

# Kinks in the dispersion relations of strongly correlated fermions

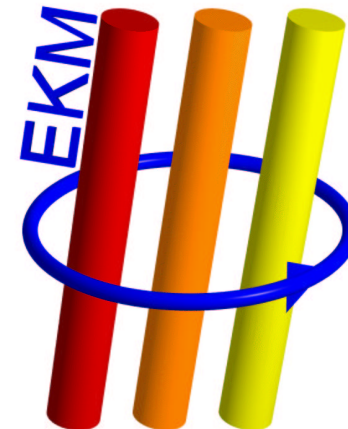
Krzysztof Byczuk

Institute of Physics, EKM, Augsburg University, Germany

*September 17th, 2006*

*dedicated to prof. Jozef Spalek*

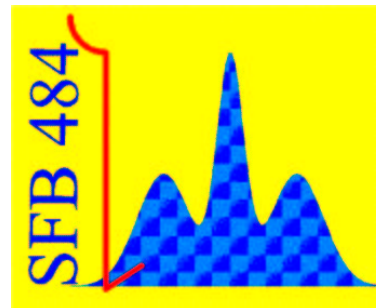
*on the occasion of his 60th birthday*



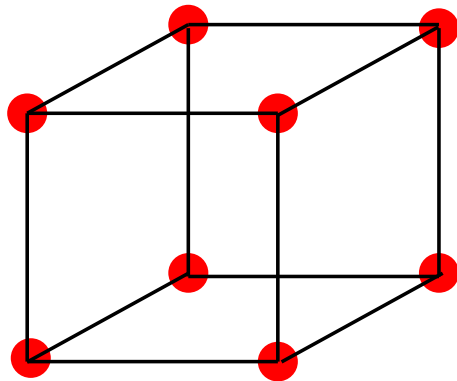
# Collaboration

- M. Kollar, D. Vollhardt, Augsburg, Germany
- K. Held, Y.-F. Yang, Stuttgart, Germany
- I. Nekrasov, Ekaterinburg, Russia
- T. Pruschke, Göttingen, Germany

Support from SFB 484



# Standard model of quantum many-body system



emergent particles

quasiparticle

quasihole

holon

spinon

plasmon

magnon

phonon

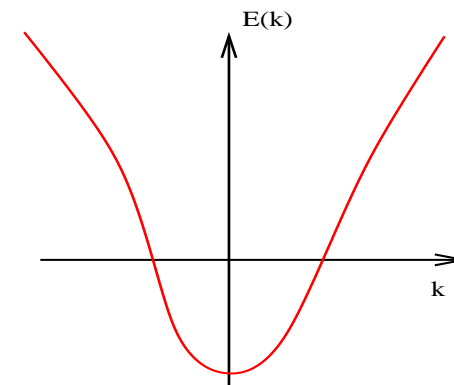
polariton

exciton

anyon

g-on

...



(i) well defined dispersion relation  $E(\mathbf{k})$

(ii) long (infinite) life-time  $\tau$

(iii) proper set of quantum numbers

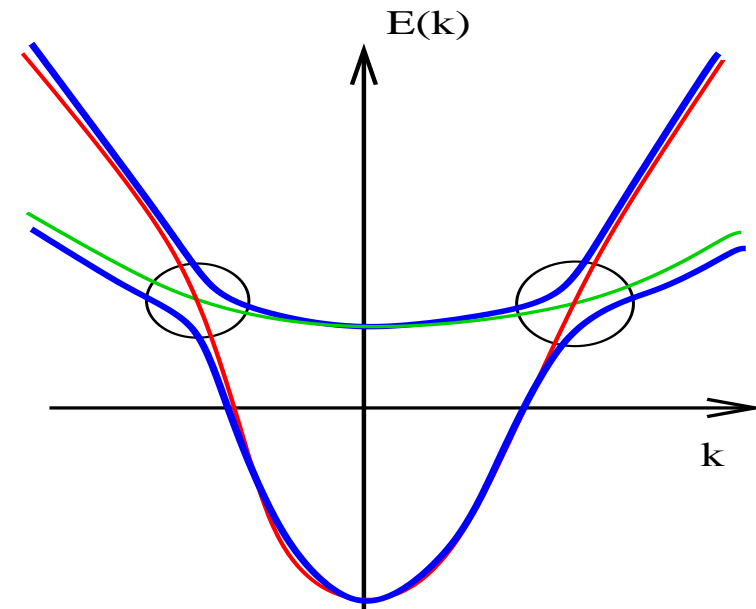
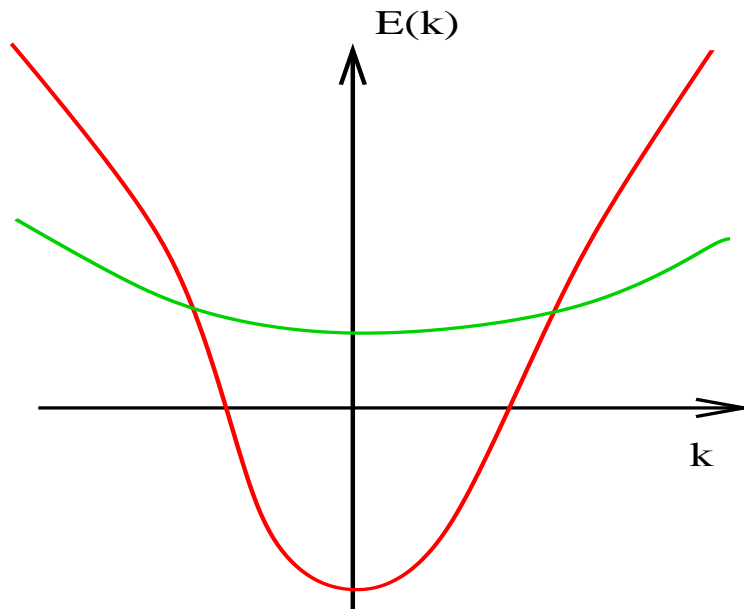
(iv) statistics

# Dispersions and kinks

Coupling/hybridization  $\hat{V}$  between different particles/modes

$$\langle \Psi | \hat{V} | \Phi \rangle \neq 0$$

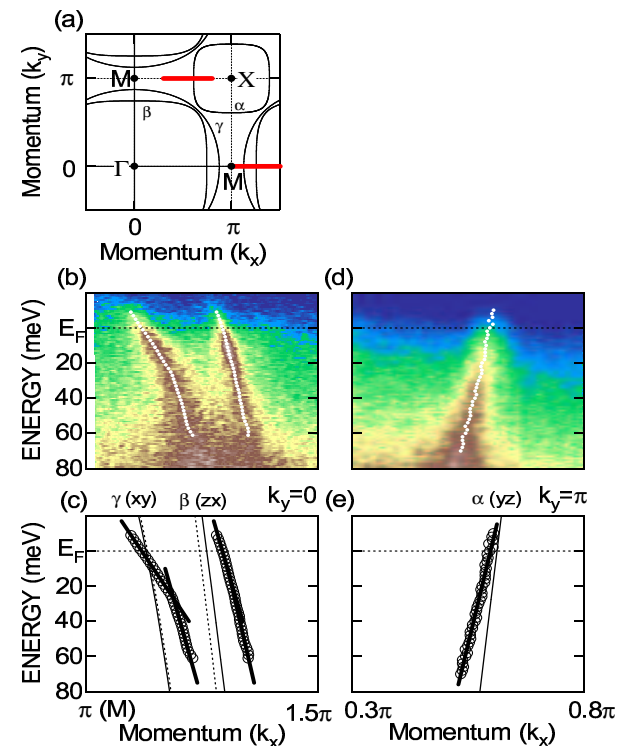
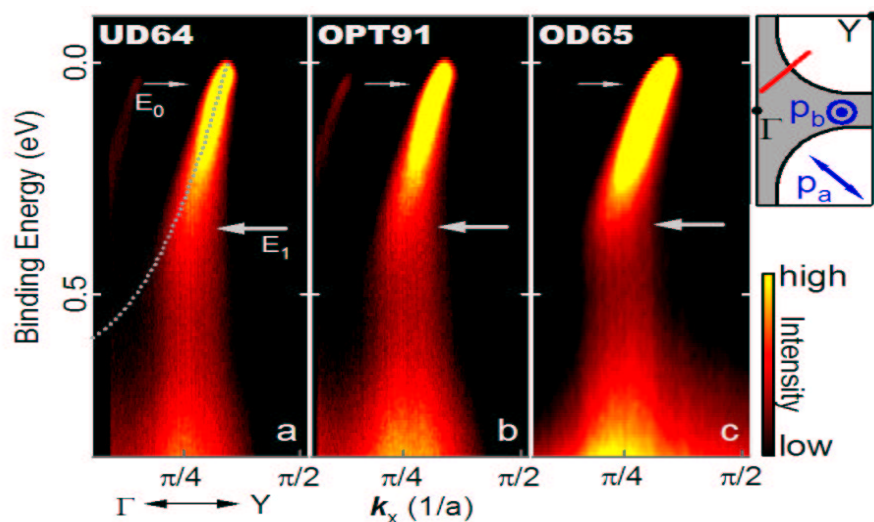
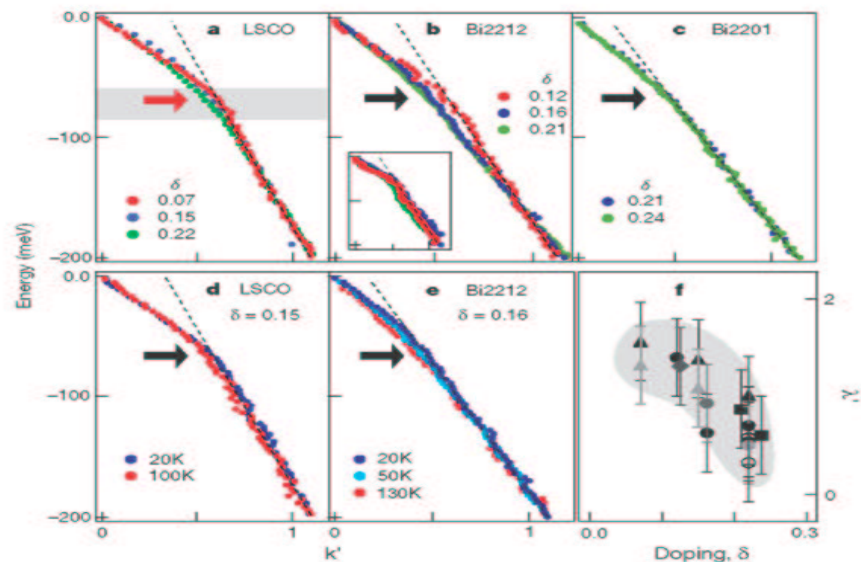
anticrossing, lifting degeneracy, ...



**Df. kinks are abrupt slope changes in the dispersion relations**

they provide information on different modes and their coupling

# Examples of kinks in ARPES

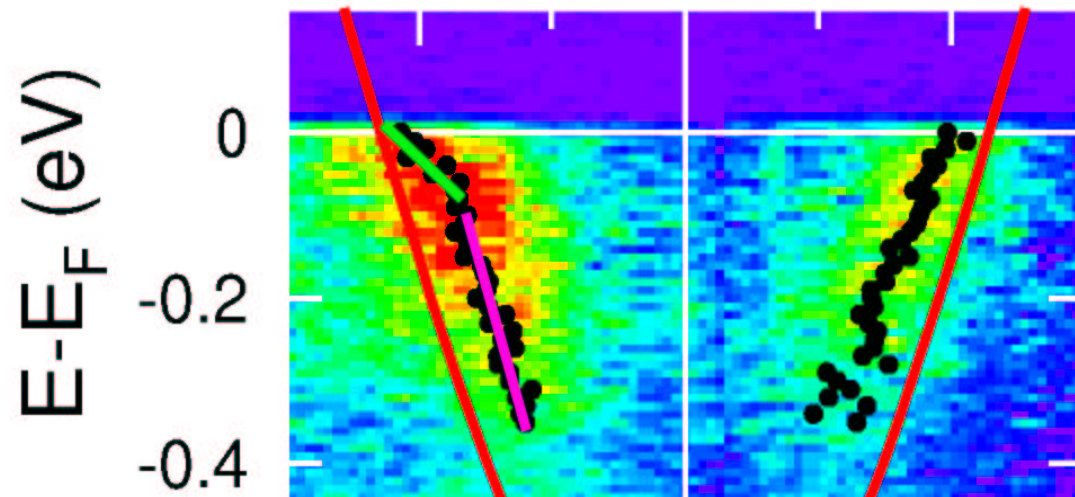


$Sr_2RuO_4$ , cond-mat/0508312

Kinks seen experimentally between 20-800 meV  
Origin: phonons, spin fluctuations, often not known

different HTC systems, cond-mat/0604284, cond-mat/0607319

# More examples of kinks in ARPES



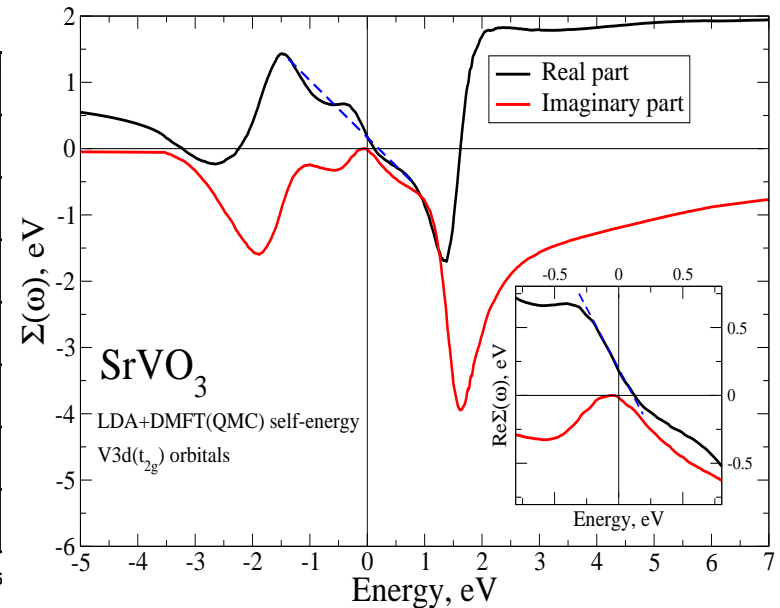
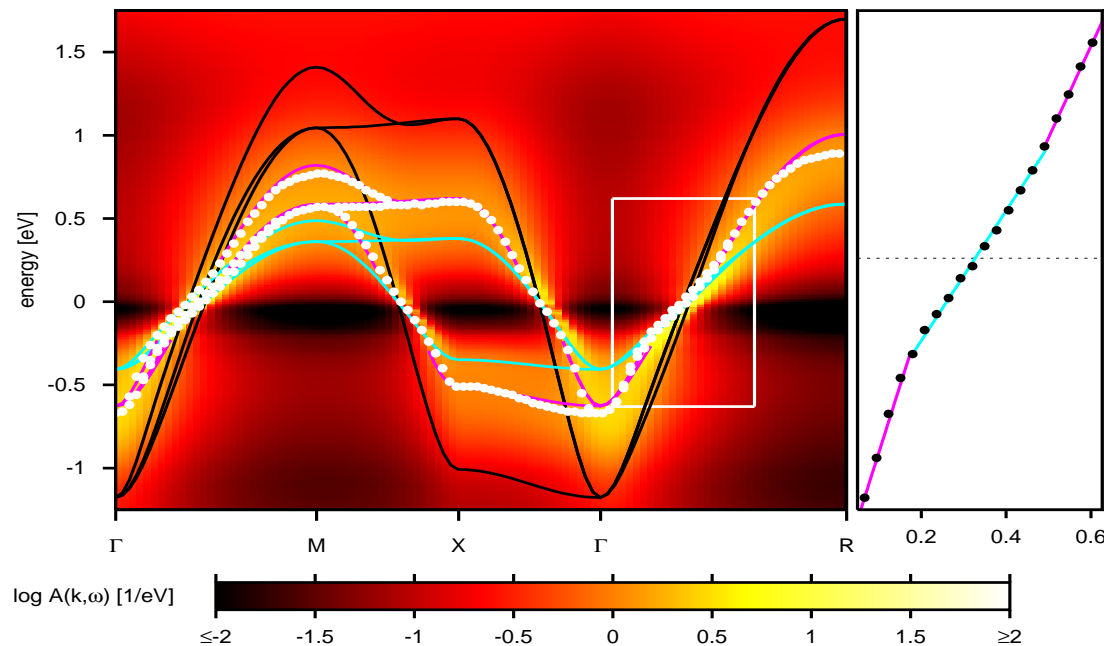
SrVO<sub>3</sub>, cond-mat/0504075

Kinks seen experimentally at 150 meV  
Pure electronic origin?

# Kinks in LDA+DMFT study of SrVO<sub>3</sub>

plain band model with local correlations, no other bosons, ... but kinks!

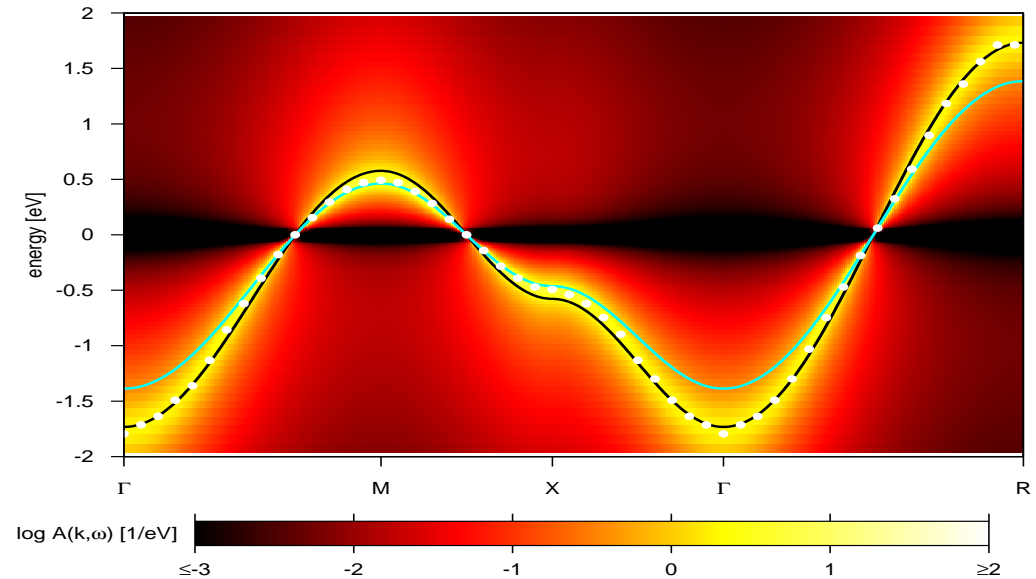
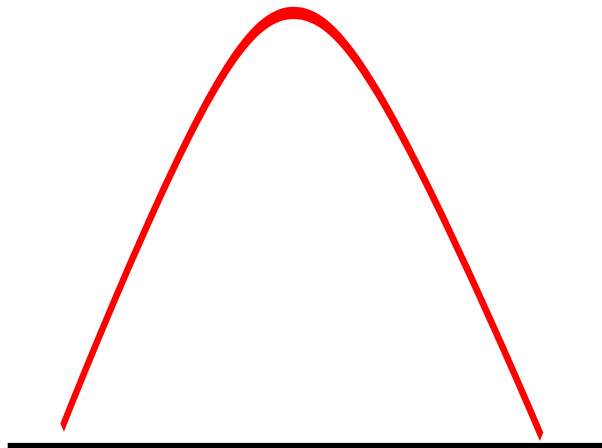
I.A. Nekrasov *et al.*, cond-mat/0508313, PRB (2006)



$$G_{\mathbf{k}}(\omega) = \frac{1}{\omega + \mu - \epsilon_{\mathbf{k}} - \Sigma(\omega)} \quad \rightarrow \quad E_{\mathbf{k}} + \mu - \epsilon_{\mathbf{k}} - \text{Re}\Sigma(E_{\mathbf{k}}) = 0$$

Not found in SIAM with simple hybridization function!  $\rightarrow$  DMFT self-consistency effect

# Weakly correlated system

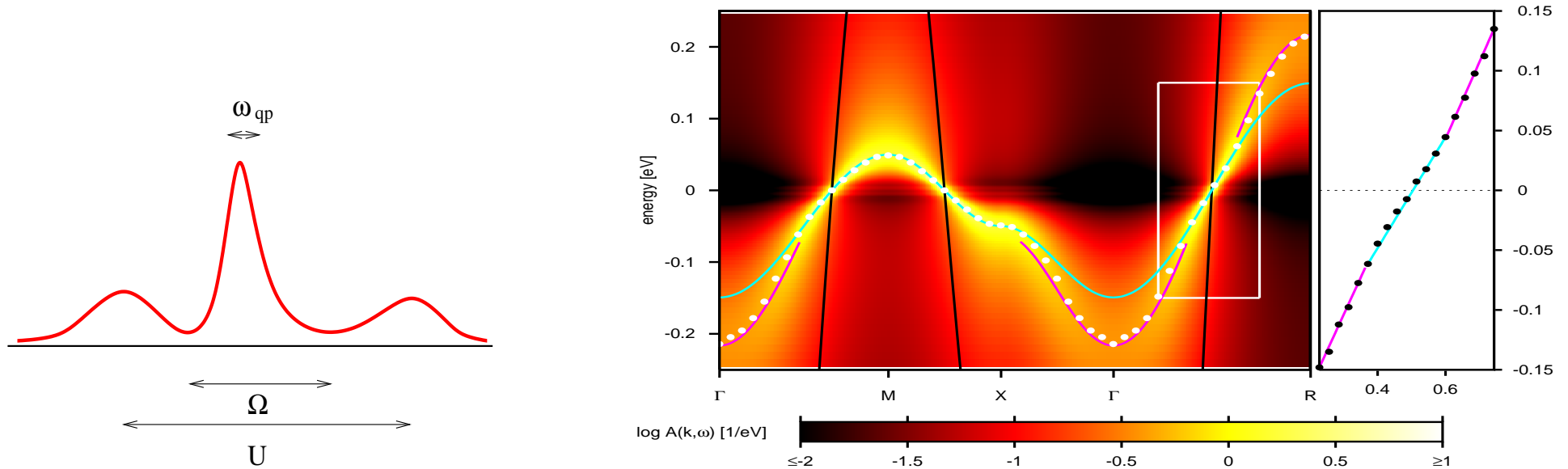


Fermi liquid  $Z_{FL} \lesssim 1$ :  $E_{\mathbf{k}} = Z_{FL} \epsilon_{\mathbf{k}}$  for  $|E_{\mathbf{k}}| < \omega_*$

$E_{\mathbf{k}} = \epsilon_{\mathbf{k}}$  for  $|E_{\mathbf{k}}| > \omega_*$



# Kinks due to strong correlations



Fermi liquid  $Z_{FL} \ll 1$ :  $E_{\mathbf{k}} = Z_{FL}\epsilon_{\mathbf{k}}$  for  $|E_{\mathbf{k}}| < \omega_*$

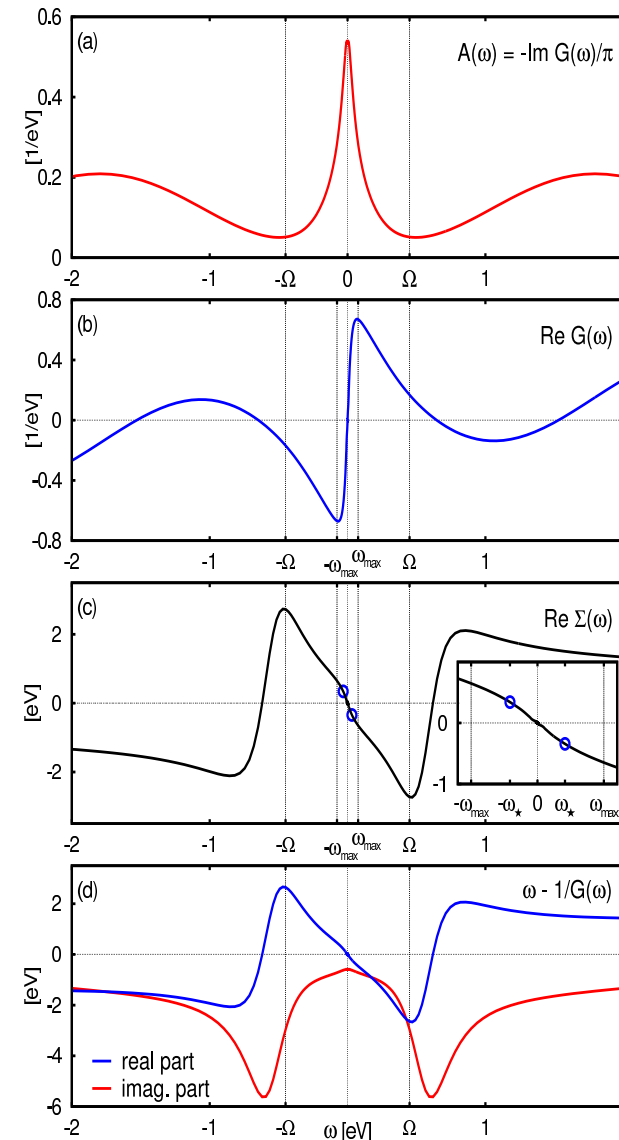
Different renormalization  $Z_{CP} \ll 1$ :  $E_{\mathbf{k}} = Z_{CP}\epsilon_{\mathbf{k}} \pm c$  for  $|E_{\mathbf{k}}| > \omega_*$

# Mathematical explanation of kinks within DMFT

DMFT self-consistency condition

$$\Sigma(\omega) = \omega - 1/G(\omega) - \Delta(G(\omega))$$

$$\Delta(G(\omega)) \approx (m_2 - m_1^2)G(\omega) + \dots$$



# Microscopic predictions - summary

- Strong correlations (three peak spectral function) a sufficient condition for electronic kinks
- **Energy scale** for electronic kinks  $\omega_* = Z_{FL}D$  determined by Fermi-liquid renormalization and bare (LDA) density of states
- $\omega_*$  sets the energy scale for Fermi-liquid regime where  $E_{\mathbf{k}} = Z_{FL}\epsilon_{\mathbf{k}}$  for  $|E_{\mathbf{k}}| < \omega_*$
- **Beyond Fermi-liquid regime** the dispersion is still **renormalized** and **useful**  $E_{\mathbf{k}} = Z_{CP}\epsilon_{\mathbf{k}} \pm c$  for  $|E_{\mathbf{k}}| > \omega_*$  where the offset  $c$  and  $Z_{CP}$  determined by  $Z_{FL}$  and  $D$
- Electronic kinks are within cluster extension of DMFT (DCA)  
$$\Sigma_{\mathbf{K}}(\omega) = \omega - \frac{1}{G_{\mathbf{K}}(\omega)} - \Delta(G_{\mathbf{K}}(\omega))$$
- **Electronic kinks are generic feature of strongly correlated systems**