



« Electroweak Breaking After First Three Years at the LHC »

## *Aspects of Higgs rate fits*

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Based on [arXiv:1210.3977](https://arxiv.org/abs/1210.3977) (will be updated tuesday)

& Work in progress with ***A. Djouadi***

## Outline

### A - Focusing on new fermions

- I) The Higgs fits with Extra-Fermions*
- II) Constraining single Extra-Fermions*

### B – The interests of rate ratios

- I) Get rid of the theoretical uncertainty*
- II) Fitting ratios of signal strengths*

# A - Focusing on new fermions

## *I) The Higgs fits with Extra-Fermions*

Today : The LHC has **discovered** a resonance of  $\sim 125.5$  GeV

➔ *it is probably the B.E.Higgs boson => **EWSB** mechanism*

+ Tevatron and LHC provide **58** measurements of the Higgs rates

= new precious source of indirect information on BSM physics

➔ *nature of the EWSB : within the **SM** or a **BSM** context !?*

On the theoretical side:

**New fermions** arise in most (all?) of the SM extensions,

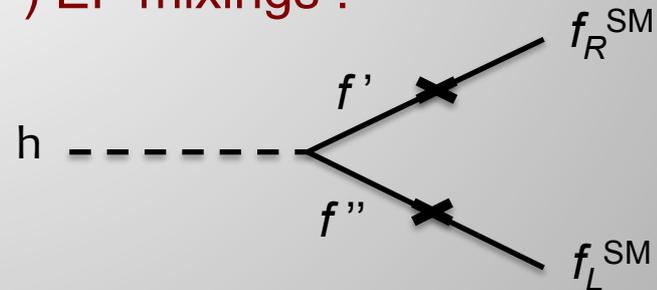
- little Higgs *[fermionic partners]*
- supersymmetry *[gauginos / higgsinos]*
- composite Higgs *[excited bounded states]*
- extra-dimensions *[Kaluza-Klein towers]*
- 4<sup>th</sup> generations *[new families]*
- GUT *[multiplet components]*
- etc...

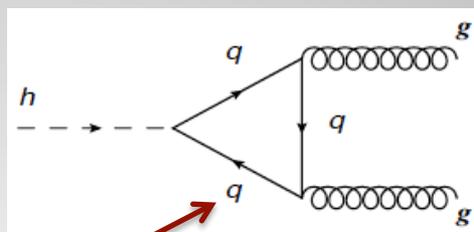
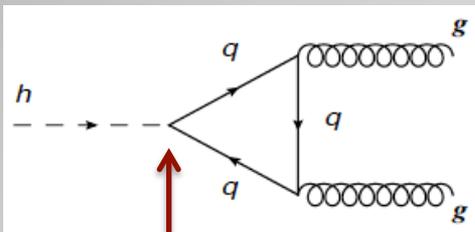
➔ *What are the present **constraints on extra-fermions** from all the experimental Higgs boson results ?*

Effective approach : Corrections on the Higgs couplings  
from **any** extra-fermions (*via mixing, new loops*)

$$\mathcal{L}_h = -c_t Y_t h \bar{t}_L t_R - c_b Y_b h \bar{b}_L b_R - c_\tau Y_\tau h \bar{\tau}_L \tau_R \\ + C_{h\gamma\gamma} \frac{\alpha}{\pi v} h F^{\mu\nu} F_{\mu\nu} + C_{hgg} \frac{\alpha_s}{12\pi v} h G^{a\mu\nu} G_{\mu\nu}^a + \text{h.c.}$$

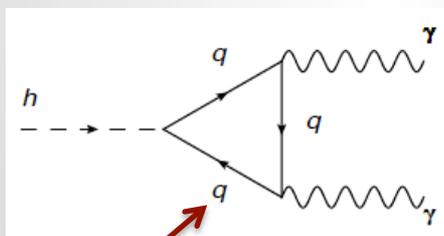
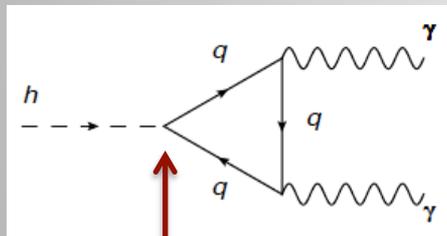
Modifications of  $Y_f$  Yukawa couplings via ( $f'$ ) EF mixings :



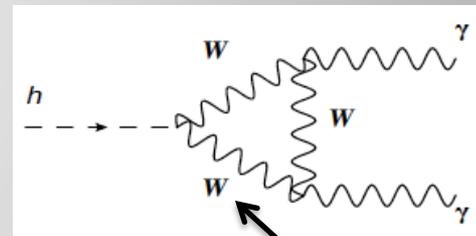


$b', q_{5/3}, \dots$

$$C_{hgg} = 2C(t) A[\tau(m_t)] (c_t + c_{gg}) + 2C(b) A[\tau(m_b)] c_b + 2C(c) A[\tau(m_c)]$$



$b', q_{5/3}, \dots$



$$C_{h\gamma\gamma} = \frac{N_c^t}{6} Q_t^2 A[\tau(m_t)] (c_t + c_{\gamma\gamma}) + \frac{N_c^b}{6} Q_b^2 A[\tau(m_b)] c_b + \frac{N_c^c}{6} Q_c^2 A[\tau(m_c)] + \frac{N_c^\tau}{6} Q_\tau^2 A[\tau(m_\tau)] c_\tau + \frac{1}{8} A_1[\tau(m_W)]$$

Higgs production cross sections over their SM expectations :

$$\frac{\sigma_{gg \rightarrow h}}{\sigma_{gg \rightarrow h}^{\text{SM}}} \simeq \frac{|(c_t + c_{gg})A[\tau(m_t)] + c_b A[\tau(m_b)] + A[\tau(m_c)]|^2}{|A[\tau(m_t)] + A[\tau(m_b)] + A[\tau(m_c)]|^2} \quad \frac{\sigma_{h\bar{t}t}}{\sigma_{h\bar{t}t}^{\text{SM}}} \simeq |c_t|^2$$

Higgs partial decay widths over the SM predictions (no new channels) :

$$\frac{\Gamma_{h \rightarrow \gamma\gamma}}{\Gamma_{h \rightarrow \gamma\gamma}^{\text{SM}}} \simeq \frac{|\frac{1}{4}A_1[\tau(m_W)] + (\frac{2}{3})^2(c_t + c_{\gamma\gamma})A[\tau(m_t)] + (-\frac{1}{3})^2c_b A[\tau(m_b)] + (\frac{2}{3})^2A[\tau(m_c)] + \frac{1}{3}c_\tau A[\tau(m_\tau)]|^2}{|\frac{1}{4}A_1[\tau(m_W)] + (\frac{2}{3})^2A[\tau(m_t)] + (-\frac{1}{3})^2A[\tau(m_b)] + (\frac{2}{3})^2A[\tau(m_c)] + \frac{1}{3}A[\tau(m_\tau)]|^2}$$

$$\frac{\Gamma_{h \rightarrow \bar{b}b}}{\Gamma_{h \rightarrow \bar{b}b}^{\text{SM}}} \simeq |c_b|^2$$

$$\frac{\Gamma_{h \rightarrow \bar{\tau}\tau}}{\Gamma_{h \rightarrow \bar{\tau}\tau}^{\text{SM}}} \simeq |c_\tau|^2$$

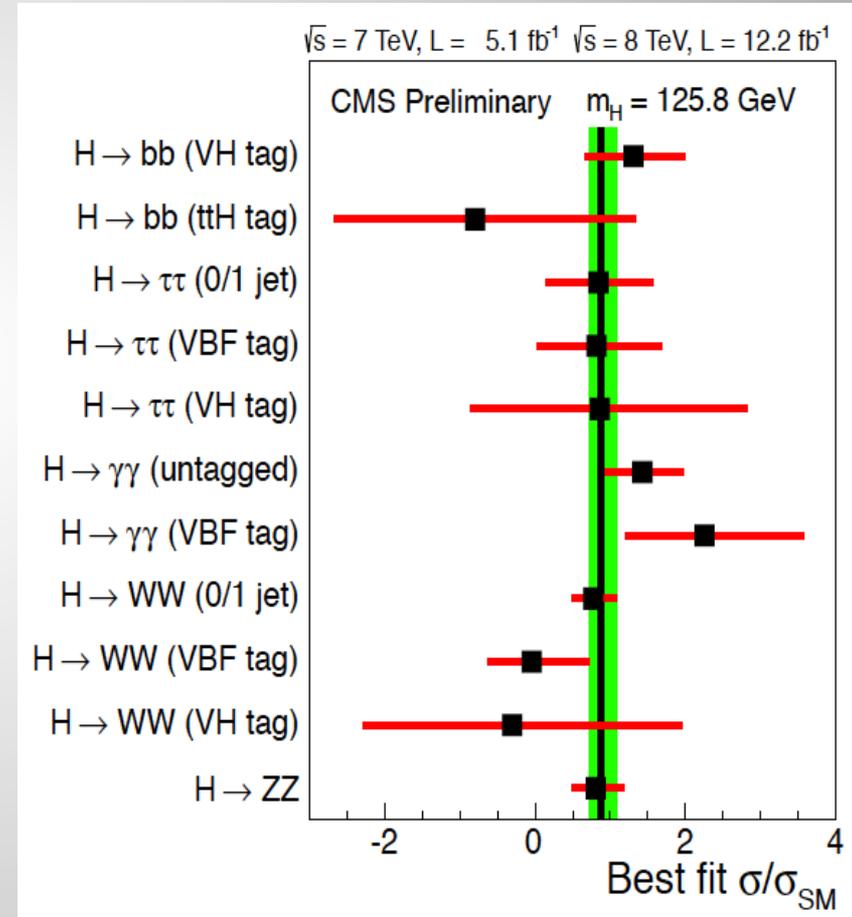
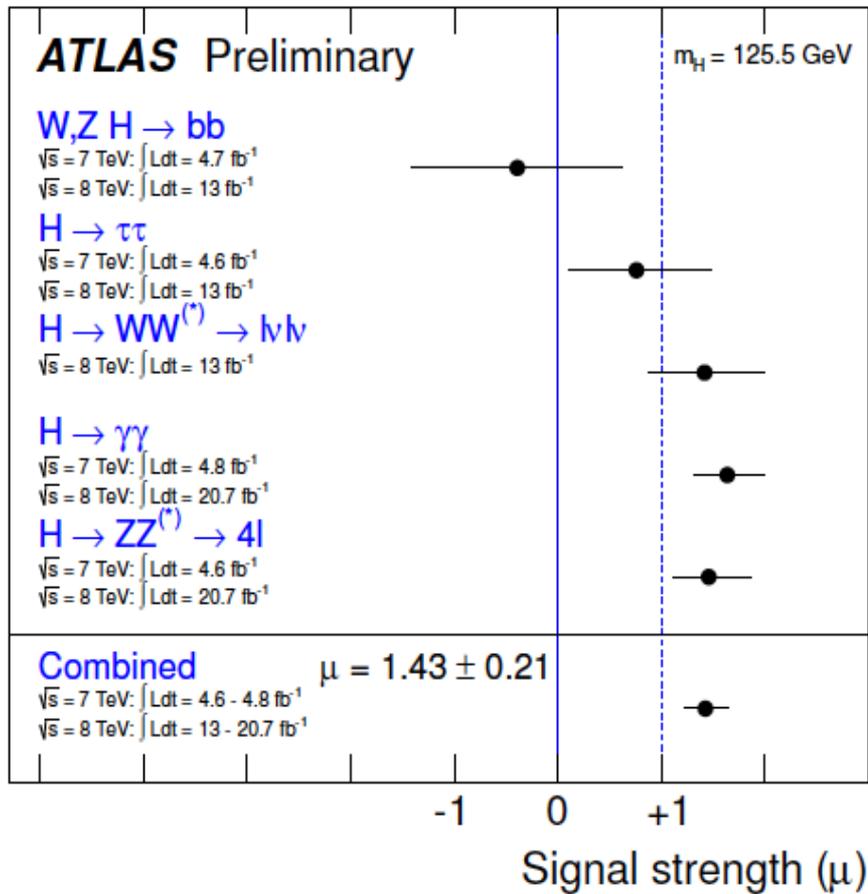
Measured signal strengths all of the form (exp. selection efficiencies) :

$$\mu_{s,c,i}^p \simeq \frac{\sigma_{gg \rightarrow h|s} + \frac{\epsilon_{hqq}}{\epsilon_{gg \rightarrow h}} \Big|_{s,c,i}^p \sigma_{hqq}^{\text{SM}}|_s + \frac{\epsilon_{hV}}{\epsilon_{gg \rightarrow h}} \Big|_{s,c,i}^p \sigma_{hV}^{\text{SM}}|_s + \frac{\epsilon_{h\bar{t}t}}{\epsilon_{gg \rightarrow h}} \Big|_{s,c,i}^p \sigma_{h\bar{t}t}|_s}{\sigma_{gg \rightarrow h}^{\text{SM}}|_s + \frac{\epsilon_{hqq}}{\epsilon_{gg \rightarrow h}} \Big|_{s,c,i}^p \sigma_{hqq}^{\text{SM}}|_s + \frac{\epsilon_{hV}}{\epsilon_{gg \rightarrow h}} \Big|_{s,c,i}^p \sigma_{hV}^{\text{SM}}|_s + \frac{\epsilon_{h\bar{t}t}}{\epsilon_{gg \rightarrow h}} \Big|_{s,c,i}^p \sigma_{h\bar{t}t}^{\text{SM}}|_s} \frac{B_{h \rightarrow \text{XX}}}{B_{h \rightarrow \text{XX}}^{\text{SM}}}$$

For the fit analysis, we define a function  $\chi^2(c_t, c_b, c_\tau, c_{gg}, c_{\gamma\gamma})$  :

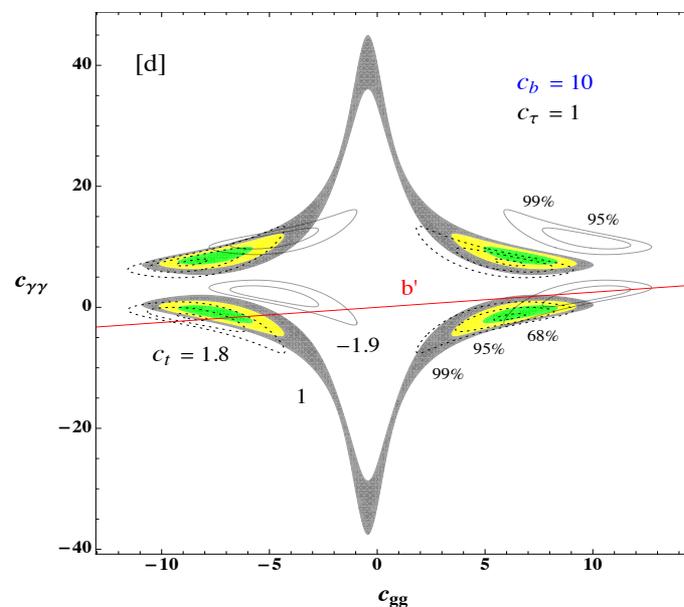
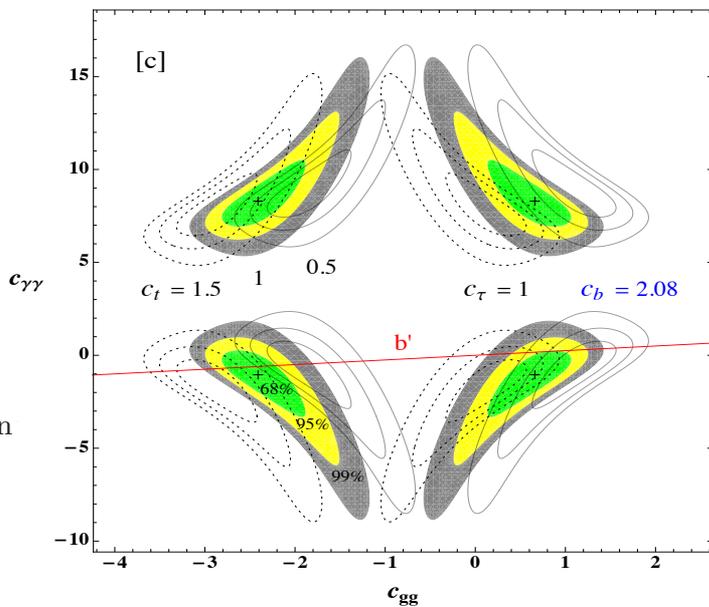
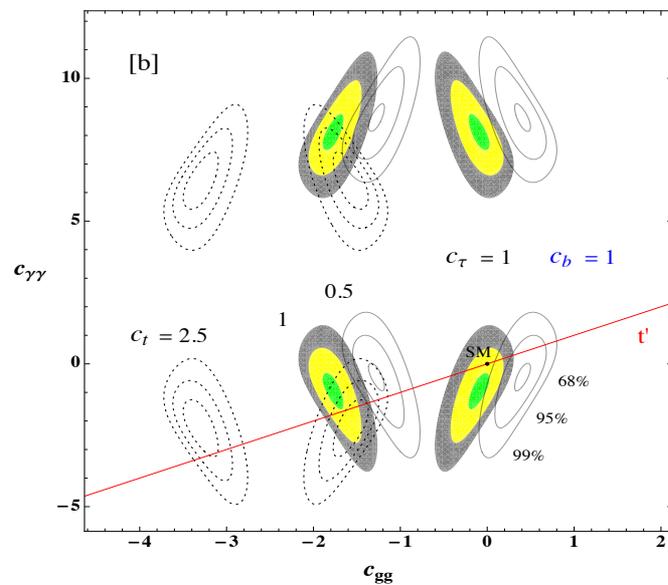
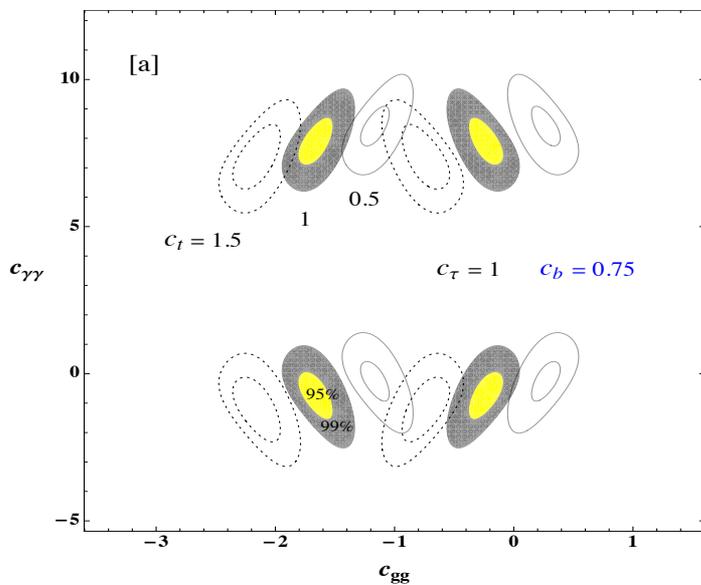
$$\chi^2 = \sum_{p,s,c,i} \frac{(\mu_{s,c,i}^p - \mu_{s,c,i}^p|_{\text{exp}})^2}{(\delta\mu_{s,c,i}^p)^2}$$

# Taking the latest experimental results...



# Higgs fit results :

( 3 free param.)



$$\Delta\chi^2 = \chi^2 - \chi_{\min}^2$$

$$\chi_{\min}^2 = 52.36$$

## « 3 conclusions for this first fit... »

- \* The SM point (  $\chi_{\text{SM}}^2 = 57.10$  ) does not belong to the  $1\sigma$  region
- \* Determination of  $c_{gg}$  and  $c_{\gamma\gamma}$  **relies** on the knowledge of  $Y_t^{\text{EF}}$  (  $c_t$  )
- \*  $Y_b^{\text{EF}}$  (  $c_b$  )  $\nearrow$   $B(h \rightarrow VV)$   $\searrow$  compensated by  $\sigma_{gg \rightarrow h}$   $\nearrow$  i.e.  $c_{gg}$   $\nearrow$

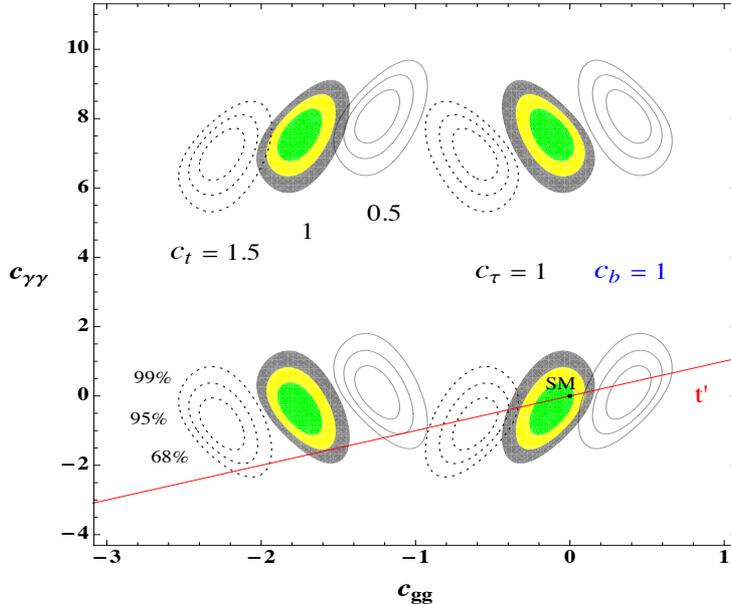
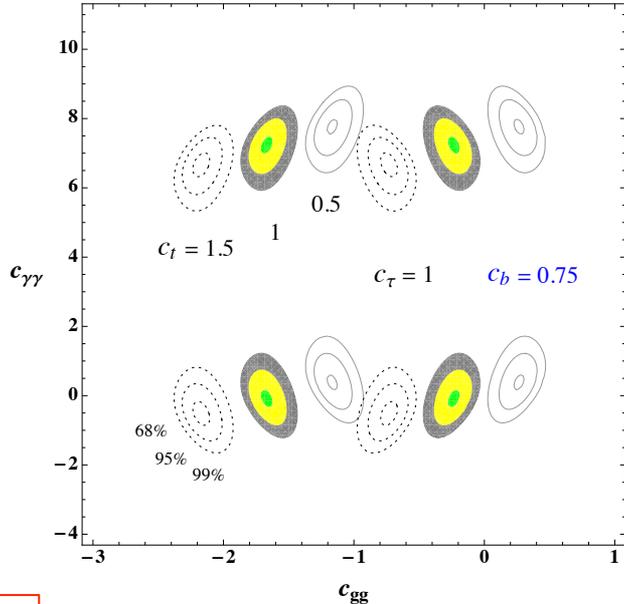
**$\Rightarrow Y_b$  cannot be determined by the (previous) Higgs fit**

*suggestion : avoid compensations by measuring*

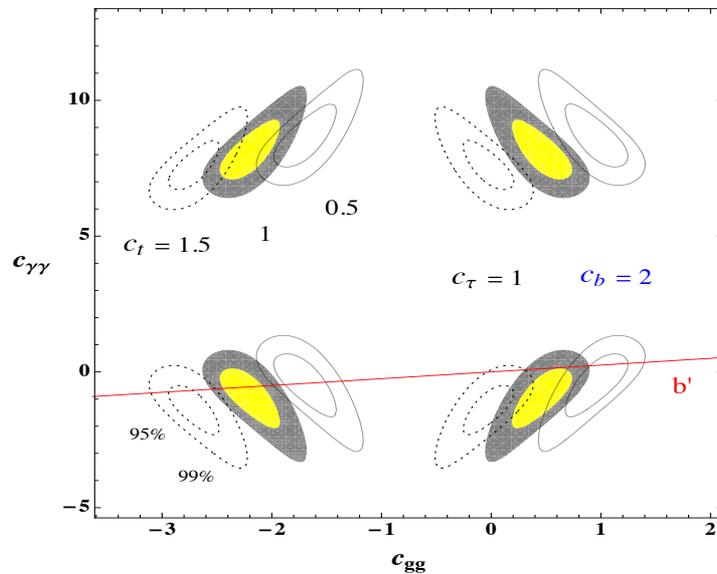
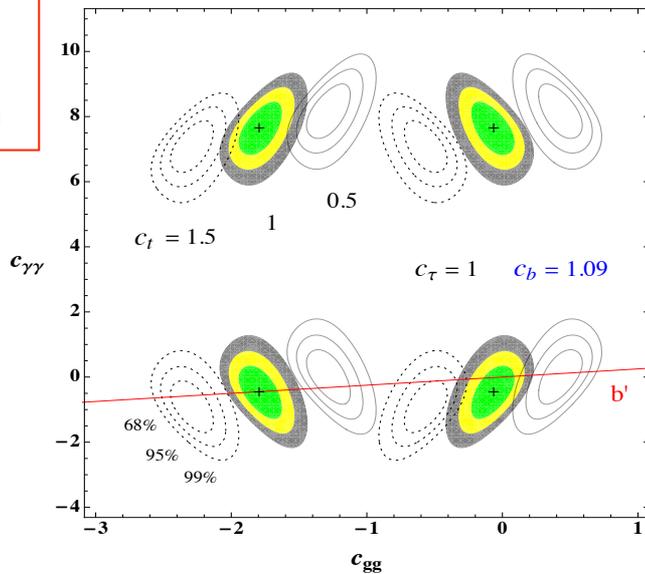
$$\bar{q}q \rightarrow h\bar{b}b \text{ and } gg \rightarrow h\bar{b}b \quad h \rightarrow \bar{b}b$$

# Higgs fit results :

( 3 free param.)



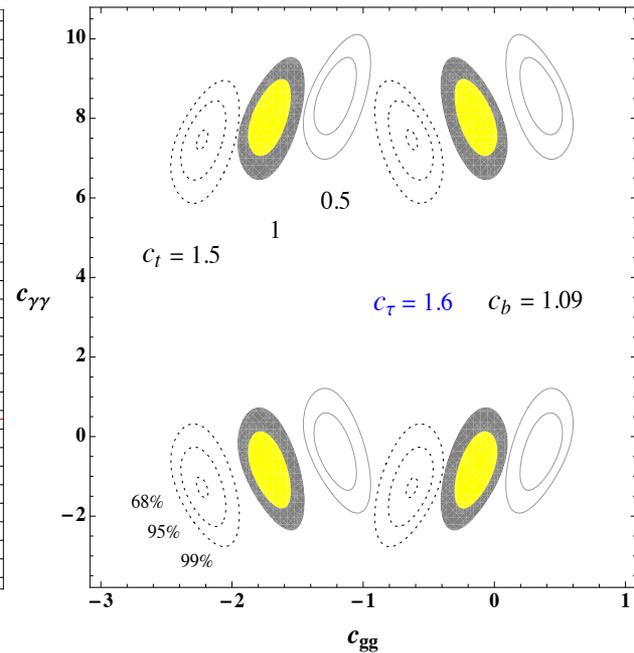
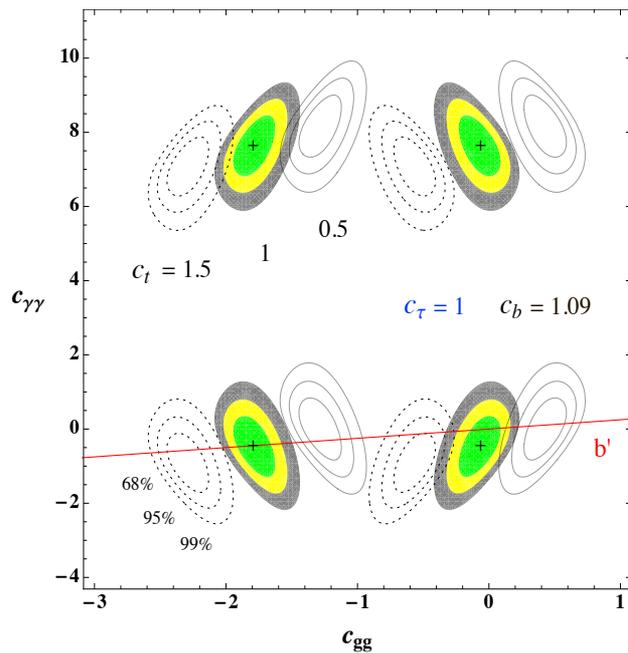
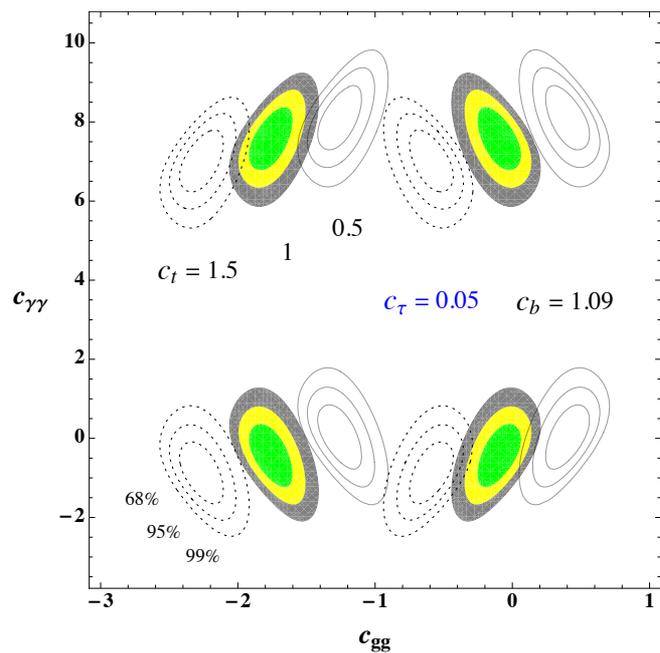
**AFTER MORIOND...**



$$\Delta\chi^2 = \chi^2 - \chi_{\min}^2$$

$$\chi_{\min}^2 = 52.36$$

Varying the last parameter :  $C_T$



## II) Constraining single Extra-Fermions

Single extra-fermion (starting approximation) => new loop-contributions :

$$c_{gg} = \frac{1}{C(t)A[\tau(m_t)]/v} \left[ -C(t') \frac{Y_{t'}}{m_{t'}} A[\tau(m_{t'})] - C(q_{5/3}) \frac{Y_{q_{5/3}}}{m_{q_{5/3}}} A[\tau(m_{q_{5/3}})] + \dots \right]$$

$$c_{\gamma\gamma} = \frac{1}{N_c^t Q_t^2 A[\tau(m_t)]/v} \left[ -3 \left(\frac{2}{3}\right)^2 \frac{Y_{t'}}{m_{t'}} A[\tau(m_{t'})] - N_c^{q_{5/3}} \left(\frac{5}{3}\right)^2 \frac{Y_{q_{5/3}}}{m_{q_{5/3}}} A[\tau(m_{q_{5/3}})] - Q_{\ell'}^2 \frac{Y_{\ell'}}{m_{\ell'}} A[\tau(m_{\ell'})] + \dots \right]$$

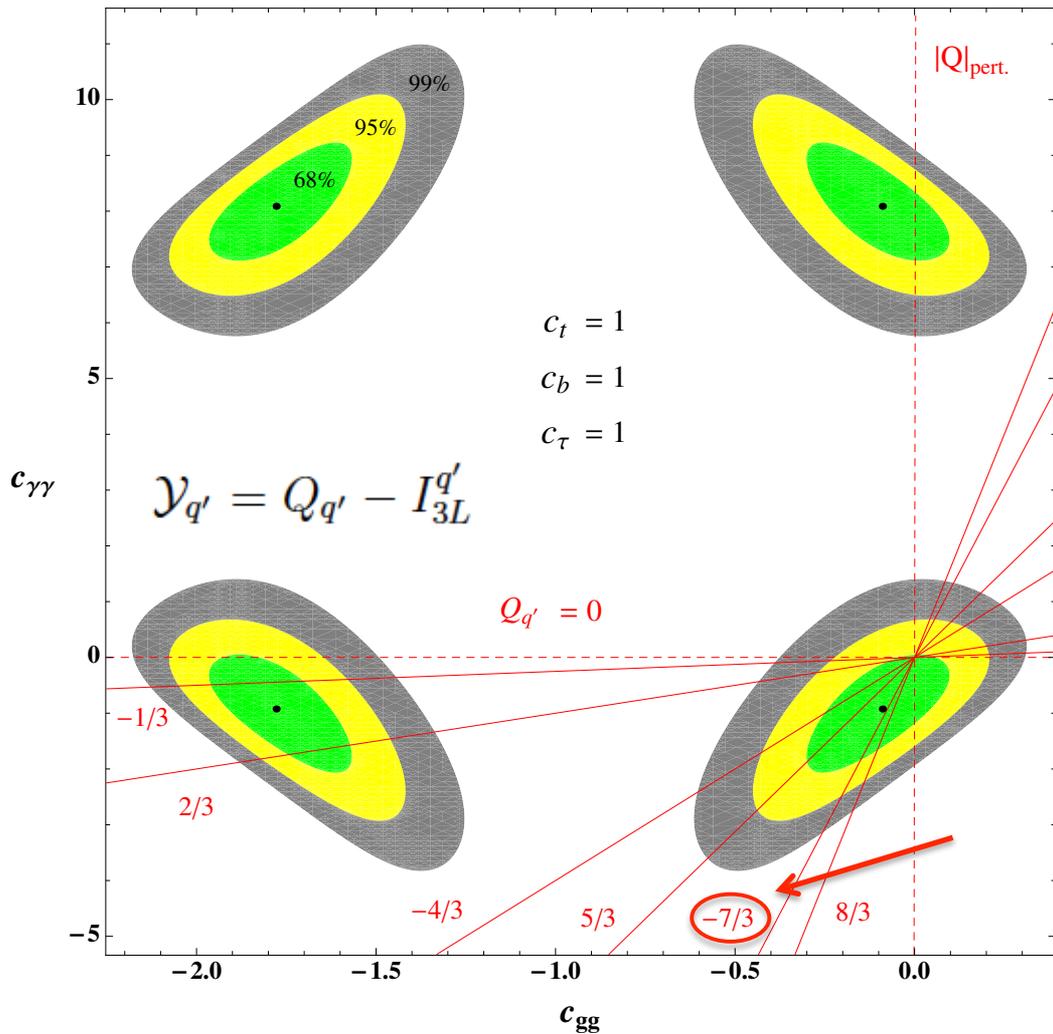
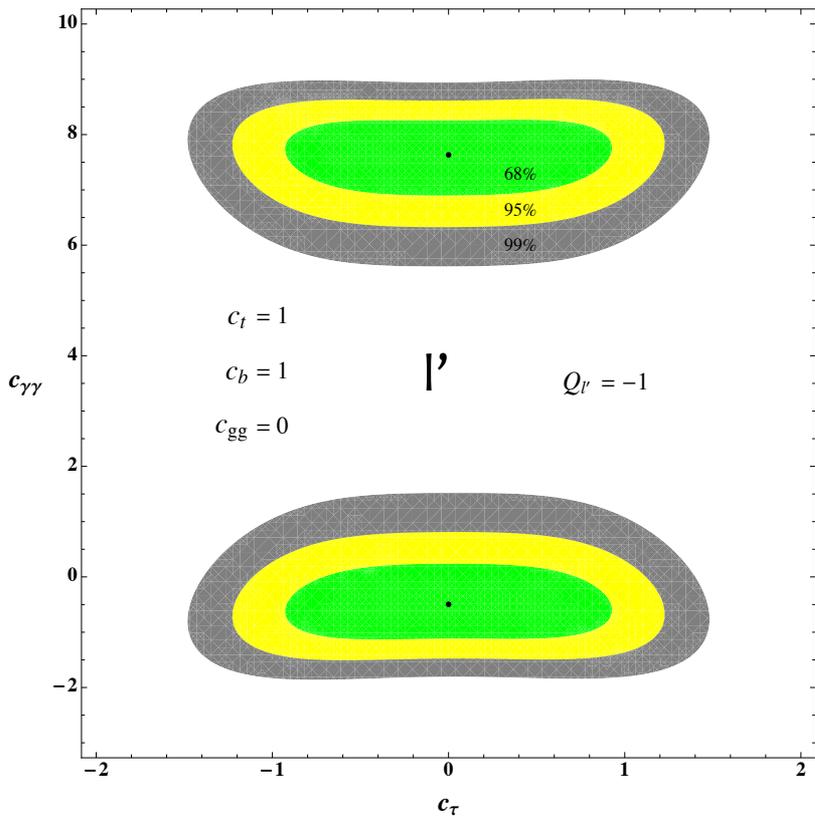


$$\frac{c_{\gamma\gamma}}{c_{gg}} \Big|_{q'} = \frac{Q_{q'}^2}{(2/3)^2}$$

(same color repres. as the top)

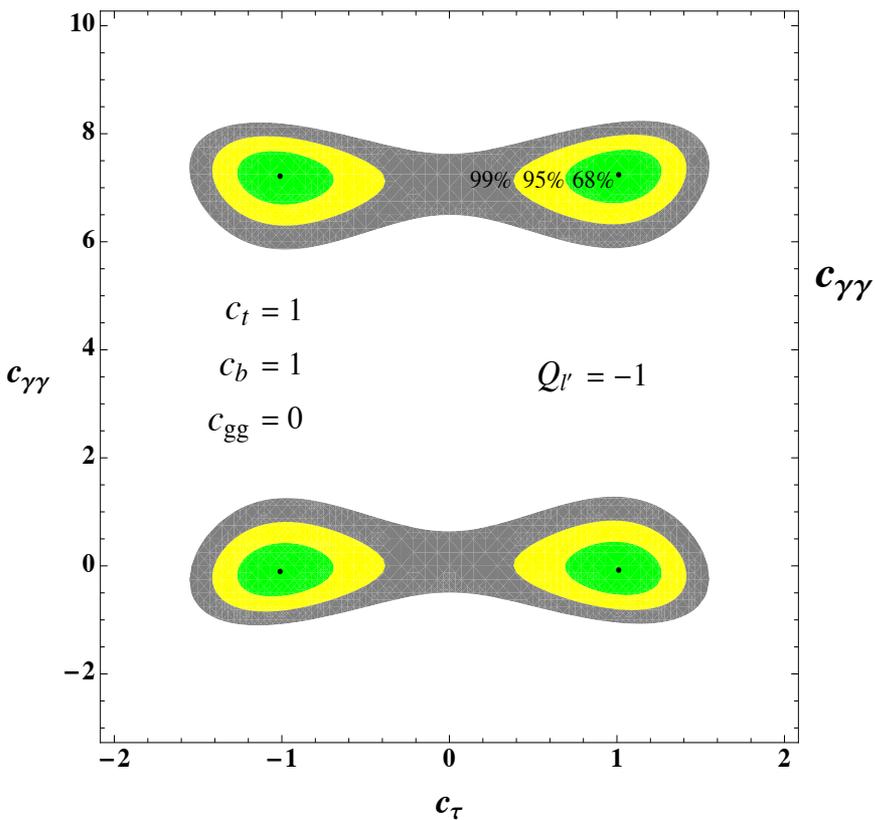
independently of  $Y_{q'}$ , masses,  $SU(2)_L$  repres.

(2 free parameters)

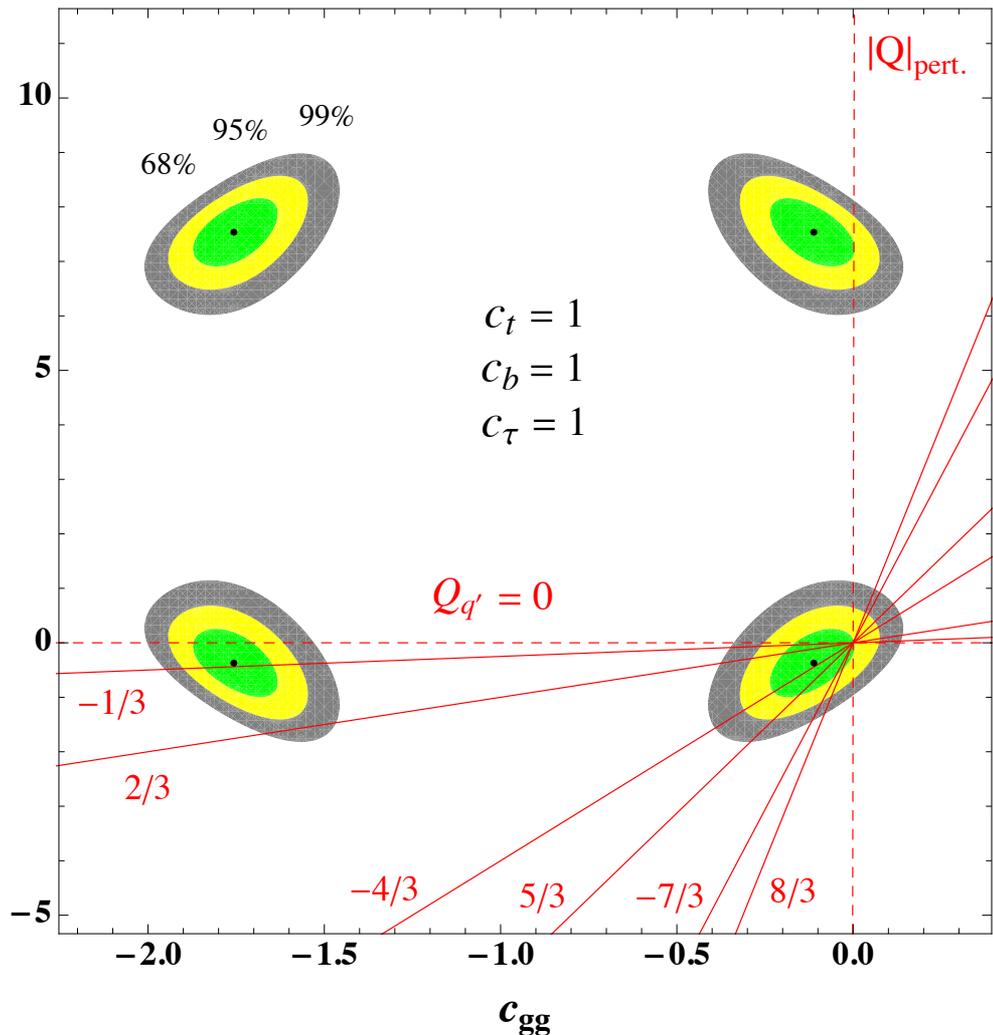


AFTER  
MORIOND...

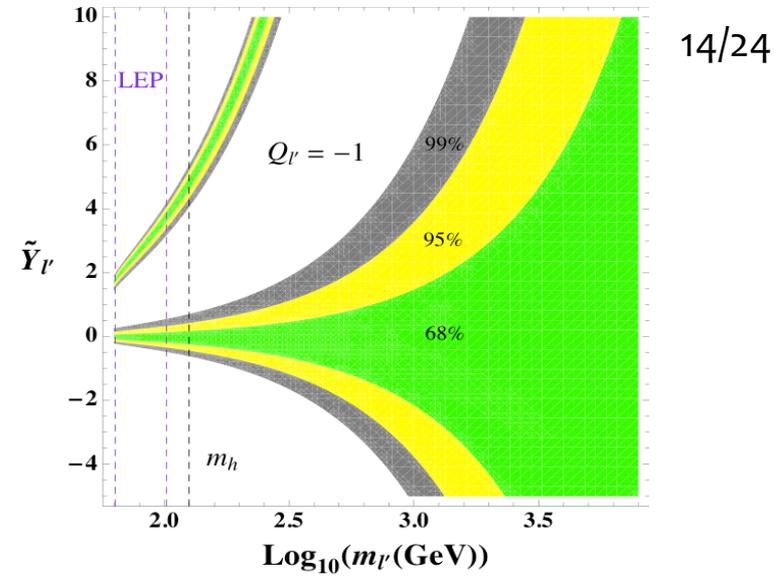
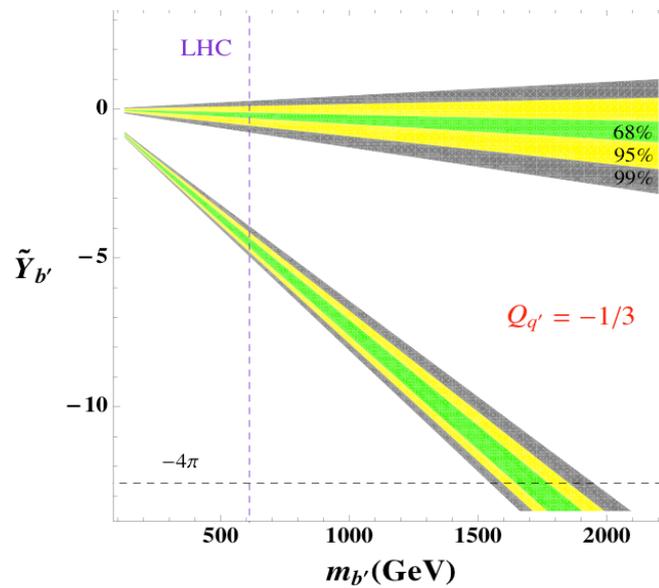
(2 free parameters)



independently of  $Y_{q'}$ , masses,  $SU(2)_L$  repres.



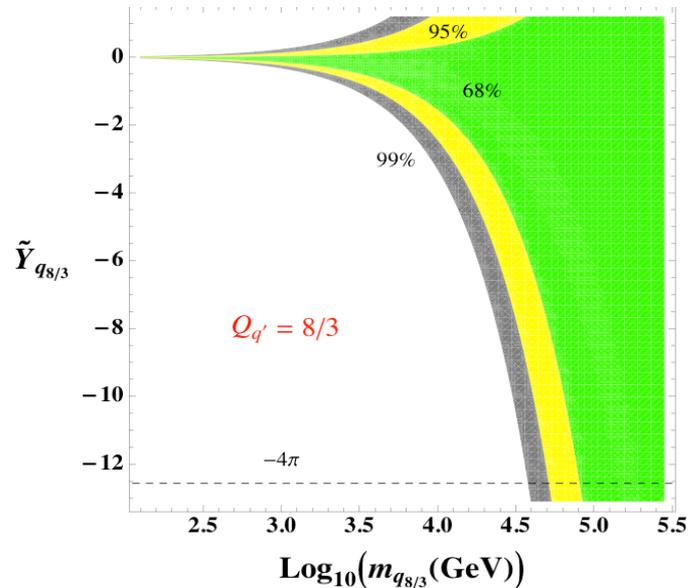
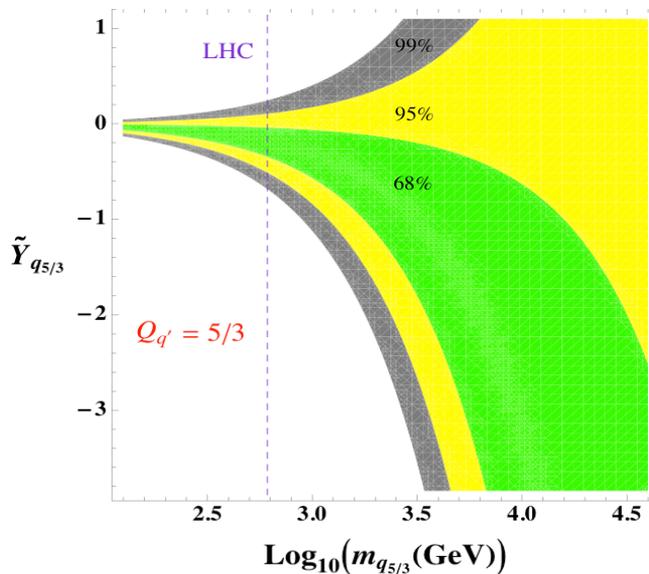
(1 free param.)



For low-charge  $q'$ ,  
*Extra-dysfermiophilia*:

$$\text{sign}\left(\frac{-Y_{q'}}{m_{q'}}\right) < 0$$

...increasing the  
diphoton rates.



$$q_{5/3} \rightarrow tW^+$$

$$q_{8/3} \rightarrow tW^+W^+$$

# Conclusions (A)

- ☀️ Already ***non-trivial*** & **generic constraints** on extra-fermions from the Higgs rate fit :
  - ☀️ Potentially stringent constraints on extra-quark electric charges **independently** of the *Yukawa's, masses,  $SU(2)_L$  representations*
  - ☀️ ***Extra-dysfermiophilia*** for low-charge single  $q'$  (colored as the top)
  - ☀️ The obtained plots can be used for any scenario with new fermions
- + ***Difficult and correlated*** determinations of some Yukawa couplings and parameters for the new loop-contributions to  $hgg$  ,  $h\gamma\gamma$ .

## B – The interests of rate ratios

### 1) *Get rid of the theoretical uncertainty*

The QCD uncertainty (PDF,  $\alpha_s^2$  @ LO, scale dependence) on the inclusive Higgs production cross section reaches  $\sim 15\text{-}20\%$  [LHCHWG]

..it affects  
the  $\mu$ 's fit

$$\mu_{XX}|_{\text{exp}} = \frac{\text{Nevts.}(pp \rightarrow H \rightarrow XX)}{\sum_i \epsilon_i^X \sigma_i(H) \text{BR}(H \rightarrow XX)|_{\text{SM}} \times \mathcal{L}}$$

$$\mu_{XX}|_{\text{th}} = \frac{\sum_i \epsilon_i^X \sigma_i(H) \text{BR}(H \rightarrow XX)}{\sum_i \epsilon_i^X \sigma_i(H) \text{BR}(H \rightarrow XX)|_{\text{SM}}}$$

$\delta_{\text{exp}}$

$\delta_{\text{th}}$

Taking  $\mu$  ratios can allow to suppress the QCD error :

$$\frac{\mu_{XX}}{\mu_{YY}} \Big|_{\text{exp}} = \frac{\text{Nevts.}(pp \rightarrow H \rightarrow XX)}{\text{Nevts.}(pp \rightarrow H \rightarrow YY)} \frac{\sum_i \epsilon_i^Y \sigma_i(H)|_{\text{SM}}}{\sum_i \epsilon_i^X \sigma_i(H)|_{\text{SM}}} \frac{\text{BR}(H \rightarrow YY)|_{\text{SM}}}{\text{BR}(H \rightarrow XX)|_{\text{SM}}}$$


 $\delta_{\text{exp}}$

can cancel out !

$$\underbrace{\frac{\mu_{XX}}{\mu_{YY}} \Big|_{\text{th}}}_{D_{XY}(c_f, c_V)} = \frac{\epsilon_{gg}^X \sigma(gg \rightarrow H) + \epsilon_{\text{VBF}}^X \sigma(qq \rightarrow Hqq) + \epsilon_{\text{HV}}^X \sigma(q\bar{q} \rightarrow VH) + \epsilon_{t\bar{t}H}^X \sigma(gg \rightarrow t\bar{t}H)}{\epsilon_{gg}^Y \sigma(gg \rightarrow H) + \epsilon_{\text{VBF}}^Y \sigma(qq \rightarrow Hqq) + \epsilon_{\text{HV}}^Y \sigma(q\bar{q} \rightarrow VH) + \epsilon_{t\bar{t}H}^Y \sigma(gg \rightarrow t\bar{t}H)}$$

$$\times \frac{\sum_i \epsilon_i^Y \sigma_i(H)|_{\text{SM}}}{\sum_i \epsilon_i^X \sigma_i(H)|_{\text{SM}}} \frac{\frac{\Gamma(H \rightarrow XX)|_{\text{SM}}}{\Gamma(H \rightarrow XX)|_{\text{SM}}}}{\frac{\Gamma(H \rightarrow YY)|_{\text{SM}}}{\Gamma(H \rightarrow YY)|_{\text{SM}}}}$$

## II) Fitting ratios of signal strengths

Usual fits of the Higgs rates :

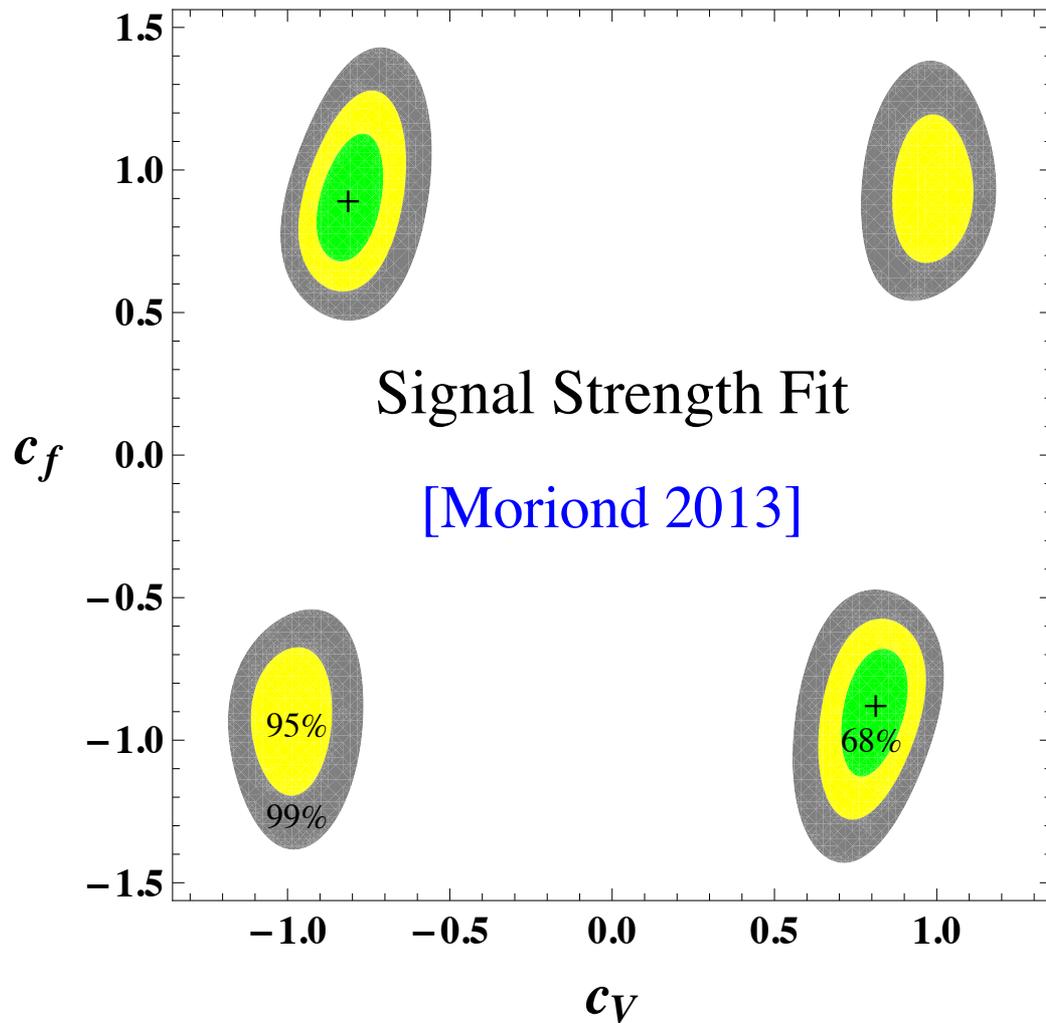
$$\begin{aligned} \mathcal{L}_h = & c_W g_{HWW} H W_\mu^+ W^{-\mu} + c_Z g_{HZZ} H Z_\mu^0 Z^{0\mu} \\ & - c_t Y_t H \bar{t}_L t_R - c_c Y_c H \bar{c}_L c_R - c_b Y_b H \bar{b}_L b_R - c_\tau Y_\tau H \bar{\tau}_L \tau_R + \text{h.c.} \end{aligned}$$

$$\left( Y_{t,c,b,\tau} = m_{t,c,b,\tau}/v \quad g_{HWW} = 2m_W^2/v, g_{HZZ} = m_Z^2/v \right)$$

$$\chi^2 = \sum_i \frac{[\mu_i(c_f, c_V) - \mu_i|_{\text{exp}}]^2}{(\delta\mu_i)^2}$$

$$\delta\mu_i = \sqrt{\delta\mu_i|_{\text{exp}}^2 + \delta\mu_i|_{\text{th}}^2}$$

(2 free parameters)



(without the CMS  
diphoton data from  
Moriond QCD)

Symmetry:

$$c_f \rightarrow -c_f, c_V \rightarrow -c_V$$

Now fitting ratios of the Higgs rates :

$$\chi_r^2 = \frac{[D_{Z\gamma}^{gg}(c_f, c_V) - \frac{\mu_{ZZ}}{\mu_{\gamma\gamma}}|_{\text{exp}}^{gg}]^2}{[\delta(\frac{\mu_{ZZ}}{\mu_{\gamma\gamma}})_{gg}]^2} + \frac{[D_{\tau W}^{gg}(c_f, c_V) - \frac{\mu_{\tau\tau}}{\mu_{WW}}|_{\text{exp}}^{gg}]^2}{[\delta(\frac{\mu_{\tau\tau}}{\mu_{WW}})_{gg}]^2} + \frac{[D_{\tau W}^{\text{VBF}}(c_f, c_V) - \frac{\mu_{\tau\tau}}{\mu_{WW}}|_{\text{exp}}^{\text{VBF}}]^2}{[\delta(\frac{\mu_{\tau\tau}}{\mu_{WW}})_{\text{VBF}}]^2}$$

$$D_{Z\gamma}^{gg} \simeq \frac{\frac{\Gamma(H \rightarrow ZZ)}{\Gamma(H \rightarrow ZZ)|_{\text{SM}}}}{\frac{\Gamma(H \rightarrow \gamma\gamma)}{\Gamma(H \rightarrow \gamma\gamma)|_{\text{SM}}}}, \quad D_{\tau W}^{gg} \simeq D_{\tau W}^{\text{VBF}} \simeq \frac{\frac{\Gamma(H \rightarrow \tau\tau)}{\Gamma(H \rightarrow \tau\tau)|_{\text{SM}}}}{\frac{\Gamma(H \rightarrow WW)}{\Gamma(H \rightarrow WW)|_{\text{SM}}}}$$

$$\left\{ \begin{array}{l} D_{Z\gamma} \simeq |c_Z|^2 \left\{ \frac{|\frac{1}{4}c_W A_1[m_W] + (\frac{2}{3})^2 c_t A[m_t] + (-\frac{1}{3})^2 c_b A[m_b] + (\frac{2}{3})^2 c_c A[m_c] + \frac{1}{3}c_\tau A[m_\tau]|^2}{|\frac{1}{4}A_1[m_W] + (\frac{2}{3})^2 A[m_t] + (-\frac{1}{3})^2 A[m_b] + (\frac{2}{3})^2 A[m_c] + \frac{1}{3}A[m_\tau]|^2} \right\}^{-1} \\ D_{\tau W} \simeq \frac{|c_\tau|^2}{|c_W|^2} \end{array} \right. \left( \begin{array}{l} \tau(m) = m_H^2/4m^2 \quad A[\tau(m) \ll 1] \rightarrow 1 \\ \text{for } m_H \simeq 125 \text{ GeV, } A_1[\tau(m_W)] \simeq -8.3 \end{array} \right)$$

(2 free parameters)

Less informations than on  
individual signal strengths

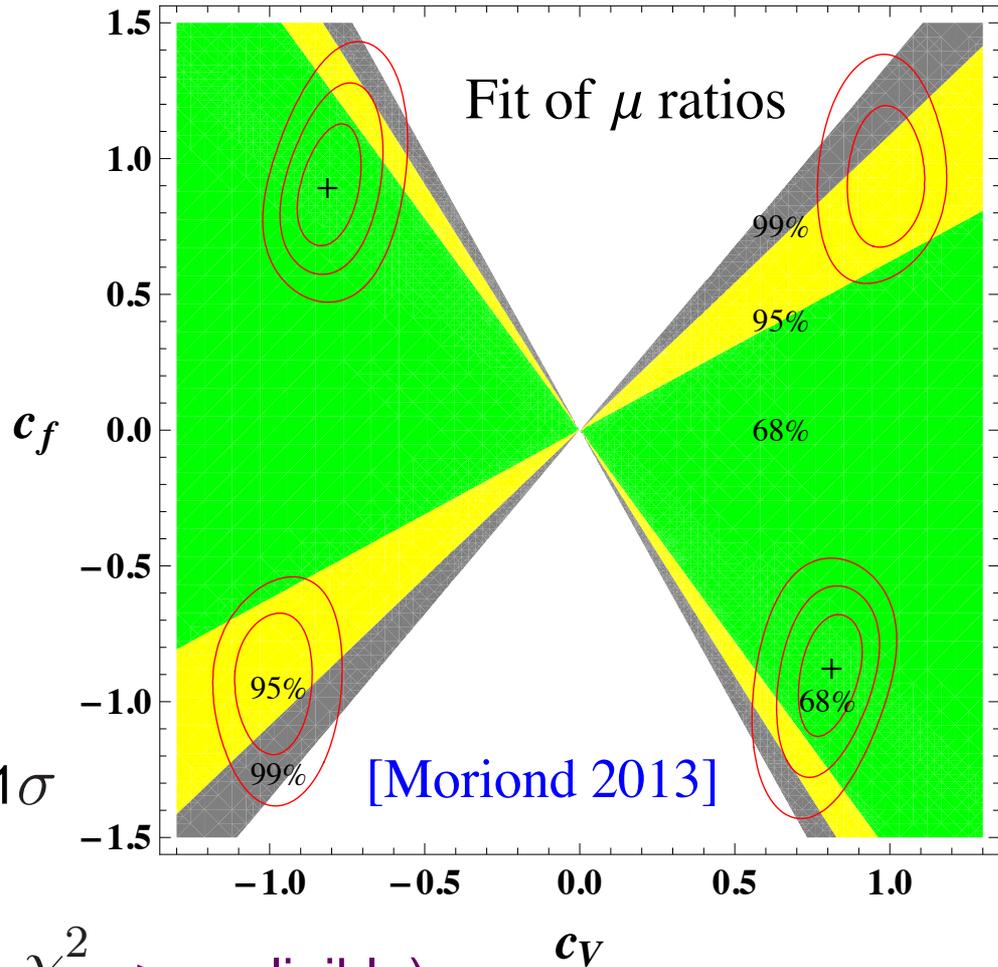
+

Combined Num. & Denominator  
experimental errors



Best-fit regions larger for ratios  
and containing the  $\mu$  domains at  $1\sigma$

(theoretical error in quadrature for  $\chi^2 \Rightarrow$  negligible)



(2 free parameters)

Theoretical error added linearly  
(no statistical distribution)

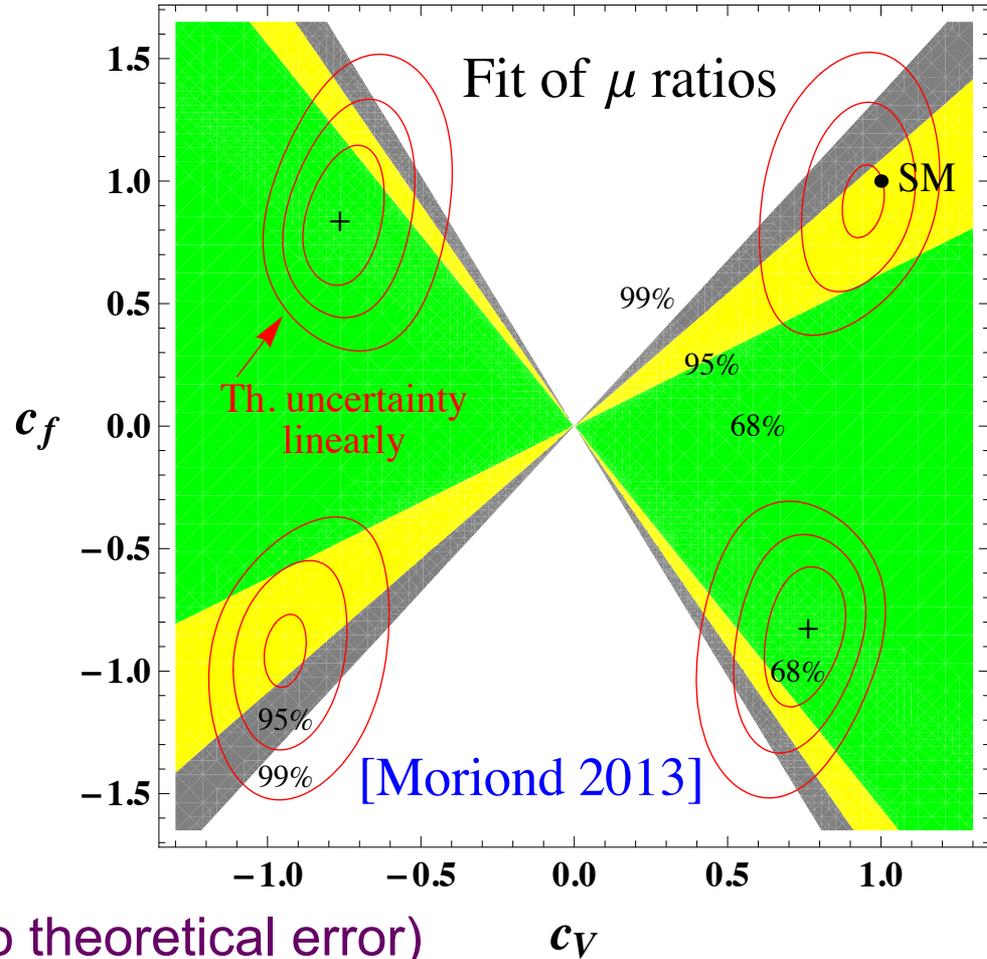


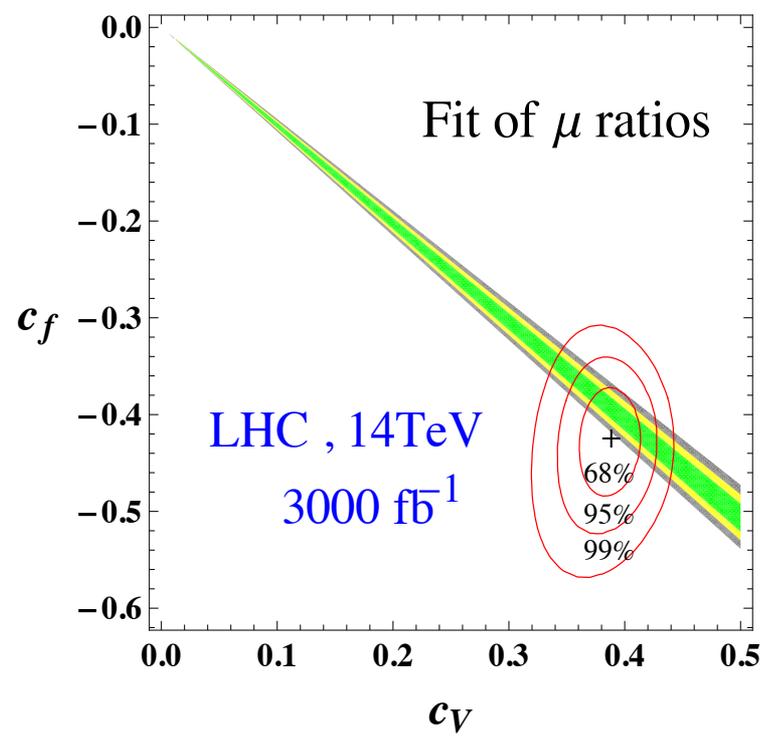
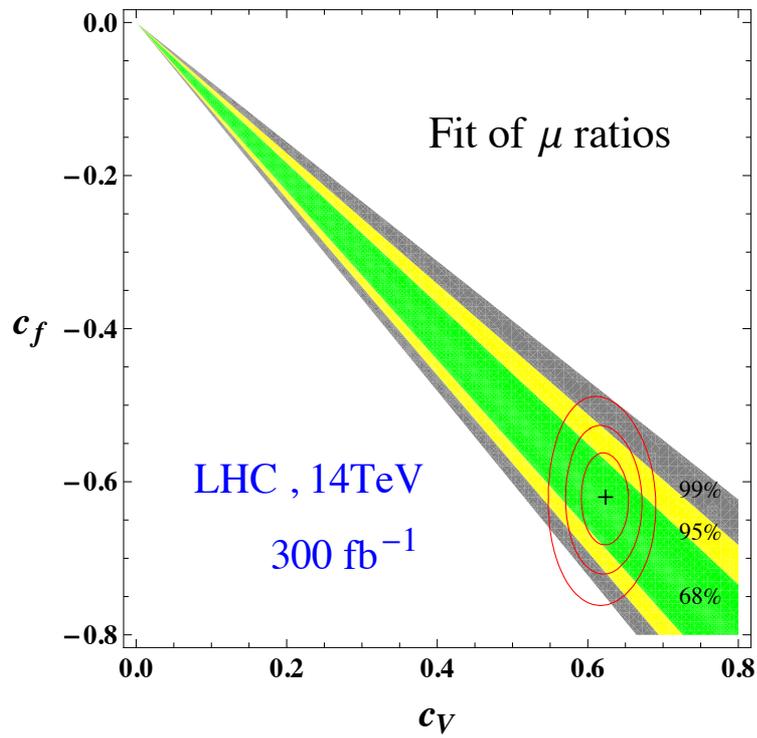
Best-fit  $\chi^2$  regions larger



$\chi_r^2$  domains rule out  
 $\chi^2$  regions at  $1\sigma$   
including the **SM** point !

(more constraining with  $\chi_r^2$  as no theoretical error)





Assuming the statistical error to decrease like  $1/\sqrt{\sigma_i \mathcal{L}}$   
we add up 14TeV LHC results in the fits...

$\chi^2$  dominated by  $\delta_{\text{th}} \Rightarrow$  constant region sizes  
 $\chi_r^2$  uncertainties decrease  $\Rightarrow$  more precise c's

Crucial  $\chi_r^2$  rôle

## Conclusions (B)

- ☀ Fitting the ratios of Higgs rates already improves the constraints on the  $c_f$ ,  $c_V$  parameters (for linear combination of exp./th. uncertainties)
- ☀ *Combining the fits of the signal strengths and of their ratios can turn out to be crucial for the precise determination of the Higgs couplings @ LHC.*

Back up

$$\epsilon_t c_t = \frac{\text{sign}(m_t)}{\text{sign}(m_t^{\text{EF}})} c_t = \frac{\text{sign}(m_t)}{\text{sign}(m_t^{\text{EF}})} \frac{\text{sign}(-Y_t^{\text{EF}})}{\text{sign}(-Y_t)} |c_t| = \frac{\text{sign}(-Y_t^{\text{EF}})}{\text{sign}(m_t^{\text{EF}})} |c_t| = \text{sign}\left(\frac{-Y_t^{\text{EF}}}{m_t^{\text{EF}}}\right) \left|\frac{Y_t^{\text{EF}}}{Y_t}\right|$$