = X'' = Y = Y'' = 0 \text{ for } z = 0 \text{ and } z = l$$

A symmetric solution always exists:  $X = Y = 0$

# Brief Historical Remarks I.

- ▶ For  $F \geq F_{cr} = \frac{\pi^2 EI}{l^2}$  asymmetric solutions appear:

$$X = C \sin kz \quad ; \quad kl = n\pi \quad ; \quad n = 1, \dots \quad ; \quad k^2 = F/EI$$

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- ▶ The ground state is degenerate.  $\Rightarrow$
- ▶ We cannot predict which direction the rod is going to bend

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- ▶ In quantum physics this implies zero mass particles

*The Goldstone particles*

## Brief Historical Remarks II.

- **Spontaneous Breaking of Chiral Symmetry**

- ▶ M. Gell-Mann and M. Lévy **Nuov. Cim. 16 (1960) 605**

The axial vector current in beta decay

The celebrated  $\sigma$ -model. No explicit mentioning of spontaneous symmetry breaking.

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Dynamical Models of Elementary Particles based on an Analogy with Superconductivity.

- ▶ 1962-1970: Current Algebras, Chiral Lagrangians, PCAC,....

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- **Spontaneous Symmetry Breaking in the presence of Gauge Interactions**
  - ▶ Two parallel stories
  - ▶ The Theory of Superconductivity
  - ▶ The Gauge Theories of Elementary Particles
  - ▶ They developed independently and often ignored each other

# Spontaneous Symmetry breaking in the Theory of Superconductivity

- ▶ L.D. Landau and B.L. Ginzburg **JETP 20 (1950) 1064**

$$\Delta \vec{A} = \dots + \frac{4\pi e^2}{mc^2} |\Psi|^2 \vec{A} \Rightarrow \vec{A}(x) \sim \vec{A}(0) e^{-x/\lambda}$$

*Note: no-one in the subsequent list refers to this paper*

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- ▶ Bardeen, Cooper and Schrieffer (BCS) **Phys. Rev. 108 (1957) 1175**
- ▶ P.W. Anderson **Phys. Rev. 112 (1958) 1900 ; 110 (1958) 827**

“Random Phase Approximation in the Theory of Superconductivity”

In BCS  $\Rightarrow$  Mass gap, + Longitudinal waves

From the Abstract : “The theory... is gauge invariant to an adequate degree throughout.”

# Spontaneous Symmetry breaking in the Theory of Superconductivity

- ▶ P.W. Anderson *Phys. Rev.* **130** (1963) 439

“Plasmons, Gauge invariance and Mass”

Shows that BCS exemplifies Schwinger’s programme.

From the Abstract : “Schwinger has pointed out that the Yang-Mills vector boson (*He only considers Abelian theories*) .....does not necessarily have zero mass.....We show that the theory of plasma oscillations is a simple non-relativistic example exhibiting all of the features of Schwinger’s idea.”

# Spontaneous Symmetry breaking in the Theory of Superconductivity

- ▶ Yoichiro Nambu *Phys. Rev.* **117** (1959) 648

“Quasi-Particles and Gauge Invariance in the Theory of Superconductivity”

BCS theory in the Hartree-Fock approximation. Shows the existence of solutions with a mass gap. Correct discussion of the properties of gauge invariance.

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- ▶ J. Goldstone *Nuov. Cim.* **19** (1961) 154

“Field Theories with “Superconductor” Solutions.

Although the word “Superconductor” appears in the title, the paper is a field theory example of what became known as “The Goldstone Theorem”.

# Spontaneous Symmetry breaking in the Gauge Theories of Elementary Particles. Early attempts

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“Gauge Invariance and Mass”

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- ▶ Julian Schwinger **Phys. Rev. 128 (1962) 2425**

“Gauge Invariance and Mass II”

The Schwinger Model (2-d QED)

*Note: No references to superconductivity*

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- ▶ In fact, Schwinger had understood the connection earlier.

From Feynman's Summary Talk at the Aix-en-Provence Conference on Elementary Particles, Sept. 14-20 1961:

“.....Since gauge invariance is usually believed to imply that the mass [of the gauge bosons] is zero, the first prediction of these theories ..... is disregarded. Schwinger pointed out to me however, that one can use gauge invariance to prove that the mass of the real photon is equal to zero, only if one assumes that in the complete dressed photon, there is a finite amplitude to find the undressed one.”



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- ▶ M. Lévy *Phys. Lett.* **7** (1963) 36 ; *Nucl. Phys.* **57** (1964) 152

Non-local, gauge invariant, QED with a massive photon

# Spontaneous Symmetry breaking in the Gauge Theories of Elementary Particles. Early attempts

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⇒ A massless particle.

On the other we had Anderson's non-relativistic counter example.

Could we find relativistic analogues?

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- ▶ A. Klein and B.W. Lee *Phys. Rev. Lett.* **12** (1964) 266

Does Spontaneous Breakdown of Symmetry Imply Zero-Mass Particles?

M. Baker, K. Johnson, B.W. Lee *Phys. Rev.* **133 B** (1964) 209

Broken Symmetries and Zero-Mass Bosons

# Spontaneous Symmetry breaking in the Gauge Theories of Elementary Particles. Early attempts

- ▶ W. Gilbert *Phys. Rev. Lett.* **12** (1964) 713

“Broken Symmetries and Massless Particles”

A no-go Theorem !!

$$\text{Sp. Sym. Br.} \Rightarrow \exists A \quad \langle 0|[Q, A]|0 \rangle \neq 0 \quad (1)$$

$$\mathcal{A}_\mu(k) = \int d^4x e^{ikx} \langle 0|[j_\mu(x), A(0)]|0 \rangle = k_\mu F(k^2) \quad (2)$$

by Lorentz invariance and  $F(k^2) \neq 0$  by (1)

$$\text{But } k^\mu \mathcal{A}_\mu = 0 \Rightarrow k^2 F(k^2) = 0 \quad F(k^2) \sim \delta(k^2) \Rightarrow$$

A massless particle

In a non-relativistic theory (2) does not hold.

**Problem:** Find the error!

# Spontaneous Symmetry breaking in the Gauge Theories of Elementary Particles. The solution

- ▶ F. Englert and R. Brout *Phys. Rev. Lett.* **13** (1964) 321

The solution as we know it to-day, using elementary scalar fields.

Some remarks on the possibility of dynamical symmetry breaking.

Abelian, Non-Abelian and chiral models are considered.

The motivation was mainly centred in strong interactions.

References include SSB (Nambu *et al*), Schwinger and Sakurai.

# Spontaneous Symmetry breaking in the Gauge Theories of Elementary Particles. The solution

- ▶ P. Higgs *Phys. Lett.* **12** (1964) 132

Explicit example answering Gilbert's objection. The Abelian model in the Coulomb gauge.

References include SSB, Klein+Lee and Gilbert

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- ▶ P. Higgs *Phys. Rev. Lett.* **13** (1964) 508

Explicit example of the Abelian model. Discussion of the  $SU(3)$  Sakurai model for strong interactions.

Explicit connection between would-be Goldstone modes and longitudinal polarisations of the massive vector bosons.

Connection with superconductivity.

References include Goldstone, Anderson, Brout+Englert, Sakurai.

# Spontaneous Symmetry breaking in the Gauge Theories of Elementary Particles. The solution

G.S. Guralnik, C.R. Hagen and T.W.B. Kibble *Phys. Rev. Lett.* **13** (1964) 585

Detailed discussion of the Abelian model. Explicit counting  $3=2+1$ .

Vague connection to superconductivity. No references.

References include Goldstone, Gilbert, Brout+Englert (published), Higgs (preprint)



# The Synthesis

S. Weinberg *Phys. Rev. Lett.* **19** (1967) 1264

The Englert-Brout-Higgs mechanism in the electroweak interactions. The same mechanism gives masses to the fermions.

# SSB: Gauge Symmetries. Conclusions:

## The Englert-Brout-Higgs Mechanism

- The vector bosons corresponding to spontaneously broken generators of a gauge group become massive.
- The corresponding Goldstone bosons decouple and disappear from the physical spectrum.
- Their degrees of freedom become the longitudinal components of the vector bosons.
- Gauge bosons corresponding to unbroken generators remain massless.
- There is always at least one physical, massive, scalar particle.
- The same mechanism gives masses to the fermions.

# SSB: Gauge Symmetries. Later developments

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The consequences of the symmetry are encoded in the invariance under BRST transformations. This invariance is not broken.

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The consequences of the symmetry are encoded in the invariance under BRST transformations. This invariance is not broken.

- ▶ In the lattice formulation gauge symmetry is exact.  $\Rightarrow$

Elitzur's Theorem: **There exists no local order parameter for a gauge symmetry in which the fields take values in a compact manifold.**

# The next steps

## The Hunting is over. Taming of the beast

- ▶ Study its properties. Measure as many branching ratios as possible.

$$\Gamma_{b\bar{b}} \quad \Gamma_{\tau^+\tau^-}, \dots$$

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- ▶ Need for a dedicated collider??

# Do we understand the Physics?

TABLE OF ELEMENTARY PARTICLES		
QUANTA OF RADIATION		
Strong Interactions	Eight gluons	
Electromagnetic Interactions	Photon ( $\gamma$ )	
Weak Interactions	Bosons $W^+$ , $W^-$ , $Z^0$	
Gravitational Interactions	Graviton (?)	
MATTER PARTICLES		
	Leptons	Quarks
1st Family	$\nu_e, e^-$	$u_a, d_a, a = 1, 2, 3$
2nd Family	$\nu_\mu, \mu^-$	$c_a, s_a, a = 1, 2, 3$
3rd Family	$\nu_\tau, \tau^-$	$t_a, b_a, a = 1, 2, 3$
HIGGS BOSON		

**Table:** This Table shows our present ideas on the structure of matter. Quarks and gluons do not exist as free particles and the graviton has not yet been observed.

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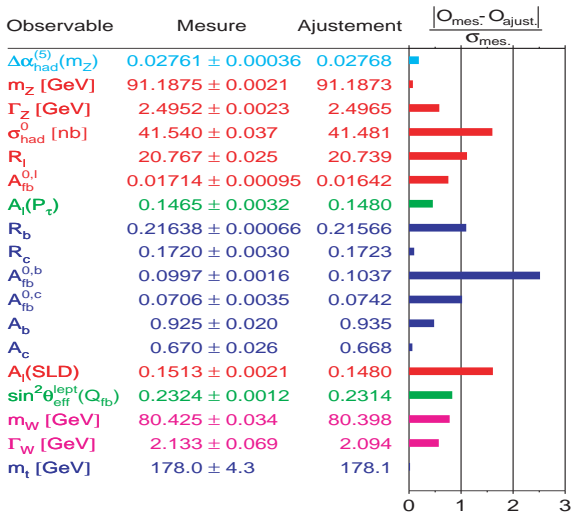
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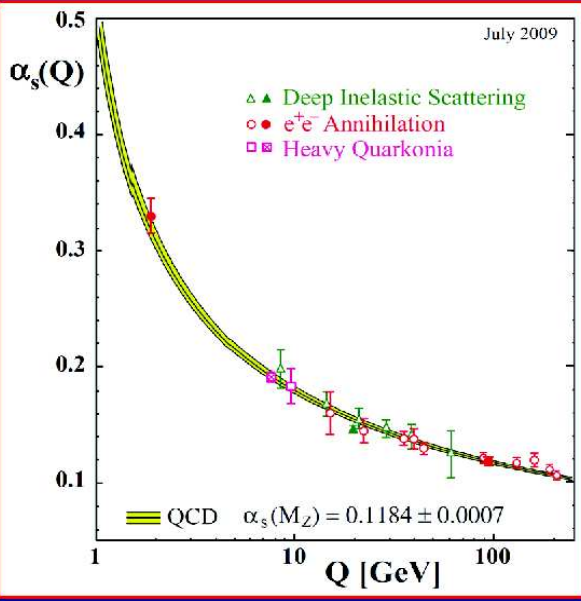
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July 2009



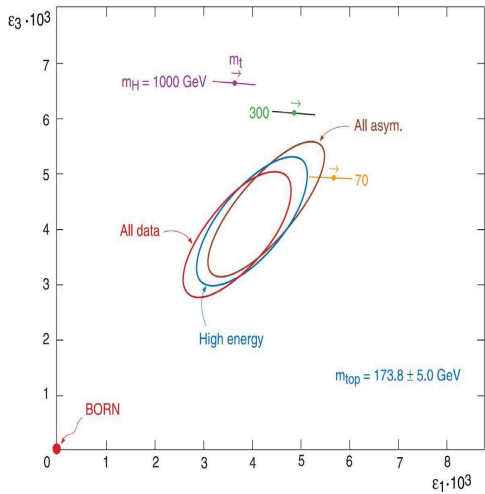


Figure 6: Data vs theory in the  $\epsilon_3$ - $\epsilon_1$  plane (notations as in fig.5)

$$\epsilon_1 = \frac{3G_F m_t^2}{8\sqrt{2}\pi^2} - \frac{3G_F m_W^2}{4\sqrt{2}\pi^2} \tan^2 \theta_W \ln \frac{m_H}{m_Z} + \dots \quad (1)$$

$$\epsilon_3 = \frac{G_F m_W^2}{12\sqrt{2}\pi^2} \ln \frac{m_H}{m_Z} - \frac{G_F m_W^2}{6\sqrt{2}\pi^2} \ln \frac{m_t}{m_Z} + \dots \quad (2)$$



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- ▶ A necessary condition for the consistency of the Model is that  $\sum_i Q_i = 0$  inside each family.

When the  $\tau$  lepton was discovered the  $b$  and  $t$  quarks were predicted with the right electric charges.

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- ▶ The final touch: The recent discovery of the Brout-Englert-Higgs scalar

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- ▶ Do we need a third world, The world of scalars?

Many arbitrary parameters. Their masses are unstable **Why??**

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- ▶ Could the scalars become also geometrical?

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- ▶ Question: Is there a space on which Internal symmetry transformations act as Diffeomorphisms?
- ▶ Answer: Yes, but it is a space with non-commutative geometry.

A space defined by an algebra of matrix-valued functions

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