Homework problems #5

- 1. Explain the source, i.e. find out in the derivation presented in the lecture, what is the reason for the gauge invariance for the kinetic term of the massless graviton.
- 2. Construct the inverse of the kinetic operator for the massless graviton

$$K_{\mu\nu;\lambda\sigma} = \frac{1}{2} \left[\eta_{\mu\lambda} \eta_{\nu\sigma} + \eta_{\mu\sigma} \eta_{\nu\lambda} - \eta_{\mu\nu} \eta_{\lambda\sigma} \right] (-\Box)$$

3. Construct the inverse of the kinetic operator for the massive graviton

$$K_{\mu\nu;\alpha\beta} = (\eta_{\mu\alpha}\eta_{\nu\beta} - \eta_{\mu\nu}\eta_{\alpha\beta})(-\Box) - \eta_{\mu\nu}\partial_{\alpha}\partial_{\beta} - \eta_{\alpha\beta}\partial_{\mu}\partial_{\nu} + \eta_{\mu\alpha}\partial_{\nu}\partial_{\beta} + \eta_{\nu\beta}\partial_{\mu}\partial_{\alpha} - m^{2}(\eta_{\mu\alpha}\eta_{\nu\beta} - \eta_{\mu\nu}\eta_{\alpha\beta})$$