

# $Z_{12}$ ORBIFOLD COMPACTIFICATION

## TOWARD STANDARD MODEL

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1. Introduction
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5. Harmless R-parity violation

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# I. Introduction

Standard model with 45 (+3) chiral fields are remarkable.

"How does this standard model arise?"  
(Big problem)

There were attempts to obtain from superstring, but a model free of any phenomenological problems has not appeared yet.

So still search for a good string vacuum is an important issue. (LHC, PLANCK, CAST, PVLAS)

Here, we follow the compactification route through orbifold. (The easiest way.) It is basically a geometric one.

Manifold with discrete action  
 $\Rightarrow$  orbifold

Supersymmetric standard model We have

- $\Rightarrow$  Directly from compactification (KKK)
- $\Rightarrow$  Through intermediate GUTs (K-Kyae)

Early attempts were just  
standard-like models

$$\left\{ \begin{array}{l} SU(3) \times SU(2) \times U(1)^n \\ 3 \text{ families} \end{array} \right.$$

late '80s

Recently, more ambitious attempts  
were tried.

From orbifold compactification, we obtain

$$\left\{ \begin{array}{l} SU(3)^3 \quad \text{trifurcation} \\ SU(5) \times U(1) \quad \text{flipped } SU(5) \\ SU(3) \times SU(2) \times U(1) \quad \text{SM} \end{array} \right.$$

← also  
from  
fermionic  
construc.  
also

There was the adjoint problem that at  $k=1$  (Kac-Moody level) no adjoint is possible. Thus, **GUTs  $SU(5)$ ,  $SO(10)$   $E_6$**  are **not good** toward MSSM.

This prefers GUTs with factor groups:

$$SU(3)^3$$

$$SU(4) \times SU(2) \times SU(2)$$

$$SU(5) \times U(1)$$

← best for  $\sin^2 \theta_w$

} manageable with matter content

OR **DIRECTLY**

**Standard model**

(KIM, KIM, KYAE)

There are several problems to be solved:

1. Approximate  $R$  parity, for proton longevity
2. Exotics problem: if exotics are not removed, severe phen. prob.
3. Vectorlike pairs problem
4. Successful fit to quark and lepton masses and mixing angles
5. Strong  $CP$  problem, etc.

The most important thing to be solved is the  $R$  parity problem: proton must live long enough!!!

SO(10) GUT : R-parity  $-1 -1 1$

Spinor, Vector  $\Rightarrow$  Yukawa  $SSV$

But if we consider nonrenormalizable couplings with singlets attached, there must be some conditions.  $SSV111\dots$

Exactly, this kind of affair arises in string compactification. Namely, R-parity condition is the most perilous disaster. I guess all string compactifications assumed R so far.

No global U(1) allowed.

NOTE

But discrete symmetry may be allowed.

For the discrete symmetry to be good,  
it must be discrete gauge symmetry.  
We consider global  $U(1)$ s,  
which must be approximate.

So most likely, the R-parity is  
approximate. We hope that it is

Approximate but sufficiently suppressed

R violating terms are  $\left\{ \begin{array}{l} \text{I.W. Kim} \\ \text{J. EK} \\ \text{B. Kyae} \end{array} \right.$

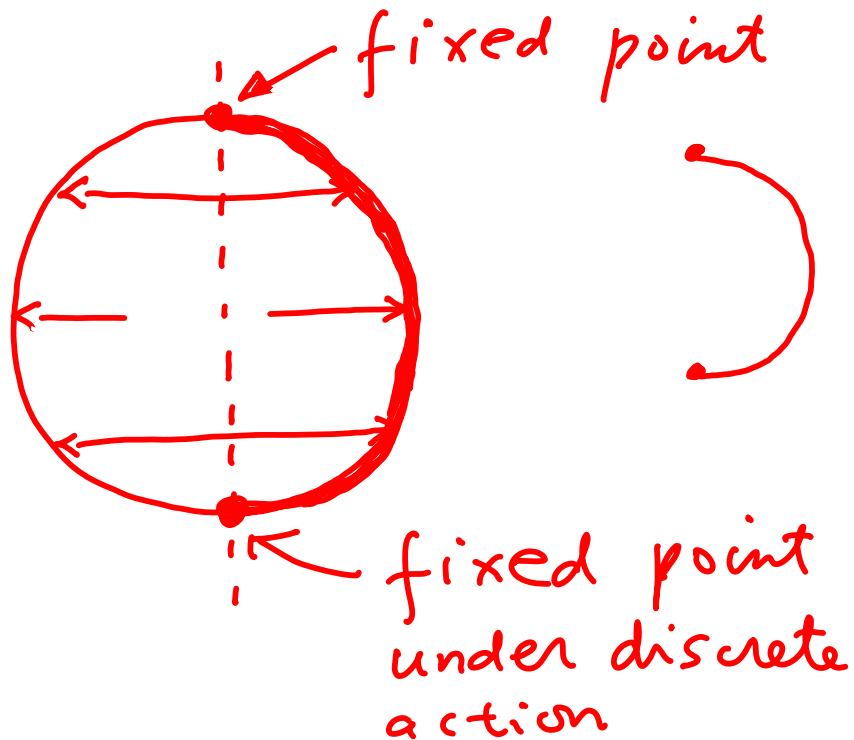
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# II Strings on Orbifolds

Manifolds moded by discrete action

$$S^1 / \mathbb{Z}_2$$

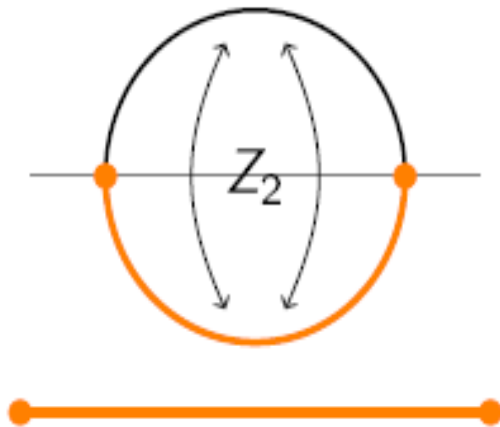


fundamental region is a line with boundary

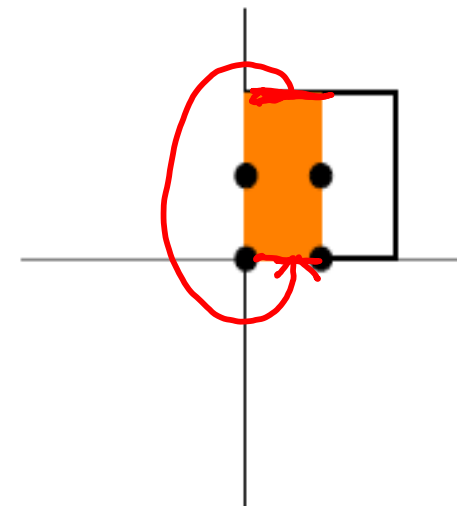
## ■ Orbifold Compactification

- ▶ Orbifold can be obtained by identifying a manifold by discrete action.

The simplest orbifold is  $S^1/\mathbb{Z}_2$ .



two dimensional version  $T^2/\mathbb{Z}_2$



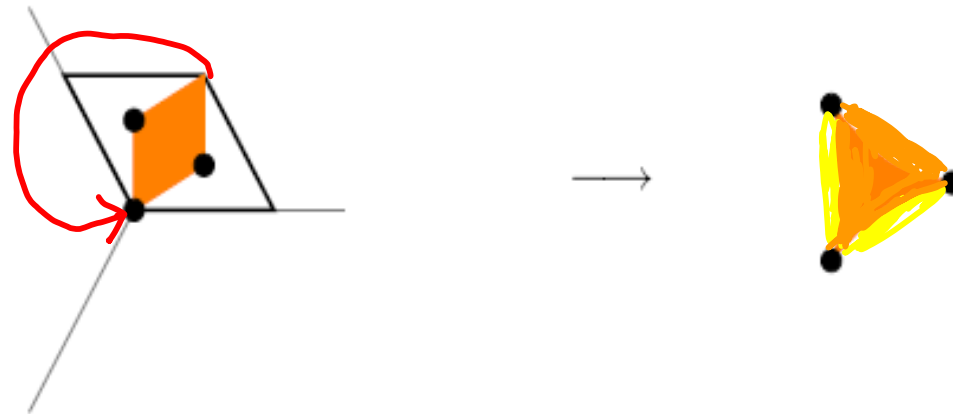
$$(x, y) \leftrightarrow (-x, -y)$$



4 fixed  
pts

For specially symmetric manifold, we can mod out the manifold by different discrete group.

e.g.)  $T^2/Z_3$



We compactify 6 dimensions. We consider a flat internal space only except singular fixed points. Starting from

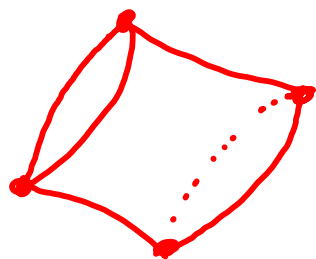
$T^6 = T^2 \otimes T^2 \otimes T^2$ , identify the space by

$$z = (z_1, z_2, z_3) \sim \theta \cdot z = (e^{2\pi i \phi_1} z_1, e^{2\pi i \phi_2} z_2, e^{2\pi i \phi_3} z_3).$$

For  $Z_N$  string orbifold, consistent condition  $\theta^N = 1$  for world-sheet spinor requires

$$N \sum_i \phi_i = \text{even integer}$$

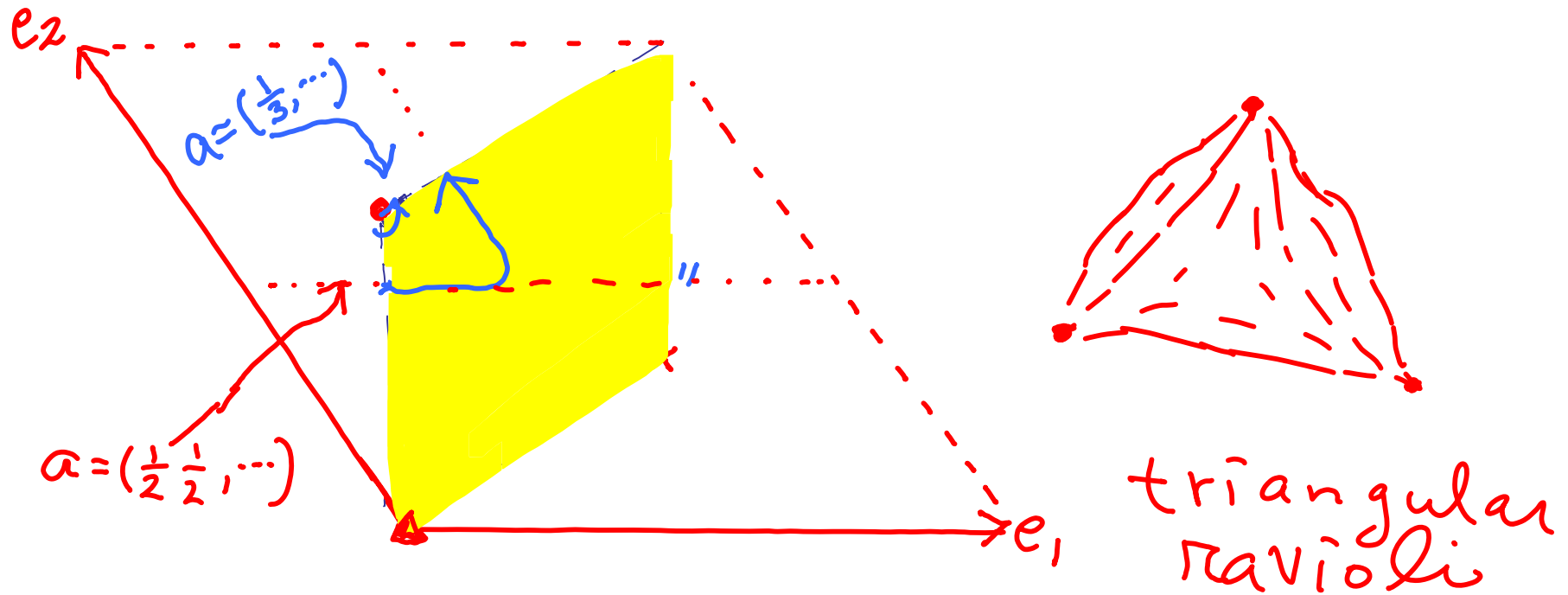
$S_2/Z_2$



pillow  
four fixed points

$(E_x) T_2 / Z_3$

$120^\circ$  rotation = discrete action



6 internal space compactified

$T_6 / Z_3$  : 27 fixed points

Six internal space  $\phi = (\frac{2}{3} \frac{1}{3} \frac{1}{3})$

We embed this orbifold action in  $E_8 \times E_8'$  group space

$$(\underbrace{\nu \nu \nu \nu \nu \nu \nu \nu}_{E_8}) (\underbrace{\nu \nu \nu \nu \nu \nu \nu \nu}_{E_8'})'$$

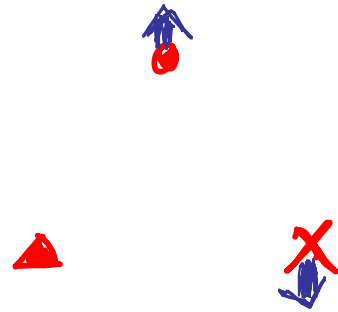
Standard embedding

$$V \equiv (\frac{2}{3} \frac{1}{3} \frac{1}{3} 0 0 0 0 0) (0 0 0 0 0 0 0 0)'$$

$$E_8 \longrightarrow E_6$$

Wilson lines : e.g.  $a_i = (0 0 0 \frac{2}{3} \frac{1}{3} \frac{1}{3} 0 0) (0)'$

If Wilson lines are present, then 3 fixed points are distinguished



3 fixed points are distinguished by fluxes, or Wilson lines

$V$	$V+a_3$	$V-a_3$
$V+a_1$	$V+a_3+a_1$	---
$V-a_1$	$V+a_3-a_1$	-----

# II Model : $Z_{12-I}$ Model

$$\phi = \left( \frac{5}{12} \quad \frac{4}{12} \quad \frac{1}{12} \right)$$

$Z_{12}$  prime  
 1 fixed pt.  
 $Z_3$   
 3 fixed pts

: In total, 3 fixed points

flipped  $SU_5$

$$V = \left( \frac{1}{4} \frac{1}{4} \frac{1}{4} \frac{1}{4} \frac{1}{4} \frac{5}{12} \frac{6}{12} 0 \right) \left( \frac{2}{12} \frac{2}{12} 0 0^5 \right)$$

$$a_3 = a_4 = \left( 0^5 \quad 0 \quad \frac{-1}{3} \quad \frac{1}{3} \right) \left( 0 \quad 0 \quad \frac{2}{3} \quad 0^5 \right)$$

$$a_1 = a_2 = a_5 = a_6 = 0$$

Kyae + JEK  
 th/0608085  
 86



Gauge group

$$\underbrace{SU(5) \times U(1) \times U(1)}_X^3 \times SU(2)' \times SO(10)' \times U(1)'^2$$

flipped  $SU(5)$

← NHE from  
fermionic construction

which can be broken by  $\langle 10_1 \rangle$

to SM. This model gives

3 families plus 1 pair of

Higgs doublets, by Yukawa

couplings of cubic order.

• Spectrum of the model

There are 12 sectors from  $Z_{12}$  twisting.

Self CPT conjugate  
 $\overbrace{\left( \begin{array}{c} Untwisted \\ T6 \end{array} \right)}$

$$T1 \xleftrightarrow{CPT} T11$$

$$T2 \xleftrightarrow{CPT} T10$$

No T3, T9

$$T4 \xleftrightarrow{CPT} T8$$

$$T7 \xleftrightarrow{CPT} T5$$

Each sector has three subsectors distinguished by Wilson line.

$T_6 T_6 U_2$

$U : (1_{-5} + 5_3 + \overline{10}_{-1})_{U_3}, (\overline{5}_2)_{U_2},$   
 $(1_{-5} + 5_3 + \overline{10}_{-1})_{U_1}, (1_0)_{U_2},$

$T_6 : \overline{10}_{-1} + \{2(1_{-5} + 1_5 + 5_{-3} + \overline{5}_3)$   
 $+ 3(\overline{10}_{-1} + 10_1)\} + 22\{1_0\},$

Breaks  
 $\swarrow$  SUSY

(Murayama)  
 -95

$T_6 T_2 T_4$

$T_2 : 1_{-5} + 5_3$   
 $+ 11\{1_0\} + 4D + 010 + 0\overline{16}$

$T_4 : 5_{-2} + 2(5_{-2} + \overline{5}_2) + 30\{1_0\} + 12D,$

$T_1 : 2(\overline{5}_{-\frac{1}{2}}) + 2(5_{+\frac{1}{2}}) + 6(1_{-\frac{5}{2}}) + 6(1_{+\frac{5}{2}})$   
 $+ (D1_{+\frac{5}{2}}) + (D1_{-\frac{5}{2}}),$

$T_7 : 2(5_{+\frac{1}{2}}) + 2(\overline{5}_{-\frac{1}{2}}) + 6(1_{+\frac{5}{2}}) + 6(1_{-\frac{5}{2}})$   
 $+ (D1_{+\frac{5}{2}}) + (D1_{-\frac{5}{2}}),$

$$UT : (1_{-5} + 5_3 + \overline{10}_{-1})^L_{U_3}, (\overline{5}_2)^L_{U_2}, (1_{-5} + 5_3 + \overline{10}_{-1})^L_{U_1}, 1^L_{U_2}$$

$$T_6 : T_6^0 \quad T_6^+ \quad T_6^- \quad \text{distinguished by Wilson line}$$

$$T_1^{0+-} : \text{No } E_8 \text{ spectrum}$$

$$T_2^{0+-} : \text{Yes observ. matter}$$

$$T_3 : \text{No matter}$$

$$T_4^{0+-} : \text{Yes}$$

$$T_5^{0+-} : \text{Exotic matter } Q_{em} = \pm \frac{1}{2}, \pm \frac{1}{6}$$

$\rightarrow T_7$  (opposite chirality)
  $\swarrow$  Quarks

Visible states	$SU(5) \times U(1)_X$	$\Gamma$	Visible states	$SU(5) \times U(1)_X$	$\Gamma$
$(\underline{+ - - - -}; + + +)$	$5_3^L (U_3)$	3	$(\underline{1, 0, 0, 0, 0}; \frac{-1}{3}, 0^2)$	$3 \cdot 5_{-2}^L (T4^0)$	-2
$(\underline{+ + + - -}; + - -)$	$\overline{10}_{-1}^L (U_3)$	-1	$(\underline{-1, 0, 0, 0, 0}; \frac{-1}{3}, 0^2)$	$2 \cdot \overline{5}_2^L (T4^0)$	2
$(+ + + + +; + + +)$	$1_{-5}^L (U_3)$	-5	$(\underline{+ - - - -}; + 0 0)$	$2 \cdot 5_3^L (T6)$	4
$(\underline{-1, 0, 0, 0, 0}; -1, 0, 0)$	$\overline{5}_2^L (U_2)$	2	$(\underline{+ + + - -}; + 0 0)$	$4 \cdot \overline{10}_{-1}^L (T6)$	-2, -1
$(\underline{+ - - - -}; + - -)$	$5_3^L (U_1)$	3	$(+ + + + +; + 0 0)$	$2 \cdot 1_{-5}^L (T6)$	-6
$(\underline{+ + + - -}; + + +)$	$\overline{10}_{-1}^L (U_1)$	-1	$(\underline{+ + + + -}; - 0 0)$	$2 \cdot \overline{5}_{-3}^L (T6)$	-4
$(+ + + + +; + - -)$	$6_{-5}^L (U_1)$	-5	$(\underline{+ + - - -}; - 0 0)$	$3 \cdot 10_1^L (T6)$	2
$(\underline{+ - - - -}; \frac{-1}{6} 0 0)$	$5_3^L (T2^0)$	3	$(\underline{- - - - -}; - 0 0)$	$2 \cdot 1_5^L (T6)$	6
$(+ + + + +; \frac{-1}{6} 0 0)$	$1_{-5}^L (T2^0)$	-5			

We studied all Yukawa couplings up to  $D = 8$  superpotential terms and showed that we removed all exotics at GUT scale and obtain

$$U: (1_{-5} + 5_3 + \overline{10}_{-1})(U_1), (1_{-5} + 5_3 + \overline{10}_{-1})(U_3), (\overline{5}_2)(U_2)$$

$$T_6: \overline{10}_{-1}(T_6) \begin{array}{l} \swarrow t, b, e \\ \searrow \end{array} \begin{array}{l} \text{Inverted} \\ \text{relation for} \\ \text{leptons} \end{array}$$

$$T_2: 1_{-5} + 5_3(T_2)$$

$$T_4: 5_{-2}(T_4)$$

Higgs

Six gauged  $U(1)$  charges:

$$Z_1 = (2 \ 2 \ 2 \ 2 \ 2 ; 0^3) (0^8)'$$

$$Z_2 = (0^5 \quad ; 1 \ 0 \ 0) (0^8)'$$

$$Z_3 = (0^5 \quad ; 0 \ 1 \ 0) (0^8)'$$

$$Z_4 = (0^5 \quad ; 0 \ 0 \ 1) (0^8)'$$

$$Z_5 = (0^8) \quad (1 \ 1 ; 0 ; 0^5)'$$

$$Z_6 = (0^8) \quad (0 \ 0 ; 1 ; 0^5)'$$

$$Q_X = -Z_1, \quad Q_1 = Z_2 + 6Z_4, \quad Q_2 = -Z_2 + 6Z_4$$

$$Q_3 = Z_5, \quad Q_4 = 2Z_2 + 3Z_6$$

$$Q_{an} = -6Z_2 + Z_3 - Z_4 + 4Z_6$$

$$= (0 \ 0 \ 0 \ 0 \ 0 \ -6 \ 1 \ -1) (0 \ 0 \ 4 \ 0 \ 0 \ 0 \ 0 \ 0)$$

# IV Phenomenology

Except gauge interactions, phenomenology results from Yukawa couplings.

Yukawa couplings respect

① gauge symmetries

② in particular Lorentz symmetry  
⇒  $H$ -momentum conservation  
(from internal coordinates)

• Twisted sector fields must satisfy (modular invariance) : for  $T_k^{m_f}$

$$\sum_z k(z) = 0 \pmod{12}$$

$$\sum_z [k m_f](z) = 0 \pmod{3}$$

In  $\mathbb{Z}_3$ , the counterparts of these with gauge invariance are sufficient.



• Modular invariance require the sum of H-momenta

$$(-1, 1, 1) \bmod (12, 3, 12)$$

This condition restricts further!!!

Extensive discussion & Refs.

K.-S. Choi & JEK

"Quarks and Leptons from Orbifolded Superstring"

(Springer LNP696, 2006)

$Z_{12}$  :

$$U_1 (-1 \ 0 \ 0) \quad U_2 (0 \ 1 \ 0) \quad U_3 (0 \ 0 \ 1)$$

$$T_1 (-7/12 \ 4/12 \ 1/12) \quad T_3 (1/4 \ 0 \ -3/4) \quad T_7 (-1/12 \ 4/12 \ 7/12)$$

$$T_2 (-1/6 \ 4/6 \ 1/6) \quad T_4 (-1/3 \ 1/3 \ 1/3) \quad T_6 (-1/2 \ 0 \ 1/2)$$

$$T_2 T_4 T_6 = (-1, 1, 1)$$

From these rules, with gauge invariance, all Yukawa couplings can be calculated. Since there are  $O(100)$  chiral fields, computer search is necessary.

$$U: (1_{-5} + 5_3 + \overline{10}_{-1})(U_1), (1_{-5} + 5_3 + \overline{10}_{-1})(U_3), (\overline{5}_2)(U_2) \text{ Higgs}$$

$$T_6: \overline{10}_{-1}(T_6) \downarrow t, b, e \left\{ \begin{array}{l} \text{Inverted} \\ \text{relation for} \\ \text{leptons} \end{array} \right.$$

$$T_2: 1_{-5} + 5_3(T_2)$$

$$T_4: 5_{-2}(T_4) \text{ Higgs}$$

$$\overline{10}_{-1}(T_6) \cdot 5_3(T_2) \cdot \langle 5_{-2}(T_4) \rangle \text{ top mass}$$

If neutral singlets are allowed to get GUT scale VEVs, then all needed phenomenology can be obtained.

$K + Kyae$

th/0608086

Choi + JEK + I.W. Kim

ph/0612107

I.W. Kim + JEK + Kyae

ph/0612365

axion study

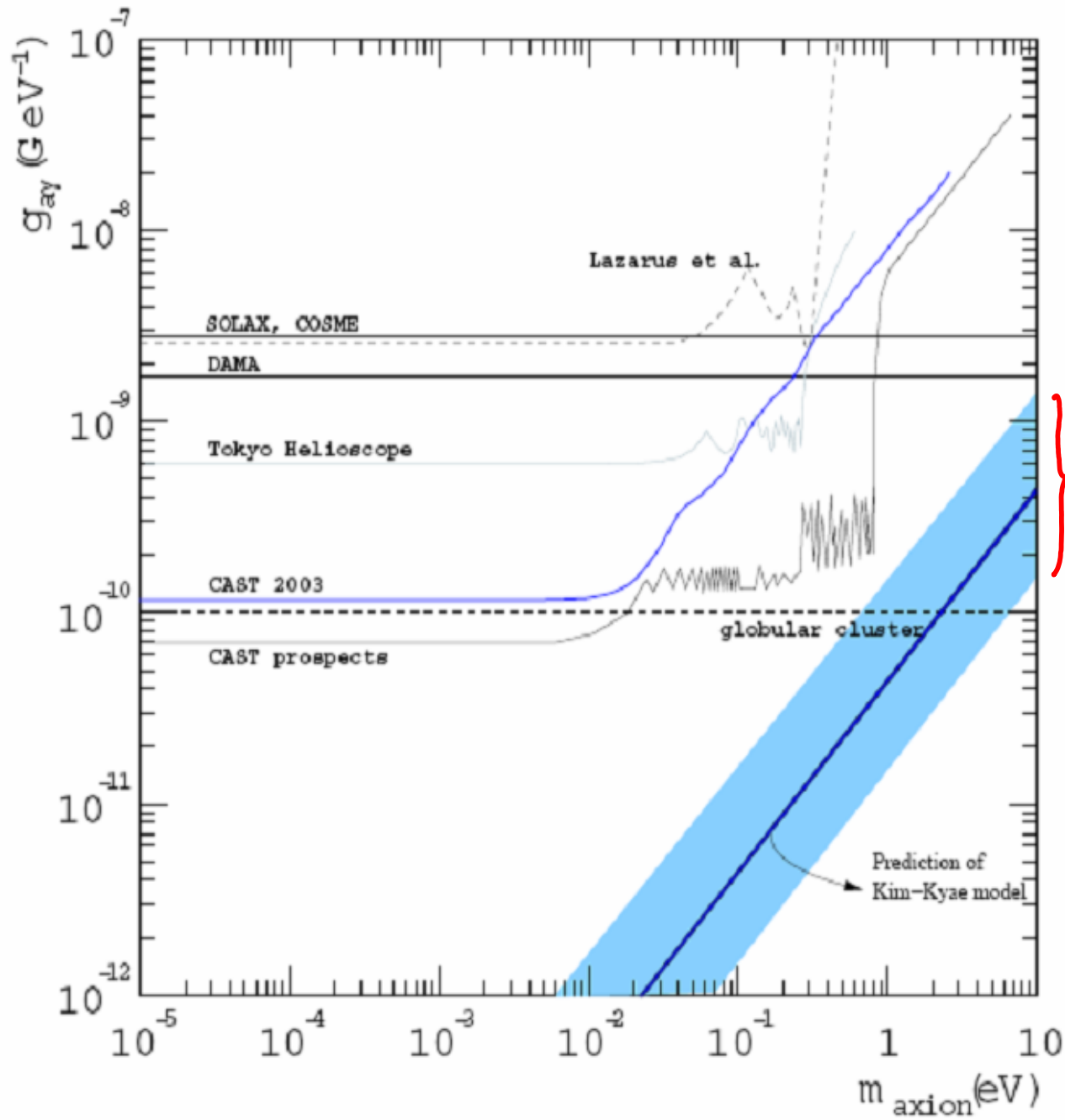
R-parity study

PQ symmetries :  $U(1)_{an} \otimes U(1)_{global}$ , approx

We find that QCD axion is possible but the decay constant at  $M_{GUT}$  Calculated  $C_{axx}$  for the first time in string

$$C_{axx} = \bar{C}_{axx} - 1.93 \approx -0.26$$

↑  
chiral symm. breaking contribution



± 20% th  
 error;  
 two loop,  
 $m_u \neq 0$   
 with inst.  
 contr.

This kind of study must be performed in a specific model. In the community, there are papers just looking at piecemeal phenomenon, which is not warranted in string phenomenology.

For example, one may consider R-sym. toward PQ symmetry. It is at best a SUGRA strategy since strings do not allow any global symmetry. It must be approximate except  $U(1)_{anom.}$

In the same vein, R-parity must be studied in a specific model. We know that there are many singlets

⇒ Many of them need GUT scale VEVs.

⇒ This fact must be taken into account.

## SUSY R PARITY

S: spinor, V: vector  
SO(10)

S	S	V	matter	in	$16_F$
-1	-1	1	Higgs	in	$10_H$

But  $SSV(111\dots)$  allowed in string, and fails for an exact R-parity in general

# U(1) SYMMETRIES

Flipped  $SU(5)$  gauged  $U(1)_X$

$$X = (-2 \ -2 \ -2 \ -2 \ -2 \ 0 \ 0 \ 0) (0^8)'$$

Untwisted matter:

$$\text{spinor} : (\pm \frac{1}{2} \ \pm \frac{1}{2} \ \pm \frac{1}{2} \ \pm \frac{1}{2} \ \pm \frac{1}{2} \ \pm \frac{1}{2} \ \pm \frac{1}{2} \ \pm \frac{1}{2})$$

$$X = \pm 1, \pm 3, \pm 5$$

$$\text{vector} : (\pm 1 \ 0 \ 0 \ 0 \ 0 \ 0 \ \pm 1 \ 0 \ 0)$$

$$(\pm 1 \ \pm 1 \ 0 \ 0 \ 0 \ 0 \ 0 \ 0 \ 0), \text{etc}$$

$$X = \pm 2, \pm 4, 0, \dots$$



If  $U(1)_X$  is broken by  $\langle V(X=2) \rangle$ ,

then

$$\begin{array}{l} U(1)_X \longrightarrow Z_2 \\ \left. \begin{array}{l} \text{vectors : } Z_2 \text{ even} \\ \text{spinors : } Z_2 \text{ odd} \end{array} \right\} \begin{array}{l} \text{perfect} \\ R \text{ parity} \end{array} \end{array}$$

But, it must be discussed in a specific model such that all SM matter fermions are in spinor, and all Higgs are in vector, including singlets.

For a successful R parity, one must succeed in Yukawa couplings. The argument of the preceding paragraph is just an idea. It must be realized in a specific model.

So far, we have not found any model. Maybe in the future?

⇒ LSP is **not likely** to exist.

# V. Harmless R-parity Violation

In our  $Z_{12}$ -I model, we removed all exotics, vectorlike pairs by VEVs of singlets. These singlets belong to  $V$  and  $S$  types. So R-parity is violated. Note all SM matter appears in the  $S$  type representation, but some needed singlets also belong to  $S$ -type.

$D = 4 :$

$$[d^c d^c u^c]_F, [q d^c l]_F \Leftarrow \langle \overline{\mathbf{10}}^H \rangle \overline{\mathbf{10}} \overline{\mathbf{10}} \mathbf{5}, \quad (8)$$

and

$D = 5 :$

$$O_1 = [qqql]_F \Leftarrow \overline{\mathbf{10}} \overline{\mathbf{10}} \overline{\mathbf{10}} \mathbf{5},$$

$$O_2 = [u^c u^c d^c e^+]_F \Leftarrow \mathbf{5} \mathbf{5} \overline{\mathbf{10}} \mathbf{1}$$

$$O_3 = [qqqH_d]_F \Leftarrow \langle \mathbf{10}^H \rangle \overline{\mathbf{10}} \overline{\mathbf{10}} \overline{\mathbf{10}} \overline{\mathbf{5}}_2,$$

$$O_4 = [qu^c e^+ H_d]_F \Leftarrow \langle \mathbf{10}^H \rangle \overline{\mathbf{10}} \mathbf{5} \mathbf{1} \overline{\mathbf{5}}_2$$

$$O_5 = [lH_u H_u]_F \Leftarrow \langle \overline{\mathbf{10}}^H \rangle \langle \overline{\mathbf{10}}^H \rangle \mathbf{5} \mathbf{5} \mathbf{5}_{-2} \mathbf{5}_{-2}, \quad O_6 = [lH_d H_u H_u]_F \Leftarrow \langle \overline{\mathbf{10}}^H \rangle \mathbf{5} \overline{\mathbf{5}}_2 \mathbf{5}_{-2} \mathbf{5}_{-2}$$

These terms appear at high orders.

$D=5$  terms are not problematic:  $\mathcal{O}(10^{-7})$ .

$D=4$  terms multiplied together gives proton decay operator.  $\mathcal{O}(10^{-26})$

$\Rightarrow$  individual terms  $\mathcal{O}(10^{-13})$ .

$5_3$	$\overline{10}_{-1}$	$\overline{10}_{-1}$	$\overline{10}_{-1}$	$H$ -mom.	$N$	$5_3$	$\overline{10}_{-1}$	$\overline{10}_{-1}$	$\overline{10}_{-1}$	$H$ -mom.	$N$
$U_1$	$U_1$	$U_1$	$T6$	$(\frac{-7}{2}, 0, \frac{1}{2})$	11	$U_3$	$U_3$	$U_3$	$T6$	$(\frac{-1}{2}, 0, \frac{7}{2})$	11
$U_1$	$U_1$	$U_3$	$T6$	$(\frac{-5}{2}, 0, \frac{3}{2})$	11	$U_3$	$U_3$	$T6$	$T6$	$(-1, 0, 3)$	12
$U_1$	$U_1$	$T6$	$T6$	$(-3, 0, 1)$	12	$U_3$	$T6$	$T6$	$T6$	$(\frac{-3}{2}, 0, \frac{5}{2})$	11
$U_1$	$U_3$	$U_3$	$T6$	$(\frac{-3}{2}, 0, \frac{5}{2})$	11	$T2$	$U_1$	$U_1$	$T6$	$(\frac{-8}{3}, \frac{2}{3}, \frac{2}{3})$	10
$U_1$	$U_3$	$T6$	$T6$	$(-2, 0, 2)$	12	$T2$	$U_1$	$U_3$	$T6$	$(\frac{-5}{3}, \frac{2}{3}, \frac{5}{3})$	10
$U_1$	$T6$	$T6$	$T6$	$(\frac{-5}{2}, 0, \frac{3}{2})$	11	$T2$	$U_1$	$T6$	$T6$	$(\frac{-13}{6}, \frac{2}{3}, \frac{7}{6})$	11
$U_3$	$U_1$	$U_1$	$T6$	$(-\frac{5}{2}, 0, \frac{3}{2})$	11	$T2$	$U_3$	$U_3$	$T6$	$(\frac{-2}{3}, \frac{2}{3}, \frac{8}{3})$	10
$U_3$	$U_1$	$U_3$	$T6$	$(\frac{-3}{2}, 0, \frac{5}{2})$	11	$T2$	$U_3$	$T6$	$T6$	$(\frac{-7}{6}, \frac{2}{3}, \frac{13}{6})$	11
$U_3$	$U_1$	$T6$	$T6$	$(-2, 0, 2)$	12	$T2$	$T6$	$T6$	$T6$	$(\frac{-5}{3}, \frac{2}{3}, \frac{5}{3})$	10

$5_3$	$5_3$	$\overline{10}_{-1}$	$1_{-5}$	$H$ -mom.	$N$	$5_3$	$5_3$	$\overline{10}_{-1}$	$1_{-5}$	$H$ -mom.	$N$	$5_3$	$5_3$	$\overline{10}_{-1}$	$1_{-5}$	$H$ -mom.	$N$
$U_1$	$U_1$	$U_1$	$U_1$	$(-4, 0, 0)$	12	$U_1$	$T2$	$U_1$	$U_1$	$(\frac{-19}{6}, \frac{2}{3}, \frac{1}{6})$	11	$U_3$	$T2$	$U_1$	$U_1$	$(\frac{-13}{6}, \frac{2}{3}, \frac{7}{6})$	11
$U_1$	$U_1$	$U_1$	$U_3$	$(-3, 0, 1)$	12	$U_1$	$T2$	$U_1$	$U_3$	$(\frac{-13}{6}, \frac{2}{3}, \frac{7}{6})$	11	$U_3$	$T2$	$U_1$	$U_3$	$(\frac{-7}{6}, \frac{2}{3}, \frac{13}{6})$	11
$U_1$	$U_1$	$U_1$	$T2$	$(\frac{-19}{6}, \frac{2}{3}, \frac{1}{6})$	11	$U_1$	$T2$	$U_1$	$T2$	$(\frac{-7}{3}, \frac{4}{3}, \frac{1}{3})$	10	$U_3$	$T2$	$U_1$	$T2$	$(\frac{-4}{3}, \frac{4}{3}, \frac{4}{3})$	10
$U_1$	$U_1$	$U_3$	$U_1$	$(-3, 0, 1)$	12	$U_1$	$T2$	$U_3$	$U_1$	$(\frac{-13}{6}, \frac{2}{3}, \frac{7}{6})$	11	$U_3$	$T2$	$U_3$	$U_1$	$(\frac{-7}{6}, \frac{2}{3}, \frac{13}{6})$	11
$U_1$	$U_1$	$U_3$	$U_3$	$(-2, 0, 2)$	12	$U_1$	$T2$	$U_3$	$U_3$	$(\frac{-7}{6}, \frac{2}{3}, \frac{13}{6})$	11	$U_3$	$T2$	$U_3$	$U_3$	$(\frac{-1}{6}, \frac{2}{3}, \frac{19}{6})$	11
$U_1$	$U_1$	$U_3$	$T2$	$(\frac{-13}{6}, \frac{2}{3}, \frac{7}{6})$	11	$U_1$	$T2$	$U_3$	$T2$	$(\frac{-4}{3}, \frac{4}{3}, \frac{4}{3})$	10	$U_3$	$T2$	$U_3$	$T2$	$(\frac{-1}{3}, \frac{4}{3}, \frac{7}{3})$	10
$U_1$	$U_1$	$T6$	$U_1$	$(\frac{-7}{2}, 0, \frac{1}{2})$	11	$U_1$	$T2$	$T6$	$U_1$	$(\frac{-8}{3}, \frac{2}{3}, \frac{2}{3})$	10	$U_3$	$T2$	$T6$	$U_1$	$(\frac{-5}{3}, \frac{2}{3}, \frac{5}{3})$	10
$U_1$	$U_1$	$T6$	$U_3$	$(\frac{-5}{2}, 0, \frac{3}{2})$	11	$U_1$	$T2$	$T6$	$U_3$	$(\frac{-5}{3}, \frac{2}{3}, \frac{5}{3})$	10	$U_3$	$T2$	$T6$	$U_3$	$(\frac{-2}{3}, \frac{2}{3}, \frac{8}{3})$	10
$U_1$	$U_1$	$T6$	$T2$	$(\frac{-8}{3}, \frac{2}{3}, \frac{2}{3})$	10	$U_1$	$T2$	$T6$	$T2$	$(\frac{-11}{6}, \frac{4}{3}, \frac{5}{6})$	9	$U_3$	$T2$	$T6$	$T2$	$(\frac{-5}{6}, \frac{4}{3}, \frac{11}{6})$	9
$U_1$	$U_3$	$U_1$	$U_1$	$(-3, 0, 1)$	12	$U_3$	$U_3$	$U_1$	$U_1$	$(-2, 0, 2)$	12	$T2$	$T2$	$U_1$	$U_1$	$(\frac{-7}{3}, \frac{4}{3}, \frac{1}{3})$	10
$U_1$	$U_3$	$U_1$	$U_3$	$(-2, 0, 2)$	12	$U_3$	$U_3$	$U_1$	$U_3$	$(-1, 0, 3)$	12	$T2$	$T2$	$U_1$	$U_3$	$(\frac{-4}{3}, \frac{4}{3}, \frac{4}{3})$	10
$U_1$	$U_3$	$U_1$	$T2$	$(\frac{-13}{6}, \frac{2}{3}, \frac{7}{6})$	11	$U_3$	$U_3$	$U_1$	$T2$	$(\frac{-7}{6}, \frac{2}{3}, \frac{13}{6})$	11	$T2$	$T2$	$U_1$	$T2$	$(\frac{-3}{2}, 2, \frac{1}{2})$	9
$U_1$	$U_3$	$U_3$	$U_1$	$(-2, 0, 2)$	12	$U_3$	$U_3$	$U_3$	$U_1$	$(-1, 0, 3)$	12	$T2$	$T2$	$U_3$	$U_1$	$(\frac{-4}{3}, \frac{4}{3}, \frac{4}{3})$	10
$U_1$	$U_3$	$U_3$	$U_3$	$(-1, 0, 3)$	12	$U_3$	$U_3$	$U_3$	$U_3$	$(0, 0, 4)$	12	$T2$	$T2$	$U_3$	$U_3$	$(\frac{-1}{3}, \frac{4}{3}, \frac{7}{3})$	10
$U_1$	$U_3$	$U_3$	$T2$	$(\frac{-7}{6}, \frac{2}{3}, \frac{13}{6})$	11	$U_3$	$U_3$	$U_3$	$T2$	$(\frac{-1}{6}, \frac{2}{3}, \frac{19}{6})$	11	$T2$	$T2$	$U_3$	$T2$	$(\frac{-1}{2}, 2, \frac{3}{2})$	9
$U_1$	$U_3$	$T6$	$U_1$	$(\frac{-5}{2}, 0, \frac{3}{2})$	11	$U_3$	$U_3$	$T6$	$U_1$	$(\frac{-3}{2}, 0, \frac{5}{2})$	11	$T2$	$T2$	$T6$	$U_1$	$(\frac{-11}{6}, \frac{4}{3}, \frac{5}{6})$	9
$U_1$	$U_3$	$T6$	$U_3$	$(\frac{-3}{2}, 0, \frac{5}{2})$	11	$U_3$	$U_3$	$T6$	$U_3$	$(\frac{-1}{2}, 0, \frac{7}{2})$	11	$T2$	$T2$	$T6$	$U_3$	$(\frac{-5}{6}, \frac{4}{3}, \frac{11}{6})$	9
$U_1$	$U_3$	$T6$	$T2$	$(\frac{-5}{3}, \frac{2}{3}, \frac{5}{3})$	10	$U_3$	$U_3$	$T6$	$T2$	$(\frac{-2}{3}, \frac{2}{3}, \frac{8}{3})$	10	$T2$	$T2$	$T6$	$T2$	$(-1, 2, 1)$	8

Product of these two operators would give proton decay.

With singlet VEVs of order

$$\frac{\langle S \rangle}{M_s} \sim \frac{1}{10} \sim \frac{1}{100}$$

proton can be made sufficiently long lived.

# CONCLUSION

We constructed a realistic string derived SSM from  $Z_{12-I}$  orb. comp. (through flipped  $SU(5)$ )

- ① Exotics removed by singlet VEVs
- ② 3 SM  $q, l$
- ③ Vectorlike pairs → removed, except of light Higgs
- ④  $C_{arr} = -0.26$ , but  $F_a \sim 10^{16}$  GeV
- ⑤ Harmless R-parity