

# Semiconductor magneto optics

## various ways of seeing spins



Jan Gaj [gaj@fuw.edu.pl](mailto:gaj@fuw.edu.pl):

Physics Department, Warsaw University

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# Outline

- Where? What?
- Fundamentals
  - Faraday and Kerr rotation
  - Magnetic circular dichroism
  - PL polarization,
- Seeing spins in experiments
  - spin energy: Zeeman effect in absorption, Faraday and Kerr rotation
  - average spin - magnetization (also spontaneous) : PL polarization
  - efficiency of spin injection: PL
  - carrier spin polarization: Faraday
  - magnetic ion spin temperature: PL
  - electron spin dynamics: time-resolved Kerr
  - spatial distribution: spin mapping: PL, Kerr

# Where?

- Medium and large gap semiconductors
- Interband transitions
- Bulk crystals and quantum wells

# What?

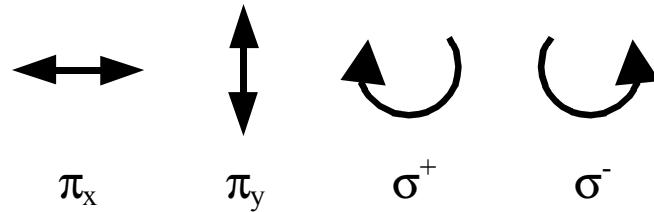
- Information about spins of carriers, excitons, magnetic ions

# Fundamentals

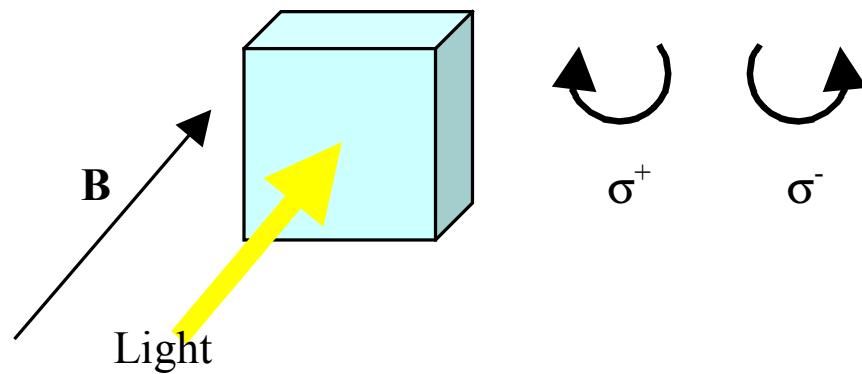
Faraday, Kerr, MCD, PL

# Faraday configuration

- In an isotropic medium all the polarizations represent eigenmodes of the electromagnetic wave.



- in Faraday configuration only  $\sigma^+$  and  $\sigma^-$  represent eigenmodes.



- polarization-dependent complex refraction index

$$\tilde{n}_{\pm} = n_{\pm} - i \kappa_{\pm}$$

# Dispersion relations

- Origin: causality principle
- Detailed form: symmetry of the response function
- Without magnetic field: Kramers – Kronig form

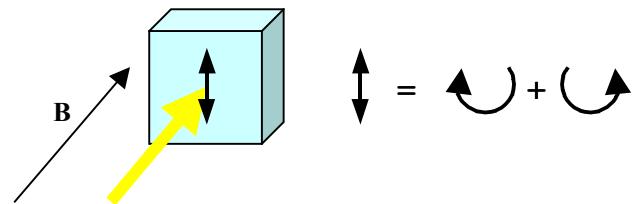
$$n(\omega) - 1 = -\frac{2}{\pi} \int_0^\infty \frac{\omega' \kappa(\omega') d\omega'}{\omega^2 - \omega'^2} \quad \kappa(\omega) = \frac{2\omega}{\pi} \int_0^\infty \frac{(n(\omega') - 1) d\omega'}{\omega^2 - \omega'^2}$$

- Applying DR to the experimental data: difficult
- Hint: modeling with real and imaginary part of a complex function (e.g., Lorentzian)

See, e.g., F. Byron and R. Fuller, *Mathematics of Classical and Quantum Physics* (Addison-Wesley, Reading, MA, 1969).

# Faraday rotation

- Decomposition of linearly polarized light in two circularly polarized waves

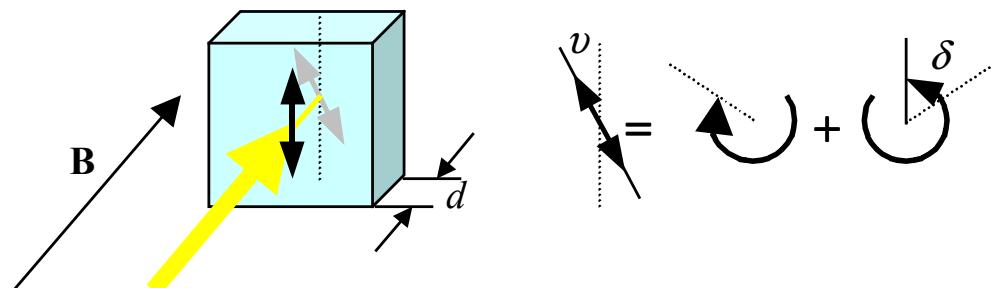


- Phase shift

$$\delta = \frac{\omega}{c} (n_+ - n_-) d$$

- Rotation of the polarization plane

$$\vartheta = \frac{1}{2} \delta = \frac{\omega}{2c} (n_+ - n_-) d$$

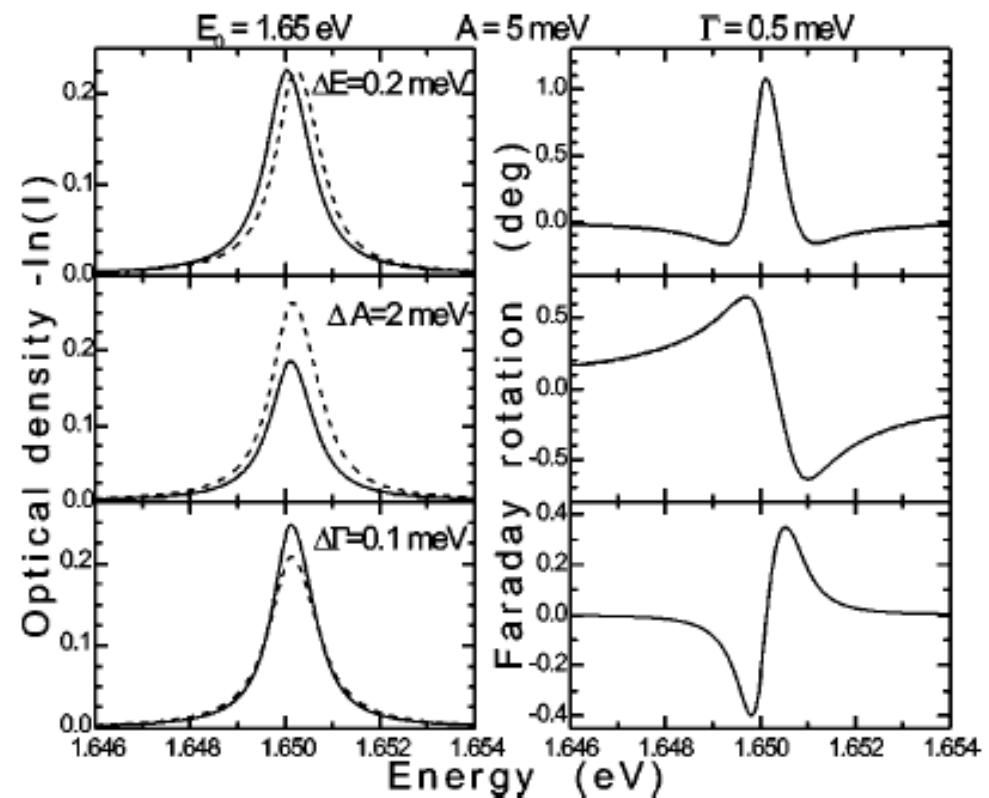


# Example: modeling Faraday rotation of a single absorption line

Zeeman

Amplitude

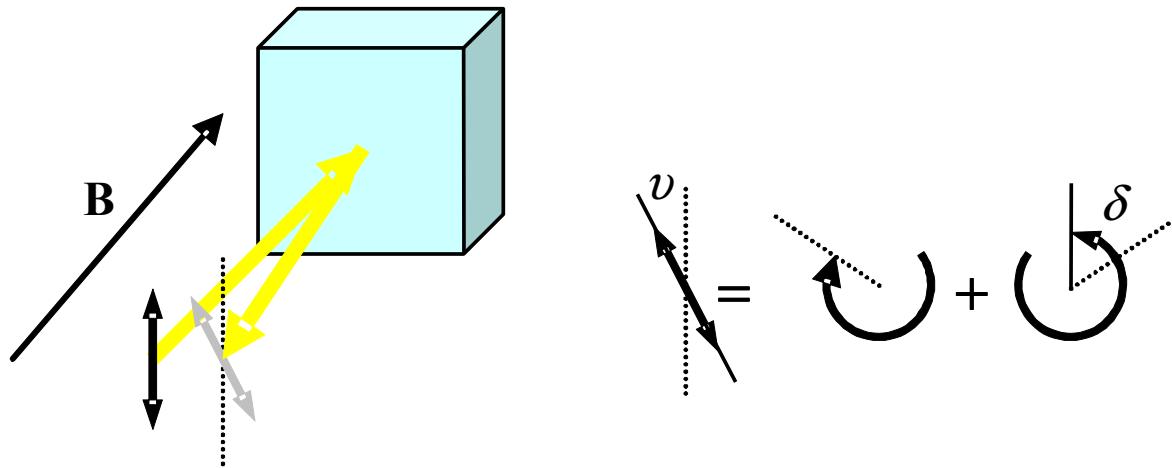
Line width



$$t = |t| e^{i\varphi} = \sqrt{T} e^{i\varphi} \quad 2 \ln t = \ln T + 2i\varphi$$

# Kerr rotation

- Phase shift between the two circularly polarized components on reflection
- Cause: magnetic field or magnetization.
- Simplest case: Faraday geometry (polar Kerr effect).



# Kerr rotation

Backscattering geometry

Amplitude ( $r$ ) and intensity ( $R$ ) reflection coefficients

$$r = \frac{\tilde{n} - 1}{\tilde{n} + 1} = \frac{n - 1 - i\kappa}{n + 1 - i\kappa} = |r|e^{i\varphi} = \sqrt{R}e^{i\varphi} \quad R = \frac{(n-1)^2 + \kappa^2}{(n+1)^2 + \kappa^2}$$

Kerr rotation angle

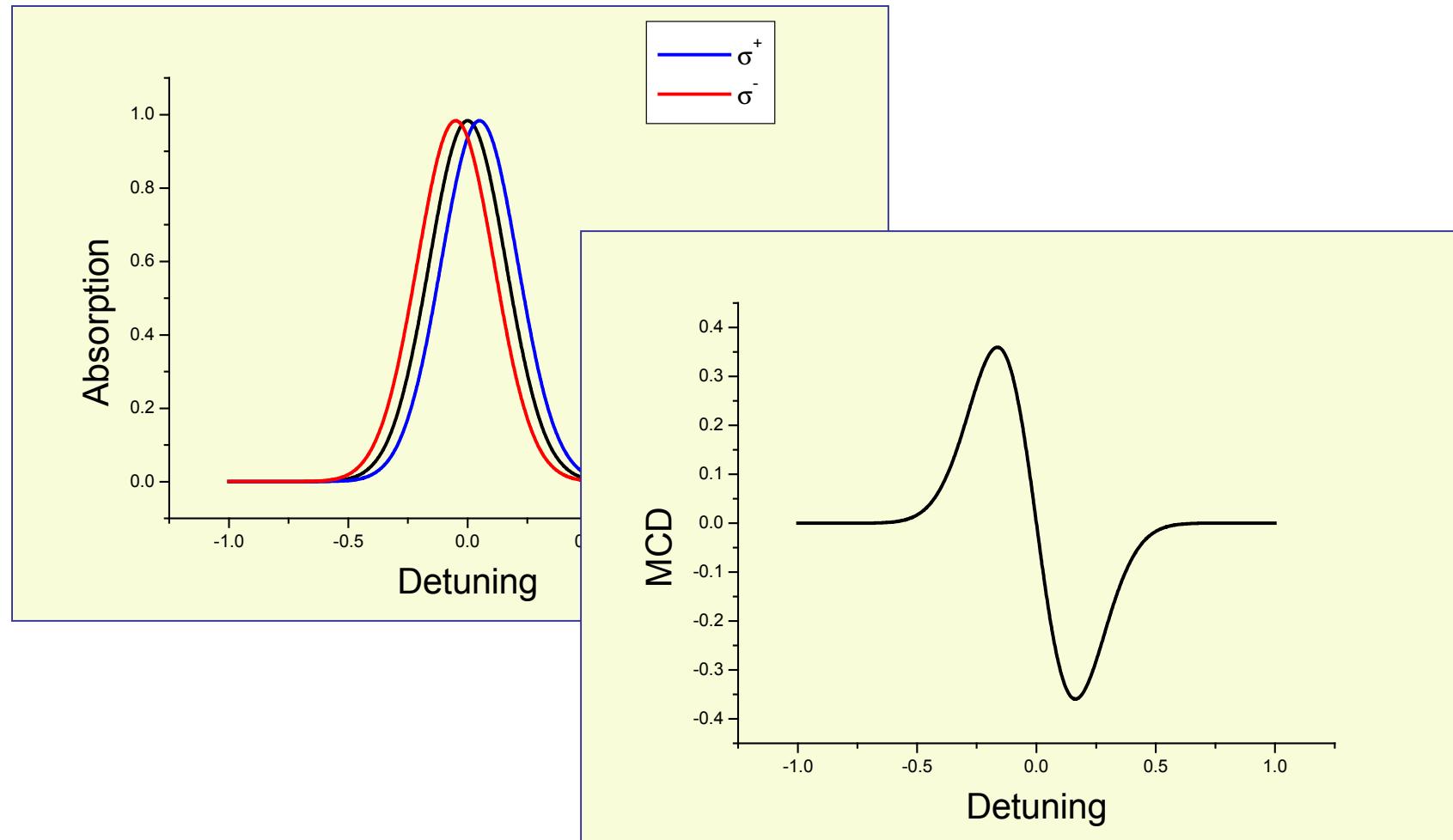
$$\vartheta_K = \frac{1}{2} \delta_K = \frac{1}{2} (\varphi_+ - \varphi_-)$$

$$2 \ln r = \ln R + 2i\varphi$$

Dispersion relations between  $\ln R$  and  $2\varphi$  useful for modeling

# Magnetic Circular Dichroism

## difference in intensity



# Real and effective magnetic field

- Magnetic field influences carriers.

$$H = H_o + H_s; \quad H_s = g\mu_B \mathbf{B} \cdot \boldsymbol{\sigma}$$

- Interaction with magnetic ions:

$$H_{exch} = \sum_j J(\mathbf{r} - \mathbf{R}_j) \mathbf{S}_j \cdot \boldsymbol{\sigma}$$

- The effective (exchange) field acts only on the carrier spin!

$$\mathbf{B}_{eff} = \frac{1}{g\mu_B} \sum_j J(\mathbf{r} - \mathbf{R}_j) \mathbf{S}_j$$

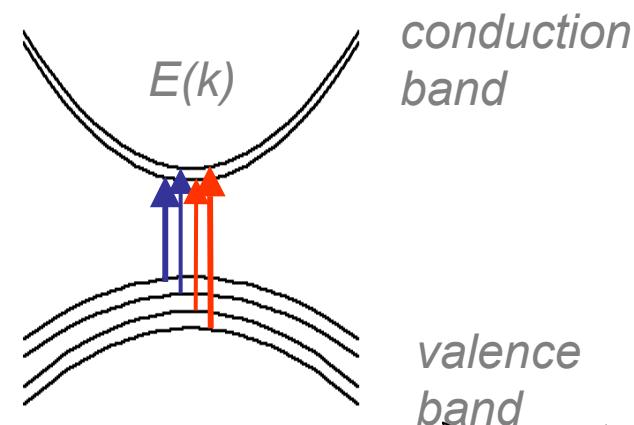
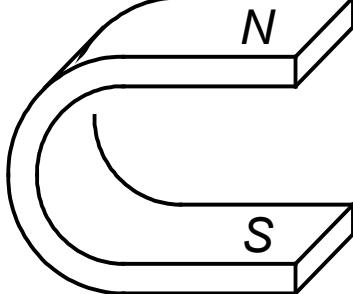
- Proportionality to magnetization

- In most cases:

$$H_{exch} \gg H_s, H_o$$

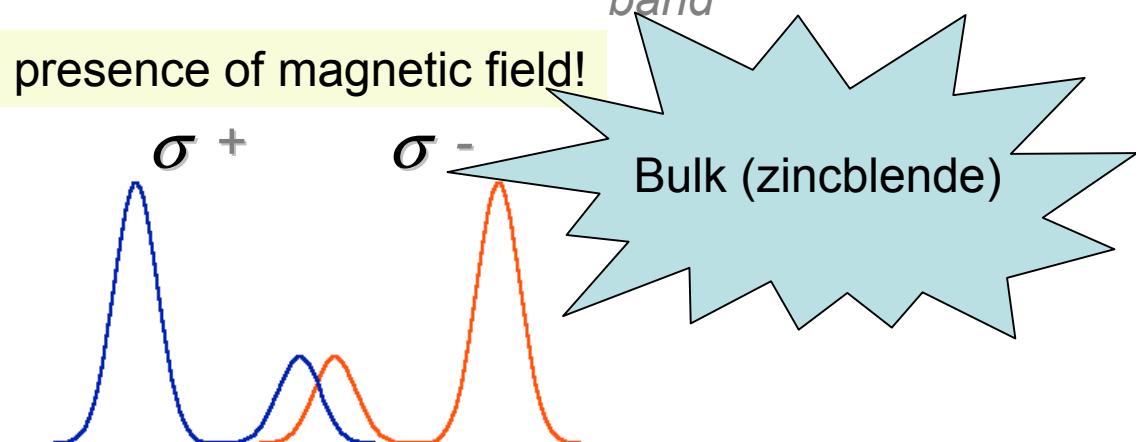
See, e.g., J.K. Furdyna, J. Appl. Phys. 64, R29 (1988)

# Diluted magnetic semiconductor



approximation: wavevector in presence of magnetic field!

- *excitonic absorption spectrum*

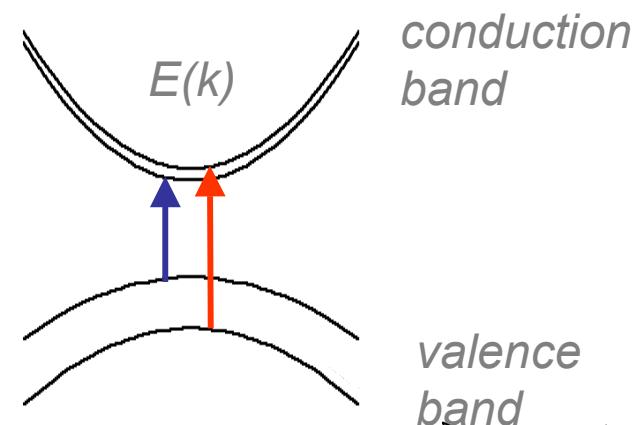
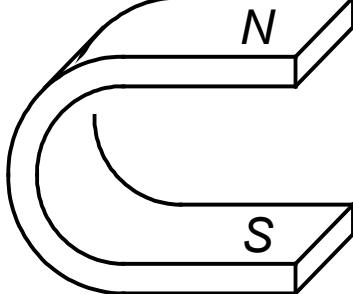


effective field proportional to magnetization (mean field approximation)

$$H = N_0 \alpha x \langle \mathbf{S} \rangle \cdot \boldsymbol{\sigma}_c$$

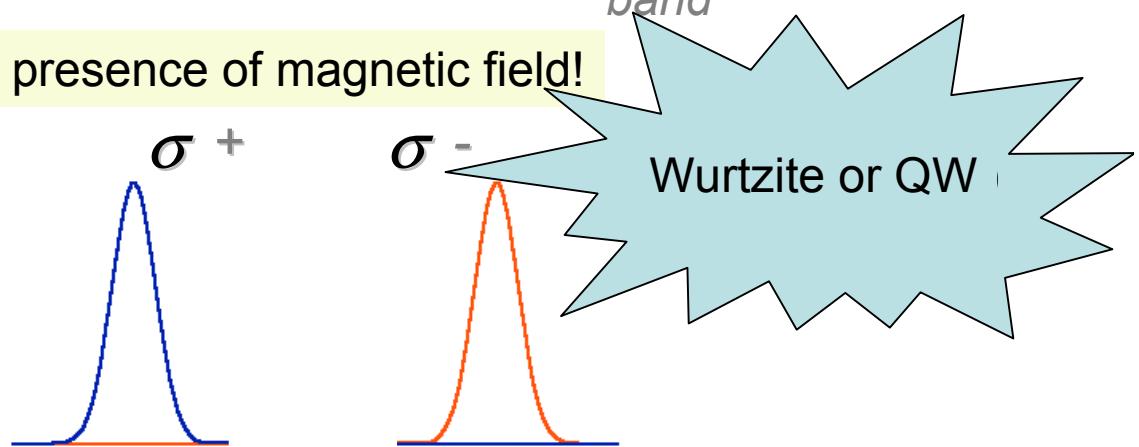
$$H = N_0 \beta x \langle \mathbf{S} \rangle \cdot \boldsymbol{\sigma}_v$$

# Diluted magnetic semiconductor



approximation: wavevector in presence of magnetic field!

- *excitonic absorption spectrum*

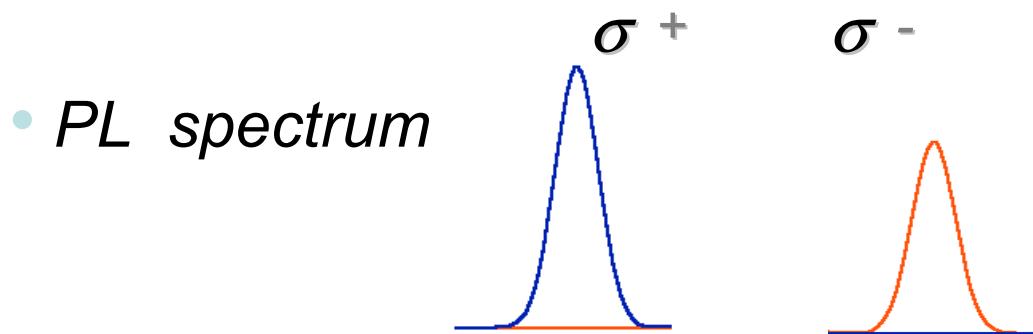
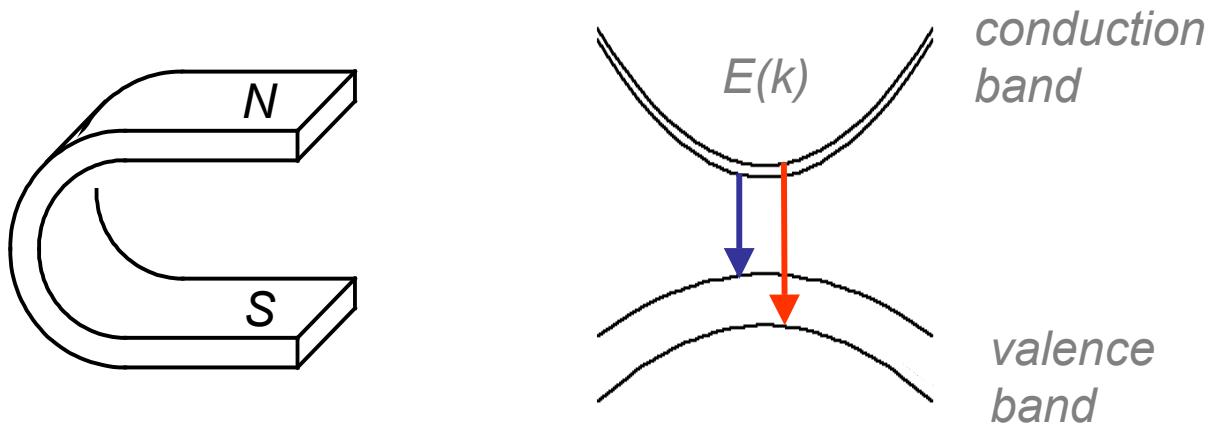


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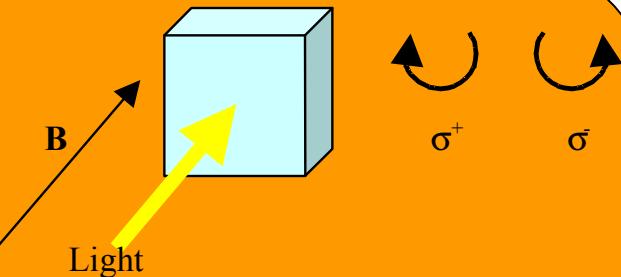
$$H = N_0 \beta x \langle \mathbf{S} \rangle \cdot \boldsymbol{\sigma}_v$$

# Photoluminescence polarization

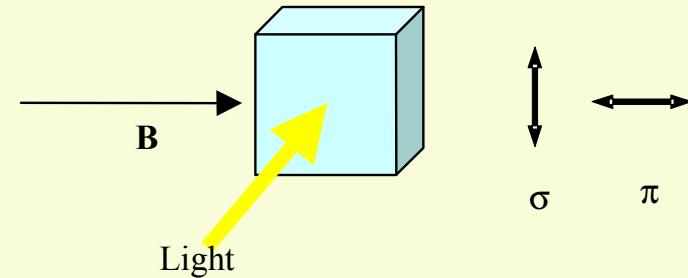


$$I_+/I_- = N_\uparrow/N_\downarrow \quad \text{valid also without magnetic field!}$$

# Various configurations

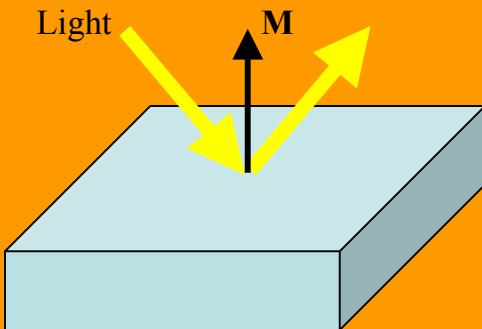


**Faraday**



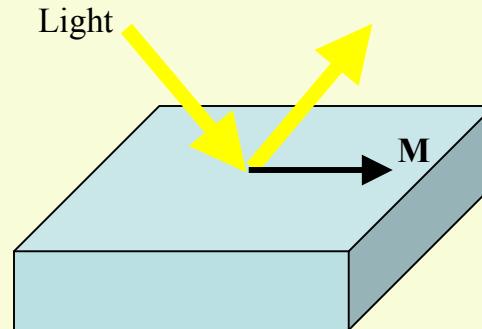
**Voigt**

Our main interest

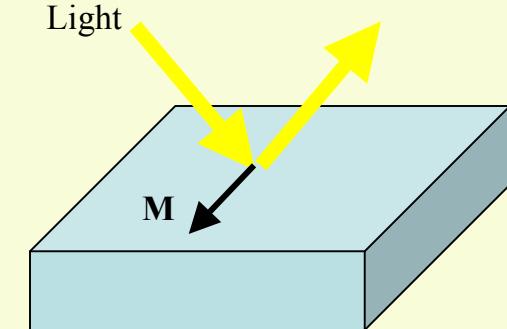


**polar**

**Identical at normal incidence**



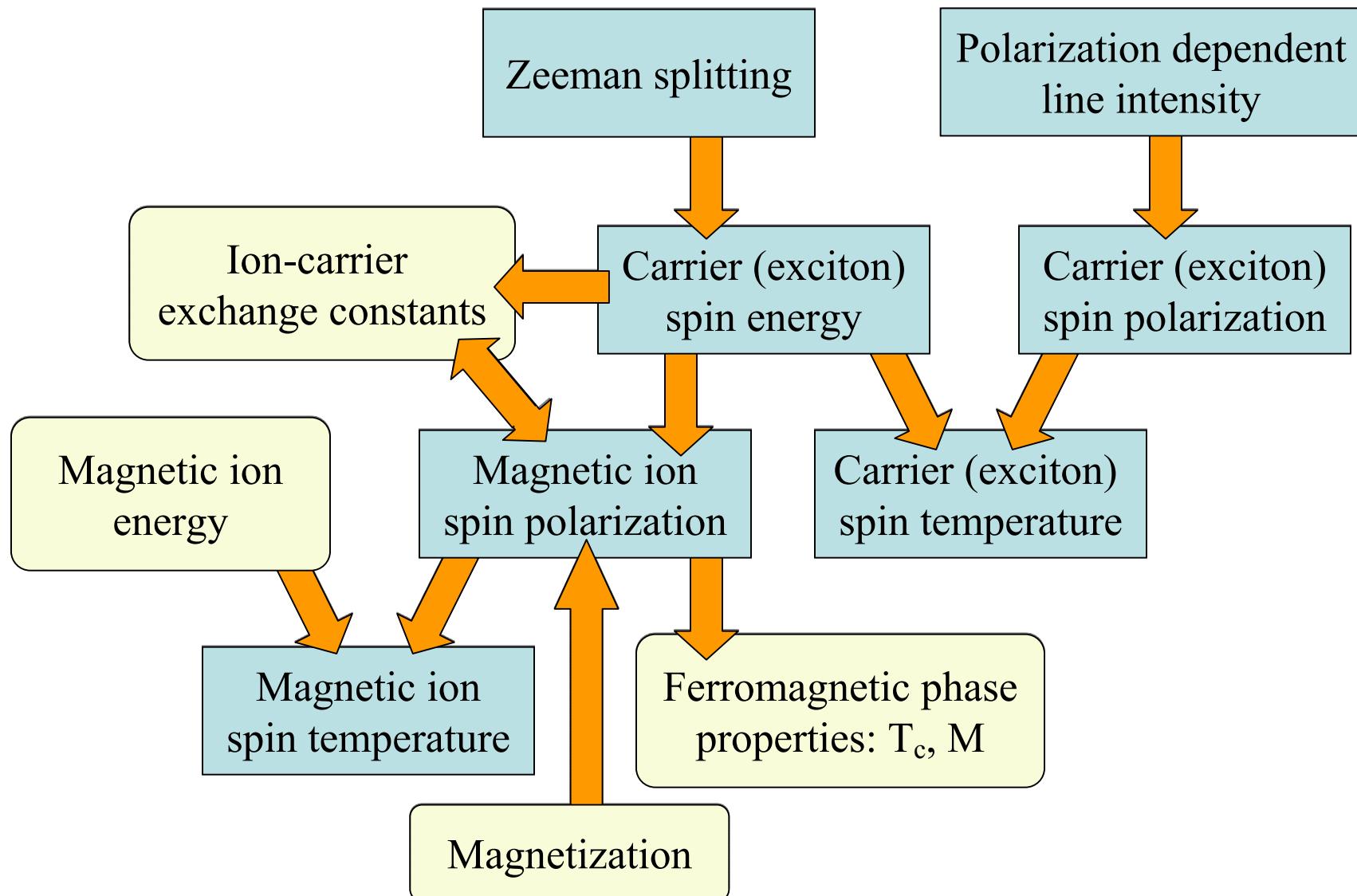
**longitudinal**



**transverse**

See, e.g., Chun-Yeol You and Sung-Chul Shin, Appl. Phys. Lett. **69**, 1315 (1996).

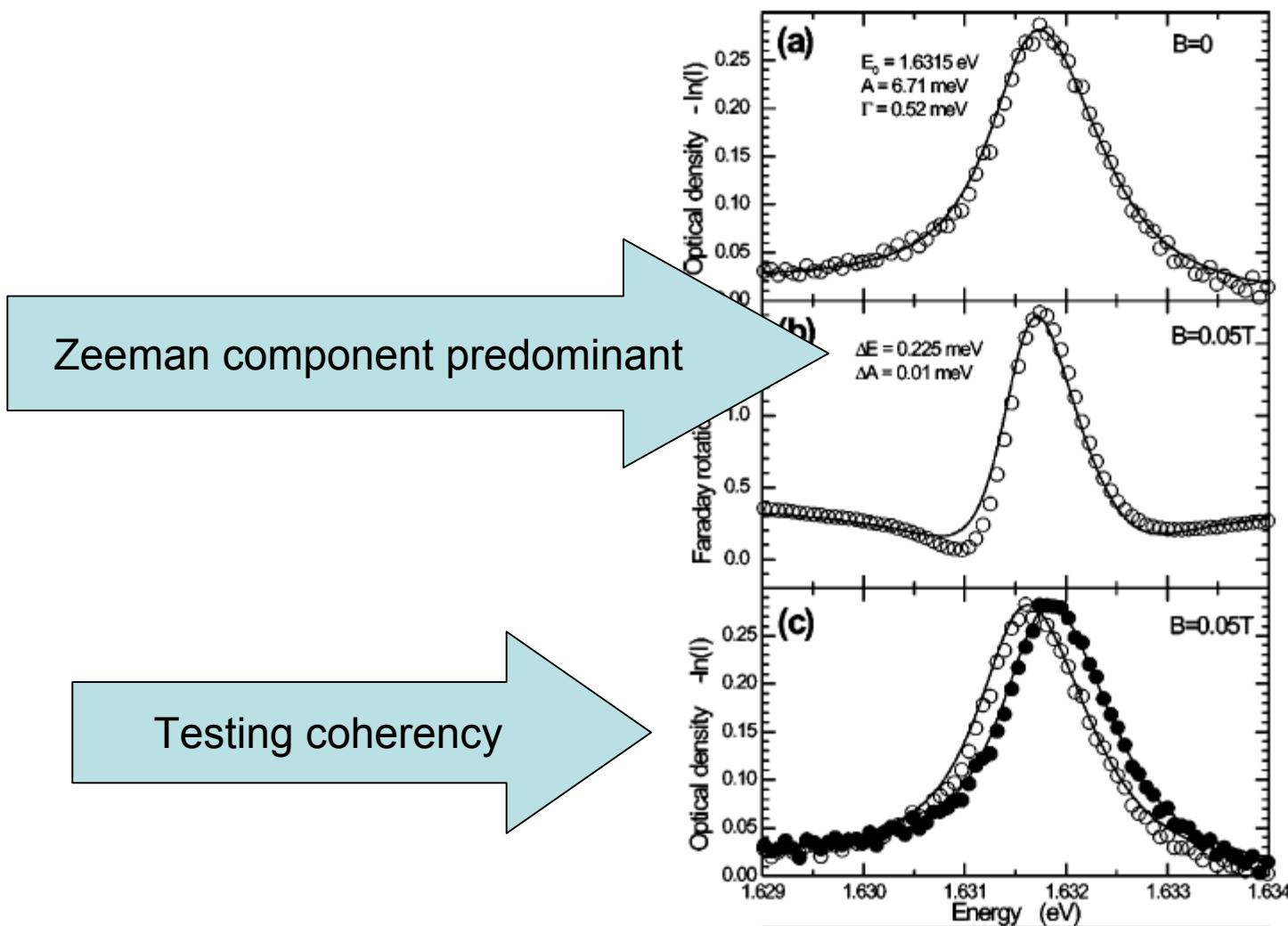
# Information from interband magneto optics



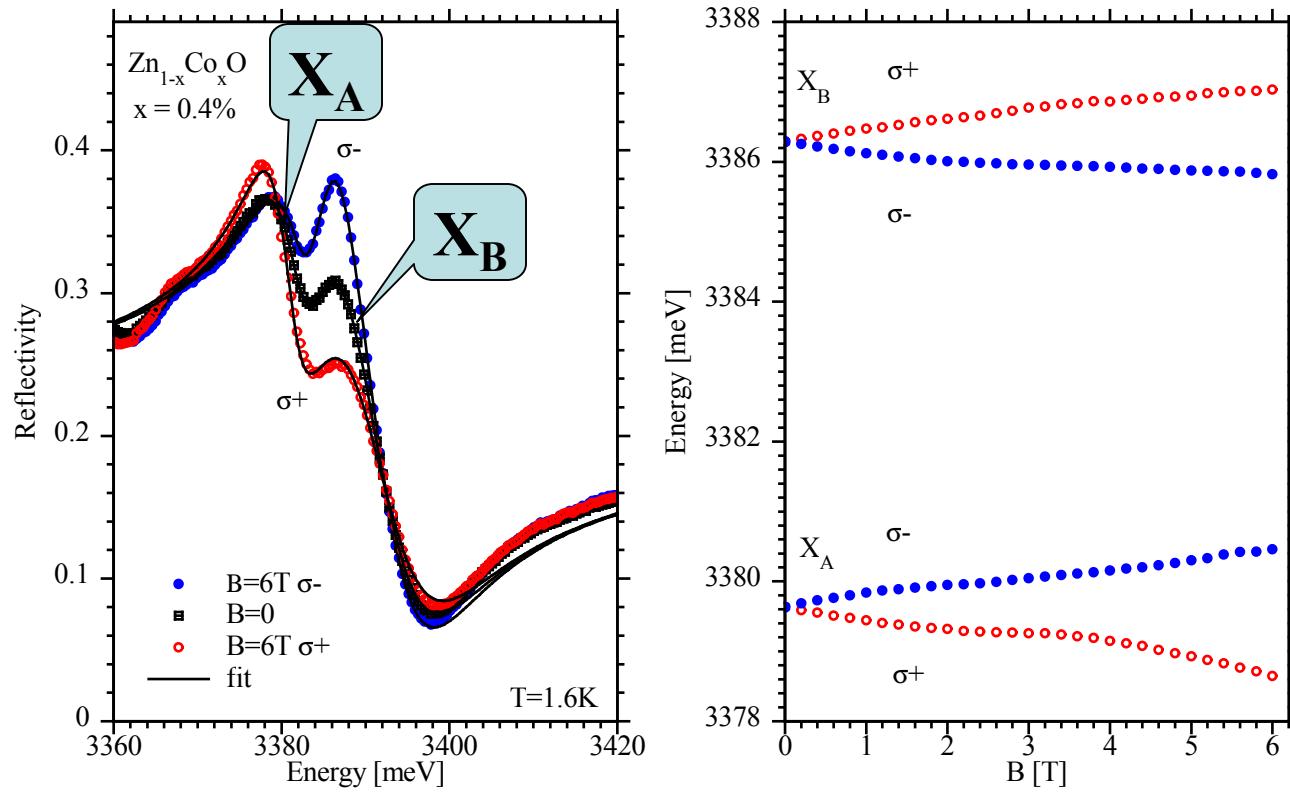
# Selected examples

Looking at spins

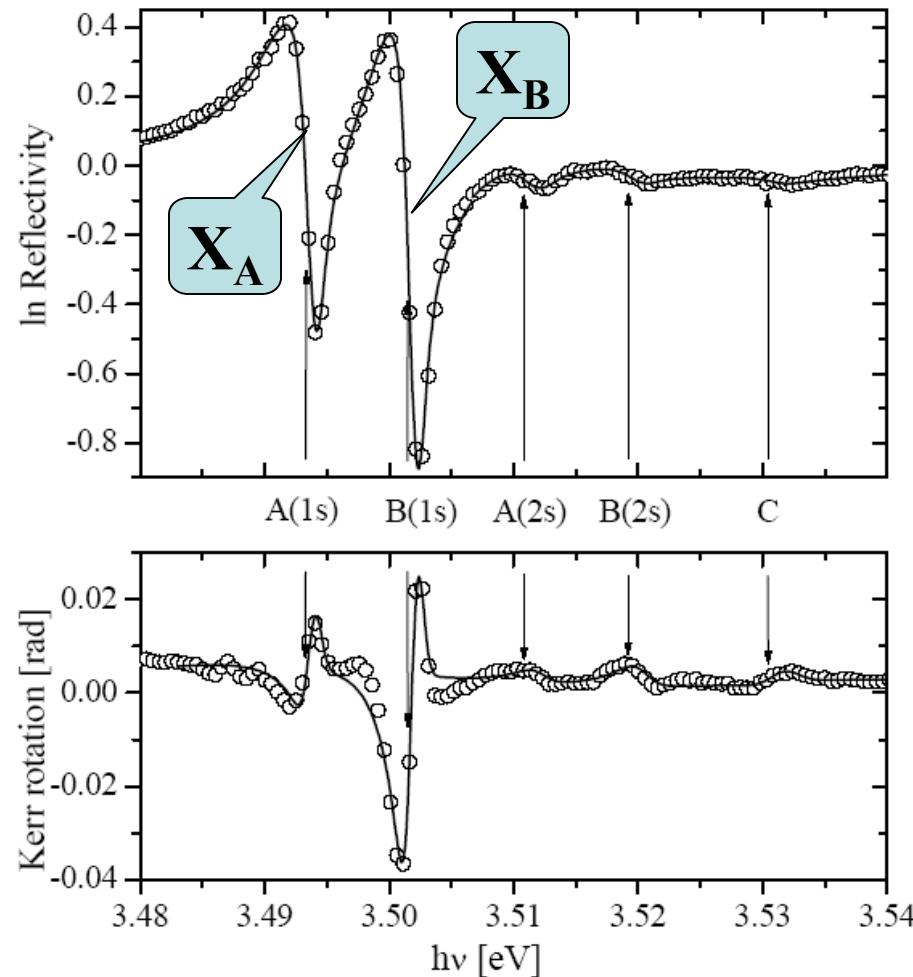
# Zeeman effect from Faraday rotation exciton line in a (Cd,Mn)Te QW



# Zeeman splittings of excitons in $(\text{Zn},\text{Co})\text{O}$ from reflectivity



# Zeeman effect of excitons in a GaN layer from Kerr rotation

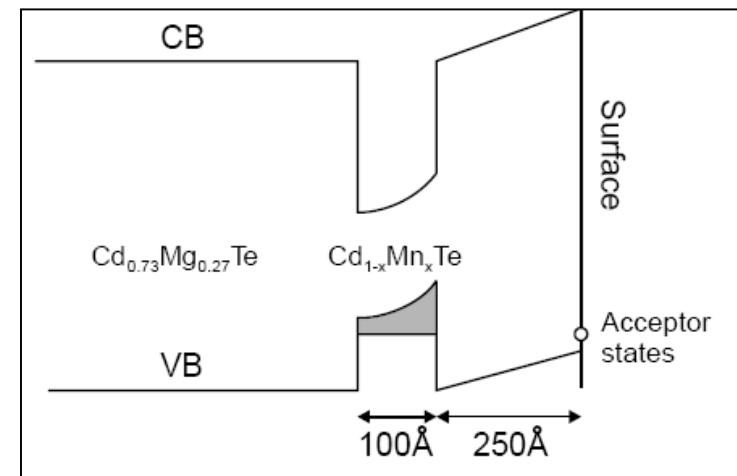
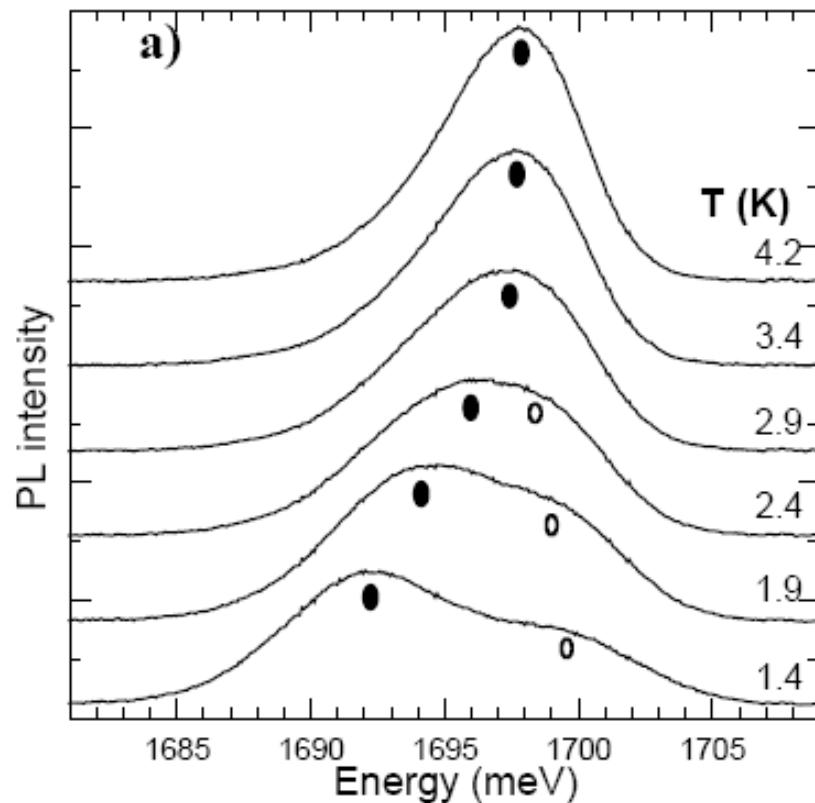


Exciton splittings at 6T  
from fit of Kerr rotation

A: 0.09 meV

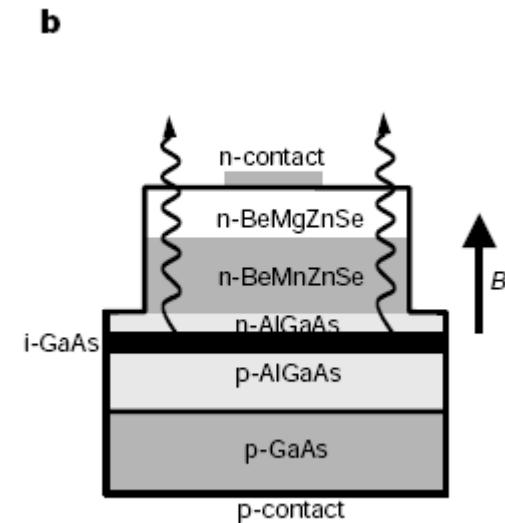
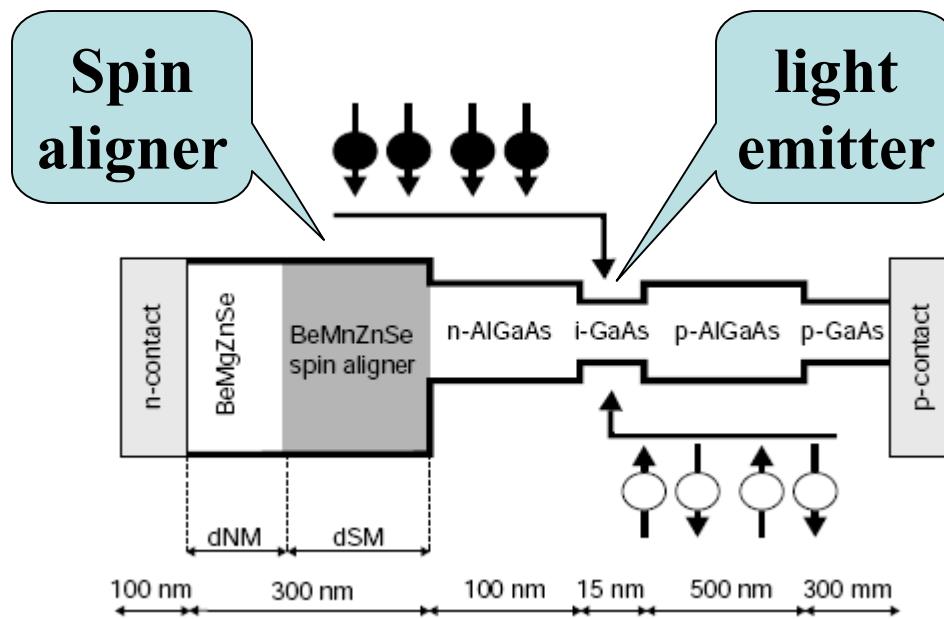
B: 0.16 meV

# Spontaneous magnetization in a ferromagnetic (Cd,Mn)Te QW from zero-field PL Zeeman splitting



Temperature dependence of zero field PL spectra  
for the surface-doped sample with 4.3% Mn in QW.  
The hole gas density is  $1.9 \times 10^{11} \text{ cm}^{-2}$ .

# Efficiency of electron spin injection into a GaAs QW

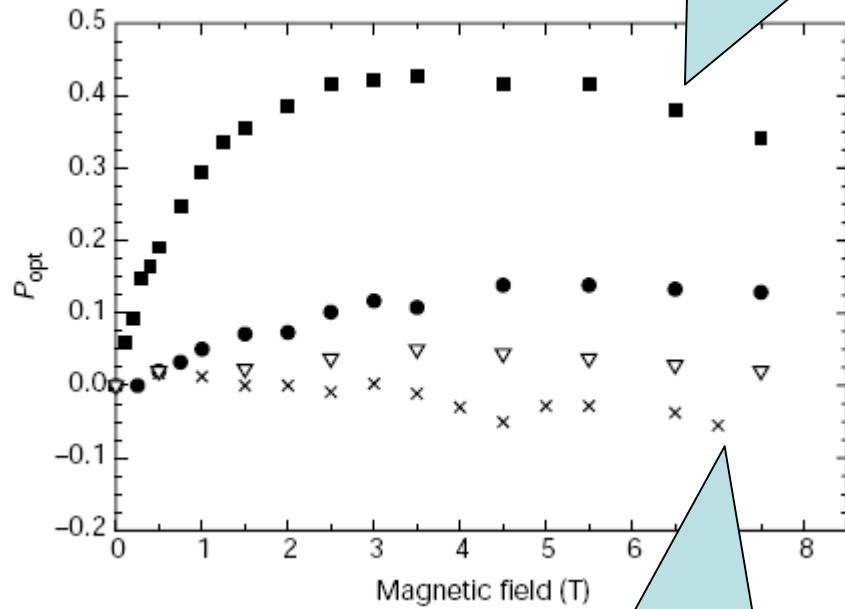


R. Fiederling et al., Nature 402, 787 (1999)

# Light → spin polarization

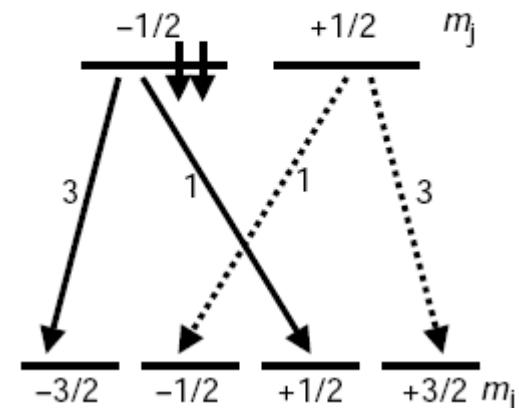
$$P_{opt} = \frac{I_+ - I_-}{I_+ + I_-}$$

Optimal parameters



GaAs ref. layer

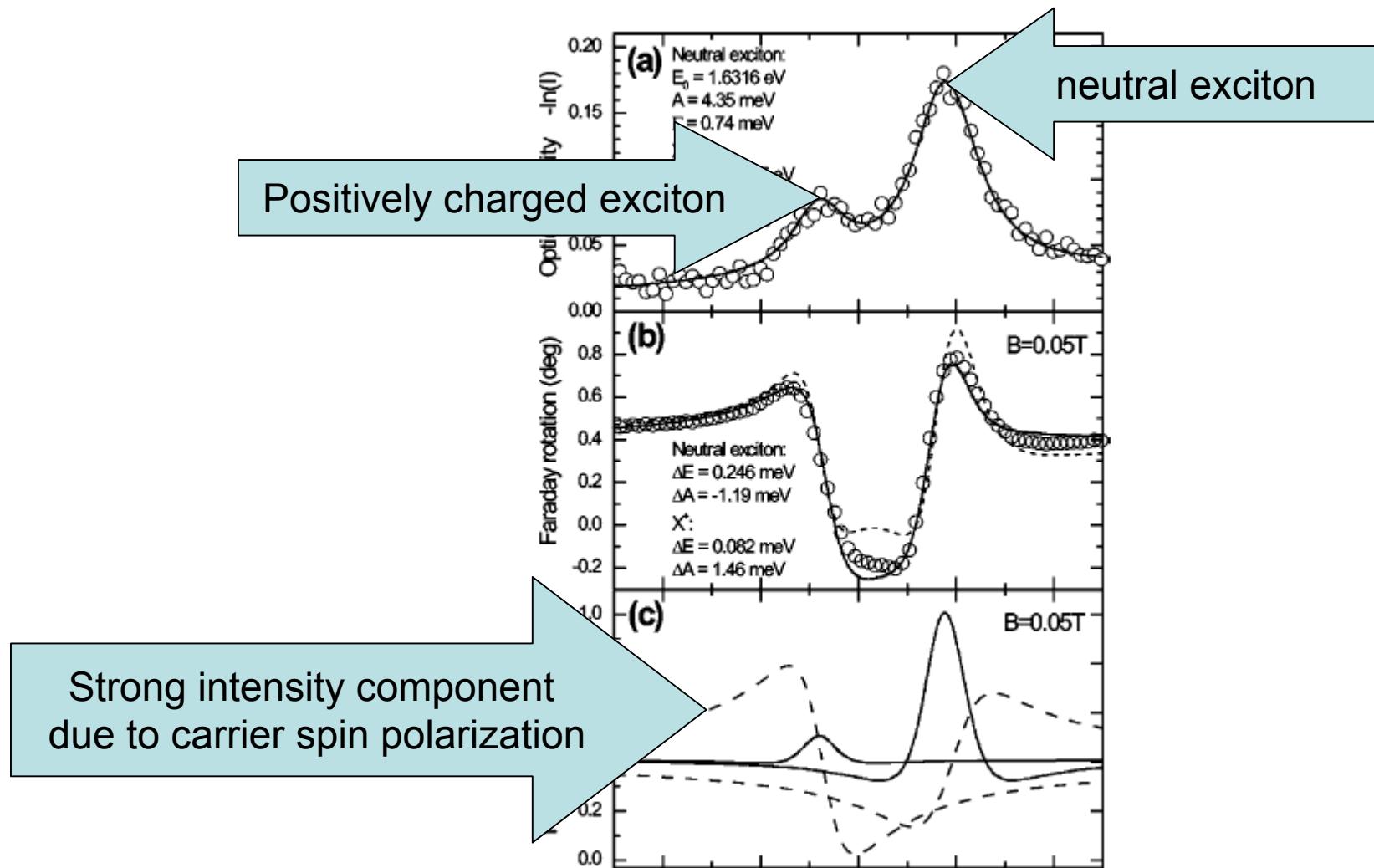
GaAs



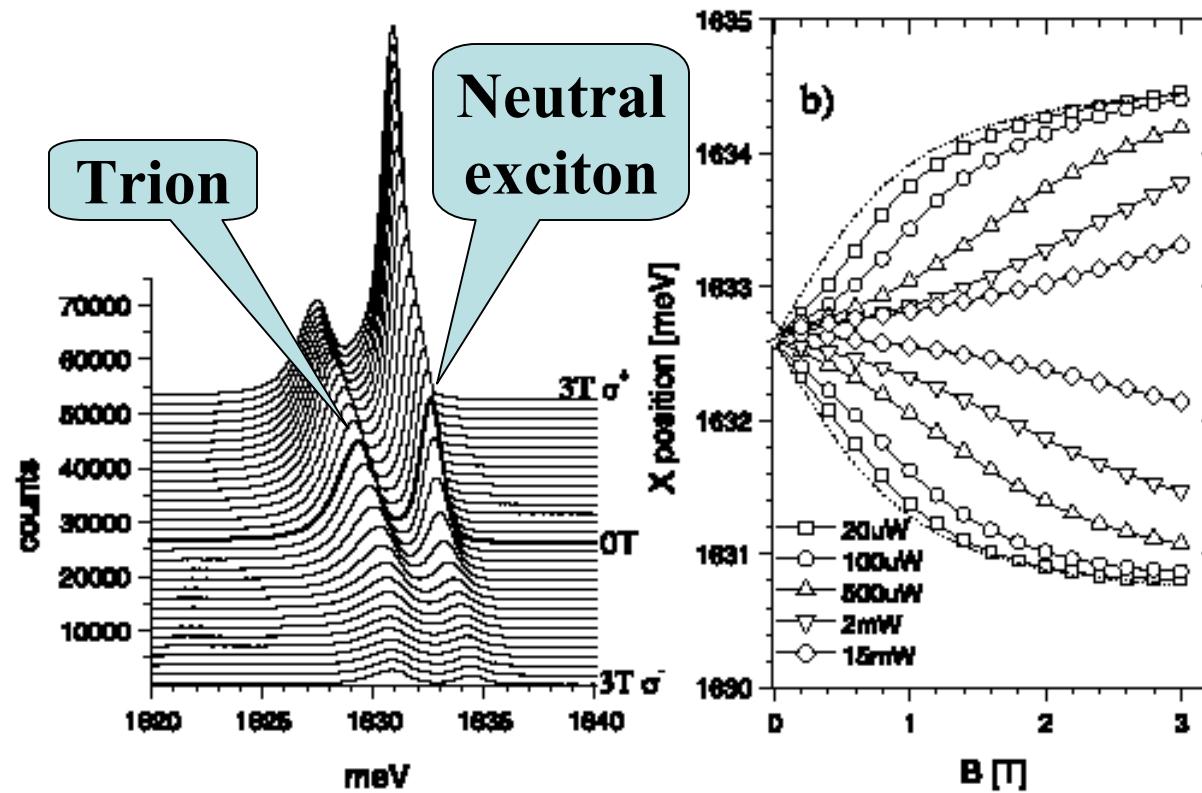
$$P_{opt} = \frac{(3n^\uparrow + n^\downarrow) - (3n^\downarrow + n^\uparrow)}{(3n^\uparrow + n^\downarrow) + (3n^\downarrow + n^\uparrow)}$$

3D zb case

# 2D hole gas spin polarization in a (Cd,Mn)Te QW

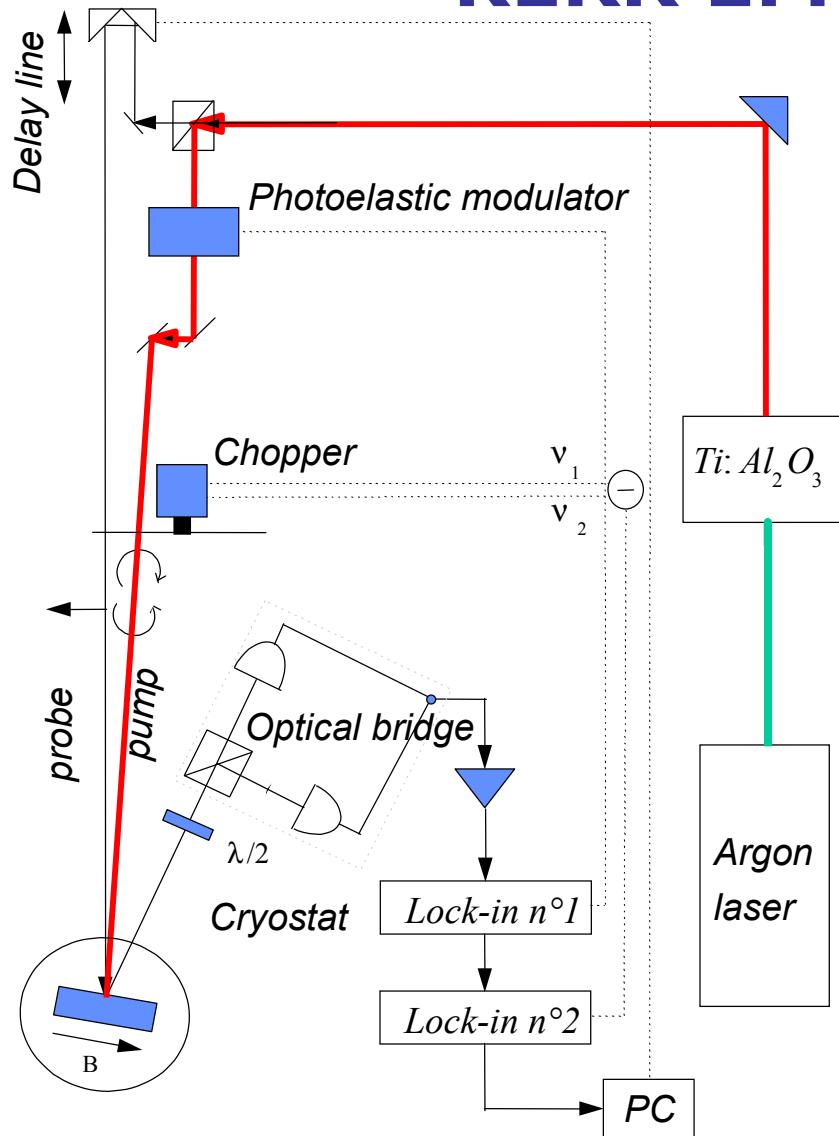


# Mn spin temperature in a (Cd,Mn)Te QW



(a) photoluminescence spectra in both circular polarizations at  $T = 1.6$  K and in magnetic field up to 3 T,  
(b) neutral exciton PL peak position versus magnetic field for indicated values of excitation power.  
Dotted line shows modified Brillouin function parameterization.

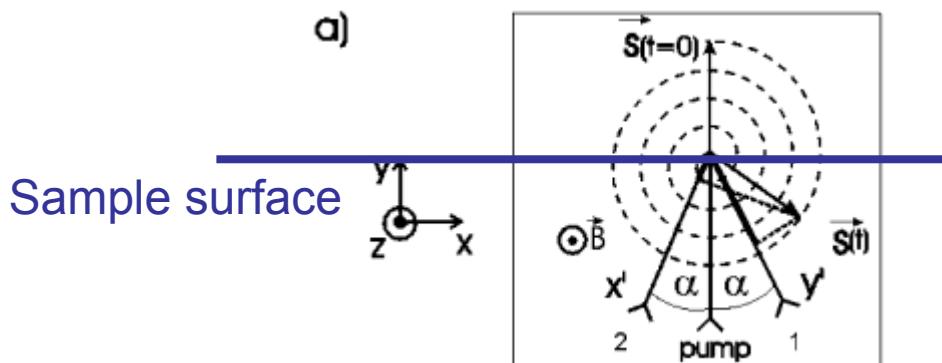
# TIME-RESOLVED MAGNETO-OPTICAL KERR EFFECT (TRMOKE)



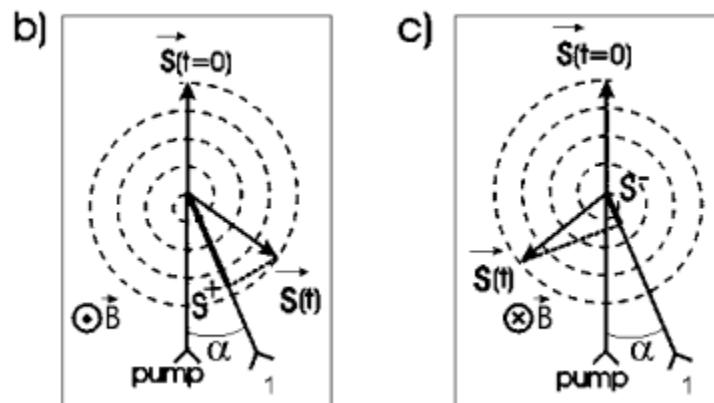
- Laser pulse: ~100 fs
- Total optical power: 3-8 mW
- Repetition rate: 82 MHz
- Magnetic field: 0 - 6T
- Temperature: 1.8-300K
- Angular resolution: 1'' ( $2.8 \times 10^{-4}$  deg)
- A.Y.Elezzabi, M.R.Freeman, M.Johnson, PRL 77, 3220 (1996) (0.1  $\mu$ rad)



# 2D spin imaging in n-doped CdTe

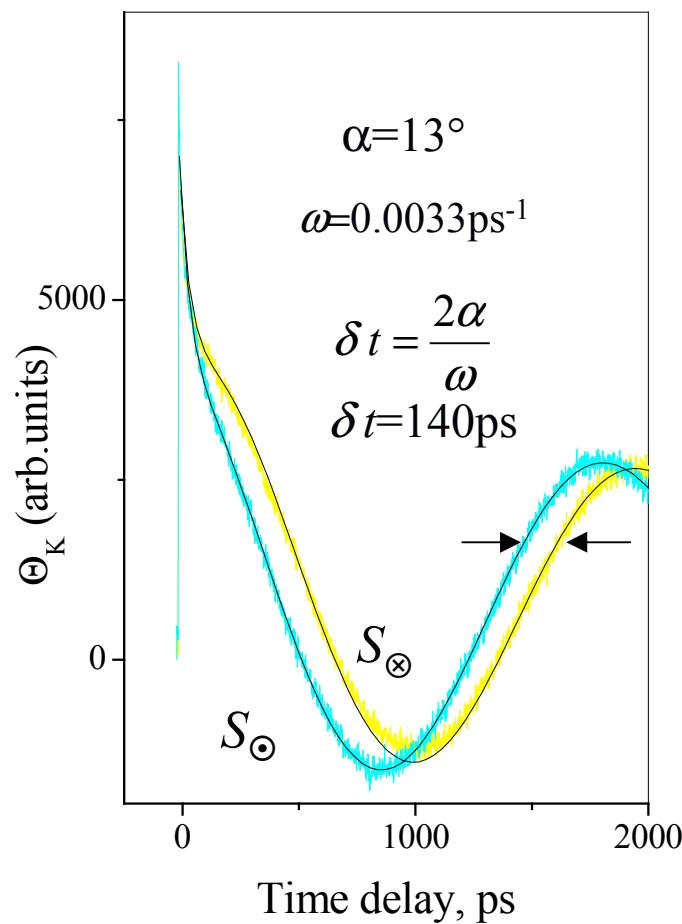


Two components of the spin vector measured through Kerr rotation along probe directions 1 and 2

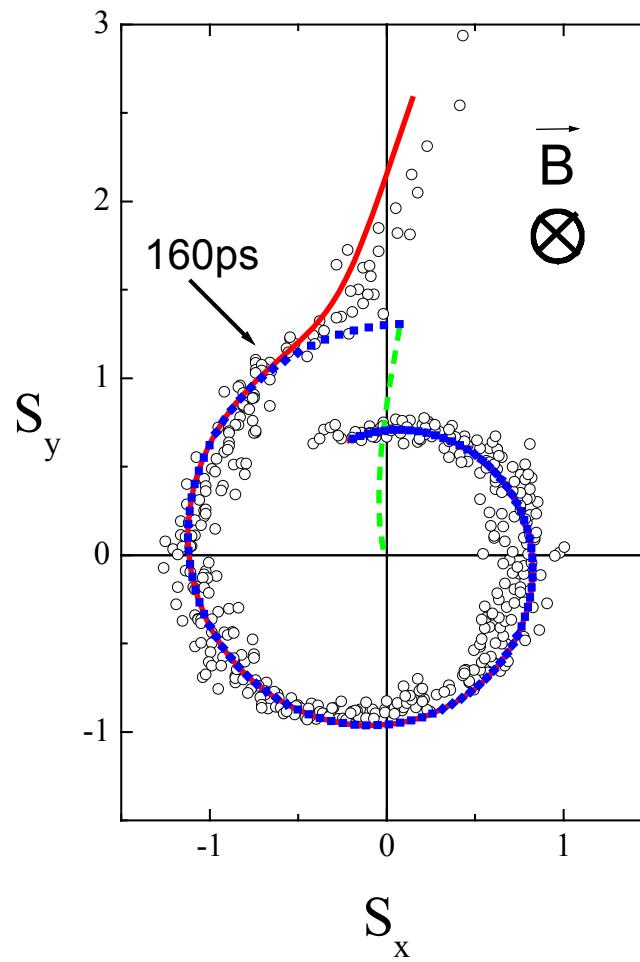


Instead of switching from direction 1 to 2, it is enough to reverse the magnetic field

# Imaging spin precession in 2D



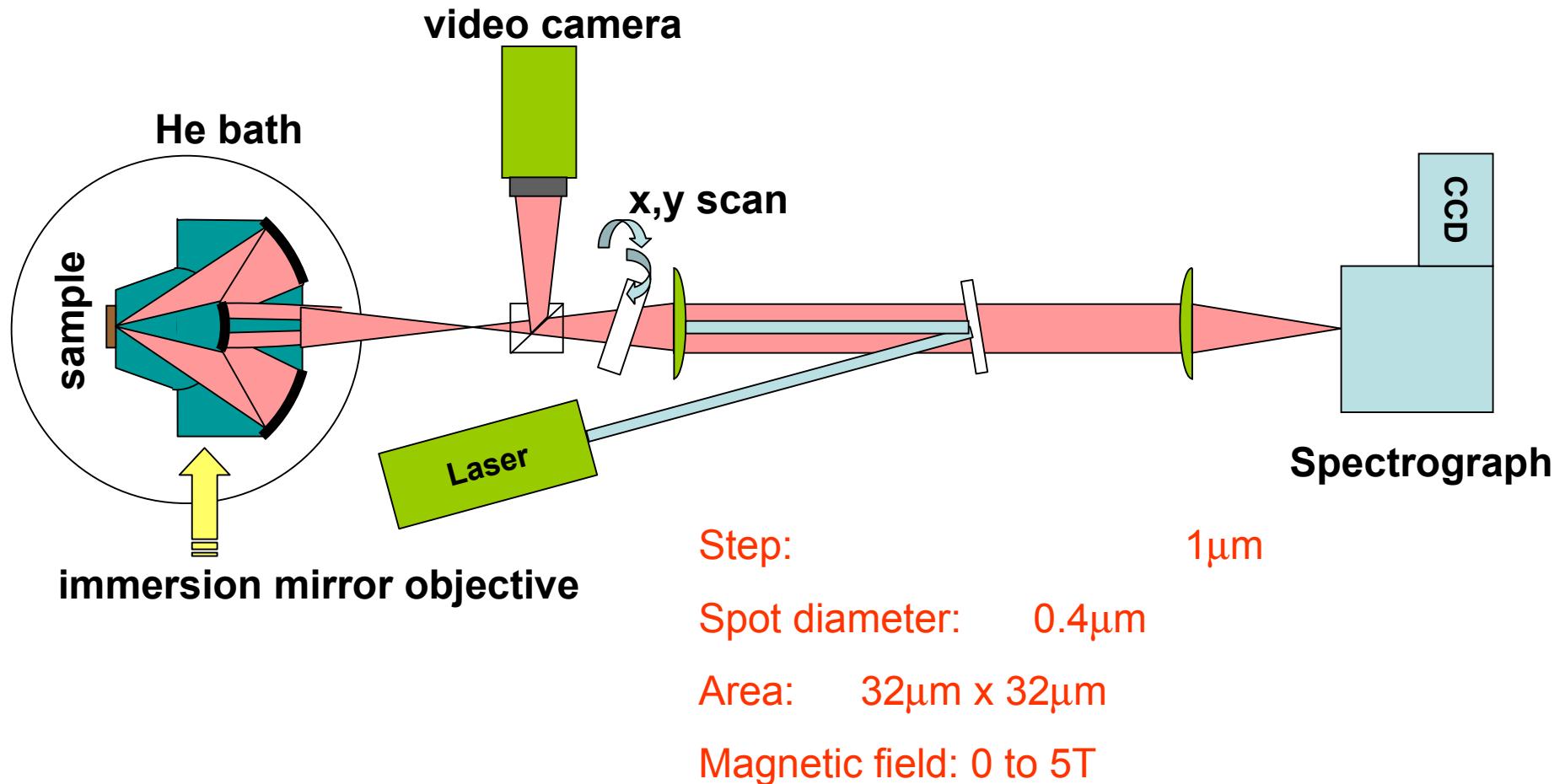
B=230G  
T=2K  
CdTe:Al.  
 $n_D = 8 \times 10^{16}$   
M1371



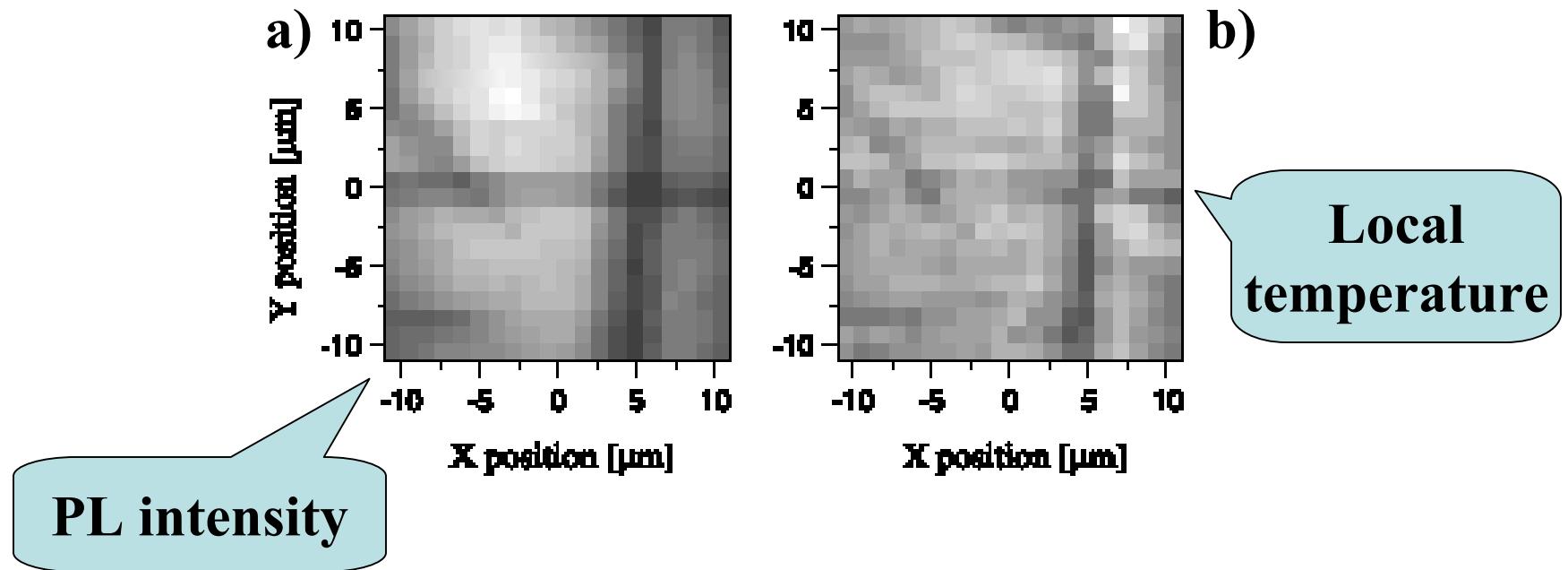
- Total spin polarization vector
- Donor-bound electron
- Free exciton

$$\Theta_K = \Theta_0 + \left( A \exp \frac{(t_0 - t)}{t_1} + B \exp \frac{(t_0 - t)}{t_2} \right) \cos(\omega(t - t_0) + \varphi)$$

# Microphotoluminescence mapping

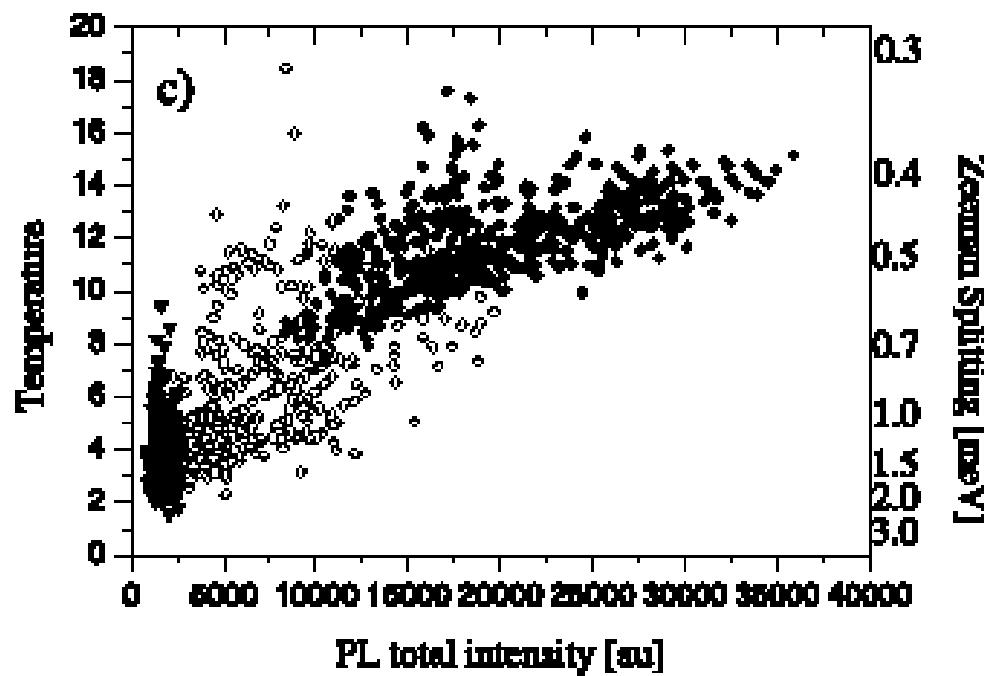


# Mapping of Mn spin temperature in a (Cd,Mn)Te QW



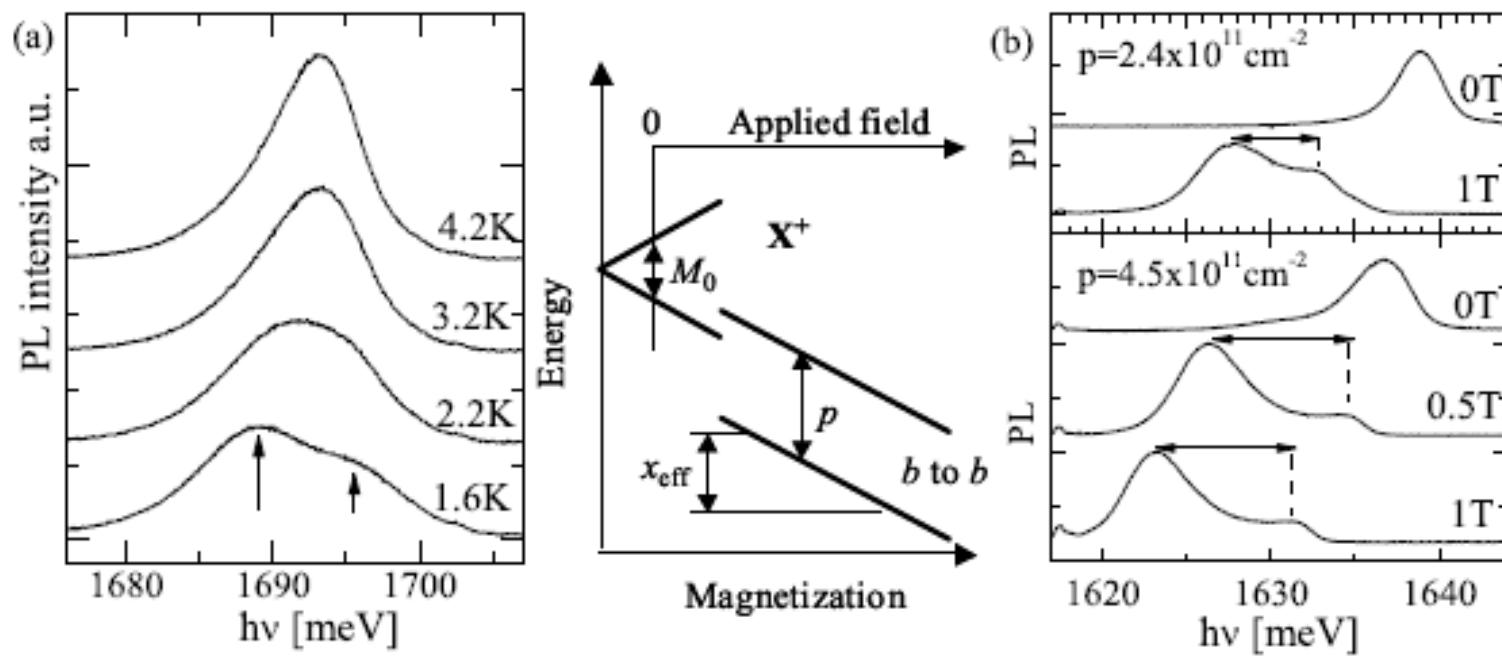
Maps of total PL intensity (a) and local temperature (b) measured with excitation photon energy 488 nm (excitation in the barrier). The helium bath temperature was 1.55 K. The scale of temperatures on (b) ranges from 1.5 K (black) to 18 K (white).

# Mapping of Mn spin temperature in a (Cd,Mn)Te QW



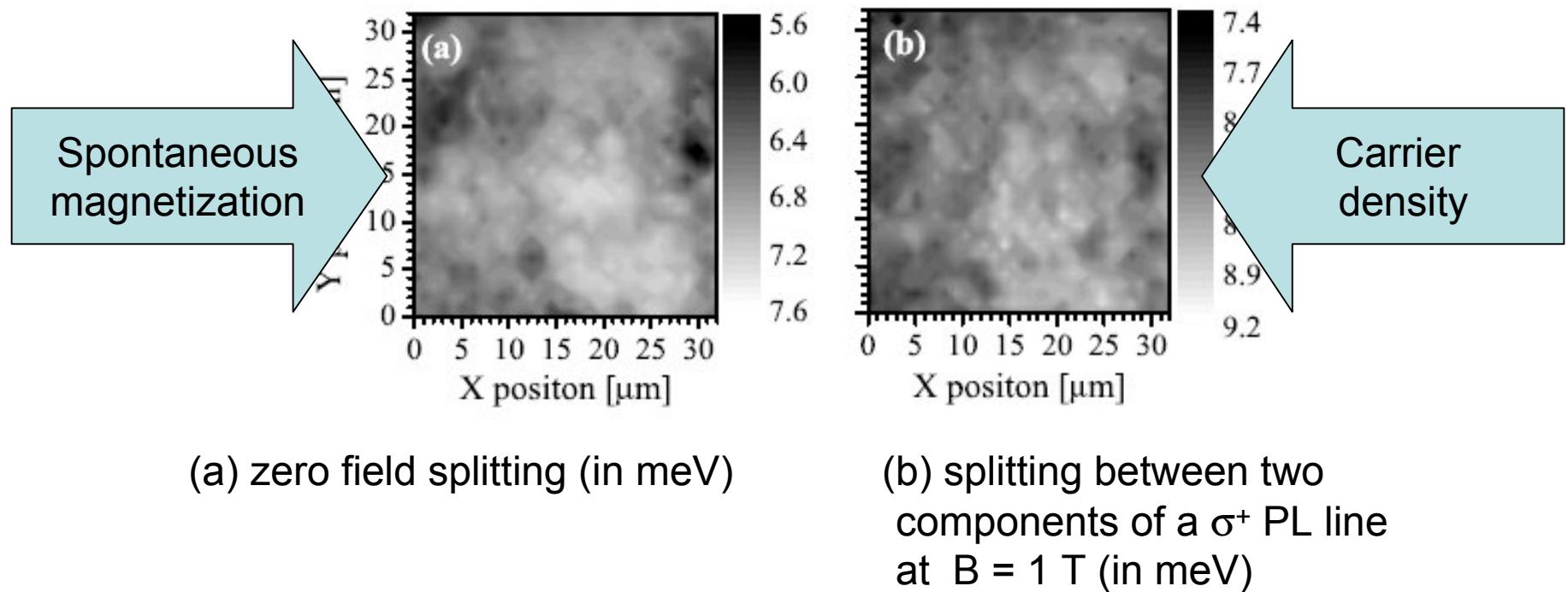
(c) Correlation of local temperature and PL intensity at different excitations:  
488 nm (in the barrier) - full symbols, 680 nm (in the QW) - open symbols.

# Ferromagnetic p-doped (Cd,Mn)Te QW determination of parameters

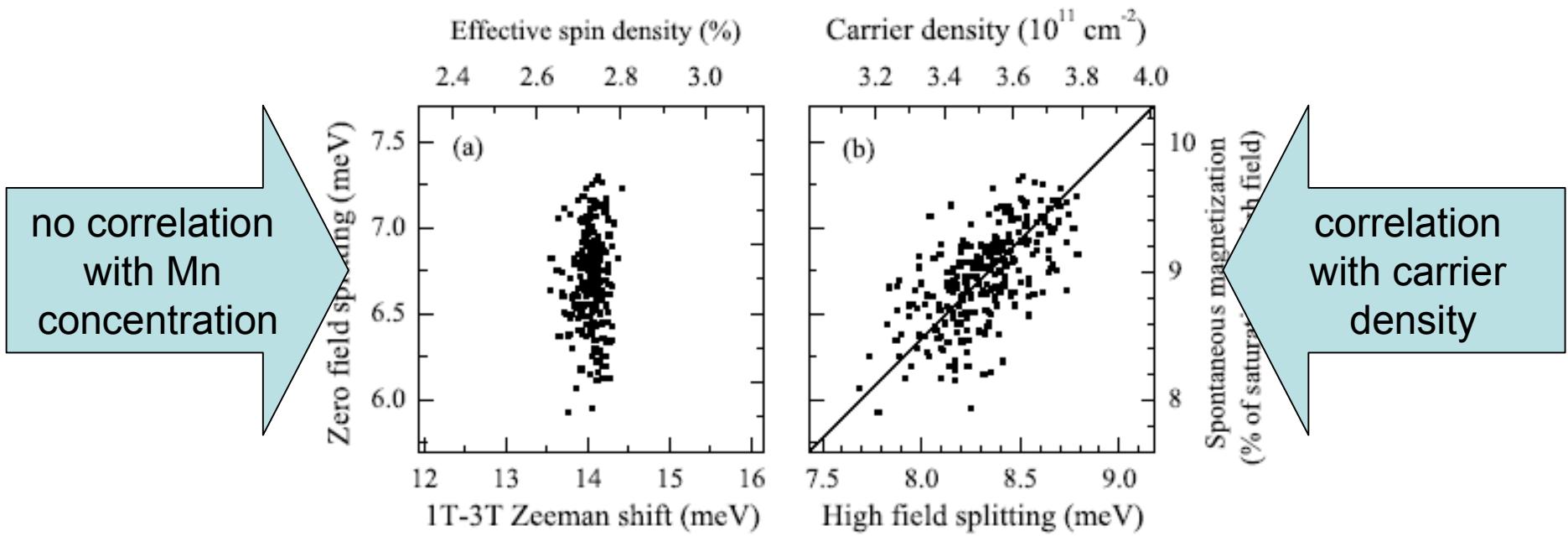


- (a) PL at zero field, from the sample with 4.65% Mn, at different temperatures. The arrows show the zero field splitting of the charged exciton ( $X^+$  in the central scheme) induced by the spontaneous magnetization  $M_0$ ;
- (b) PL from a QW with 1.4% Mn, at two values of the carrier density. The arrows on the double line (which is close to a band to band transition, b to b in the central scheme) indicate the splitting used to measure the carrier density.

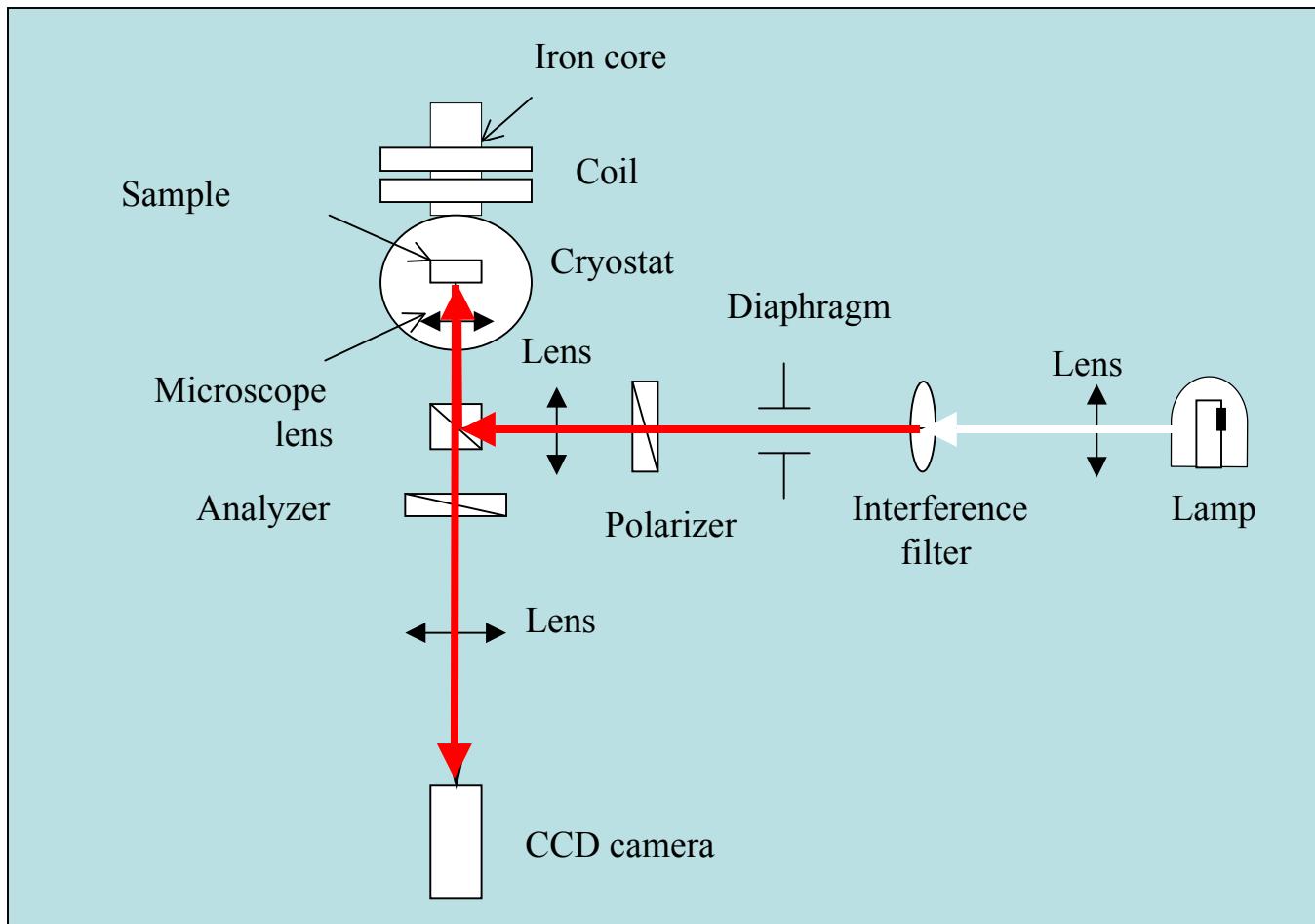
# Ferromagnetic p-doped (Cd,Mn)Te QW maps of parameters



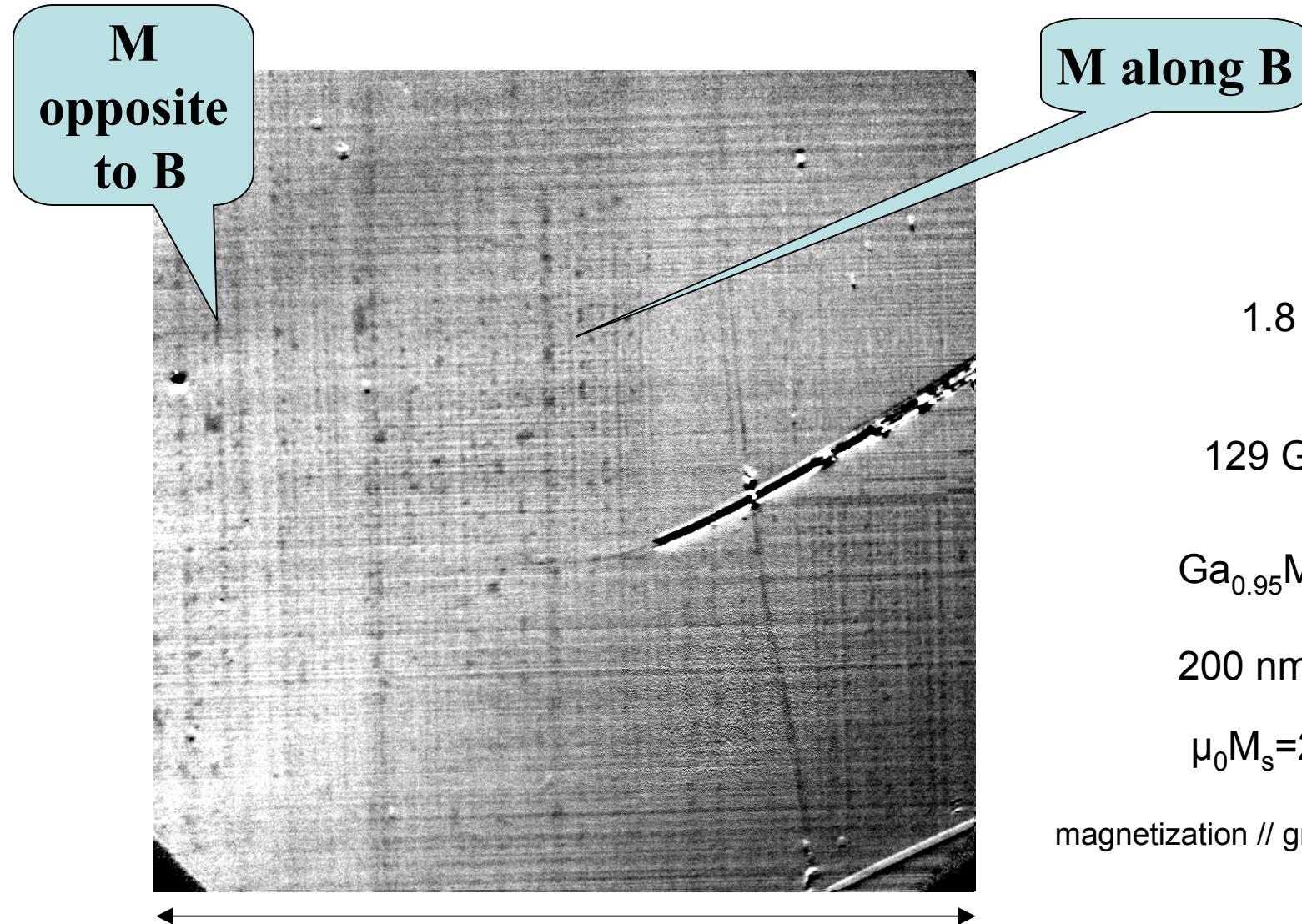
# Ferromagnetic p-doped (Cd,Mn)Te QW correlation of parameters



# Mapping of ferromagnetic domains



# Ferromagnetic domains in (Ga,Mn)As



1.8 K

129 G to 156 G

$\text{Ga}_{0.95}\text{Mn}_{0.05}\text{As}$

200 nm

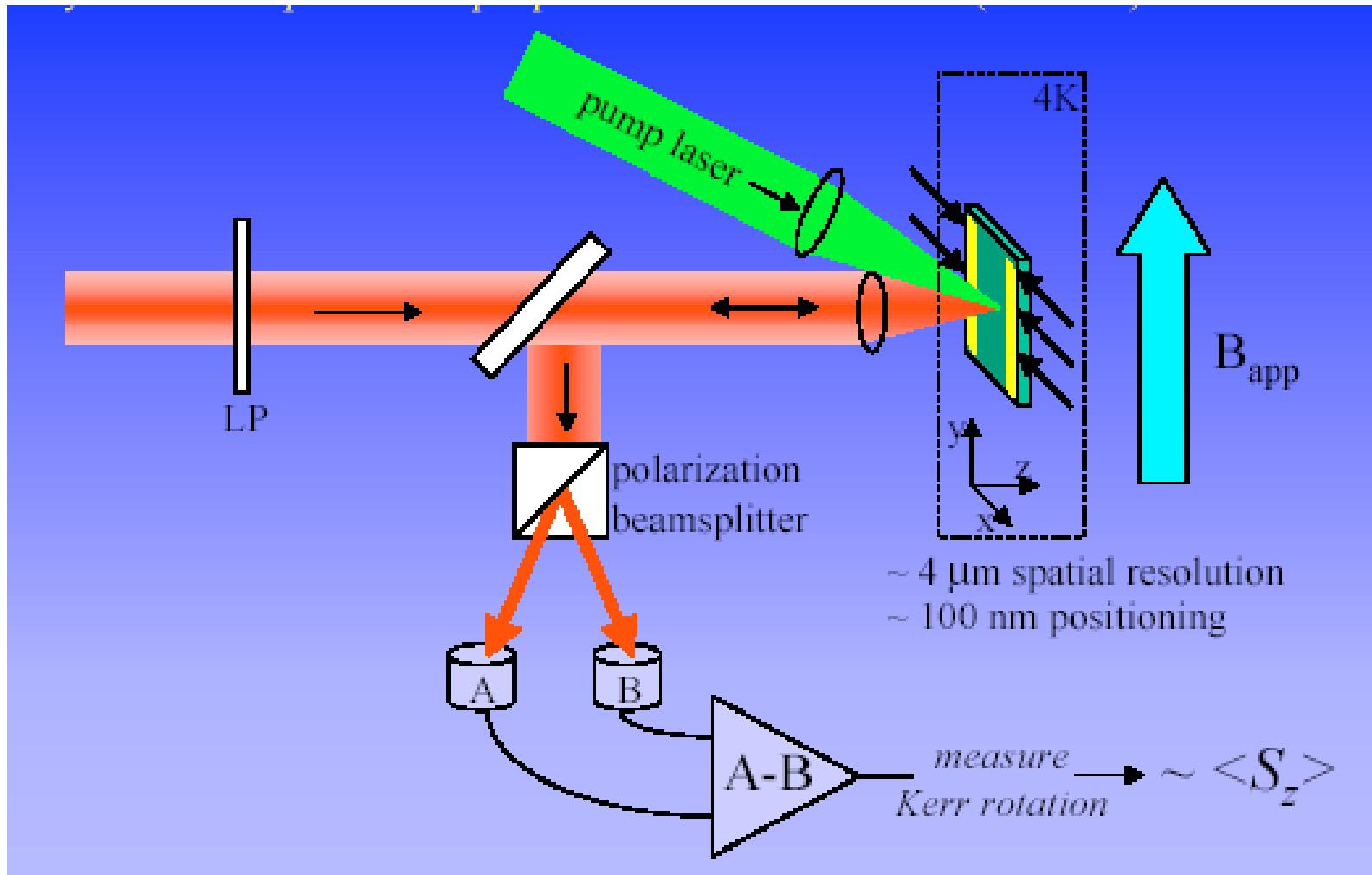
$\mu_0 M_s = 230 \text{ G}$

magnetization // growth axis

500 μm

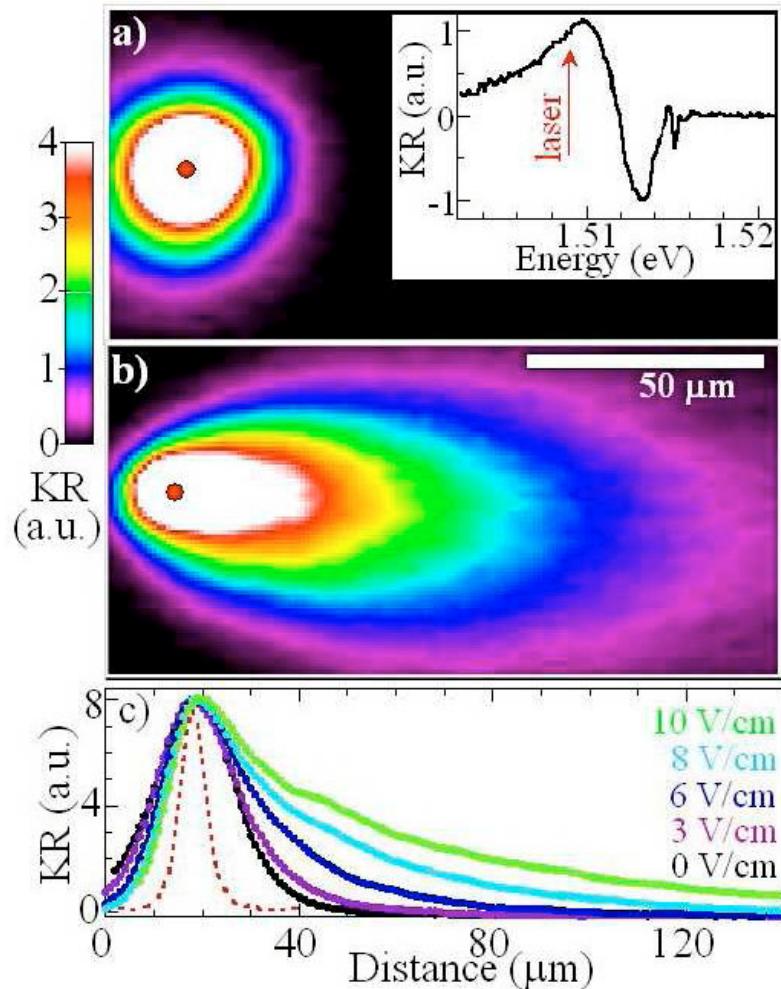
C. Gourdon INSP Paris 2005

# Spin flow imaging in n-GaAs



S. A. Crooker and D. L. Smith, PRL 94, 236601 (2005)

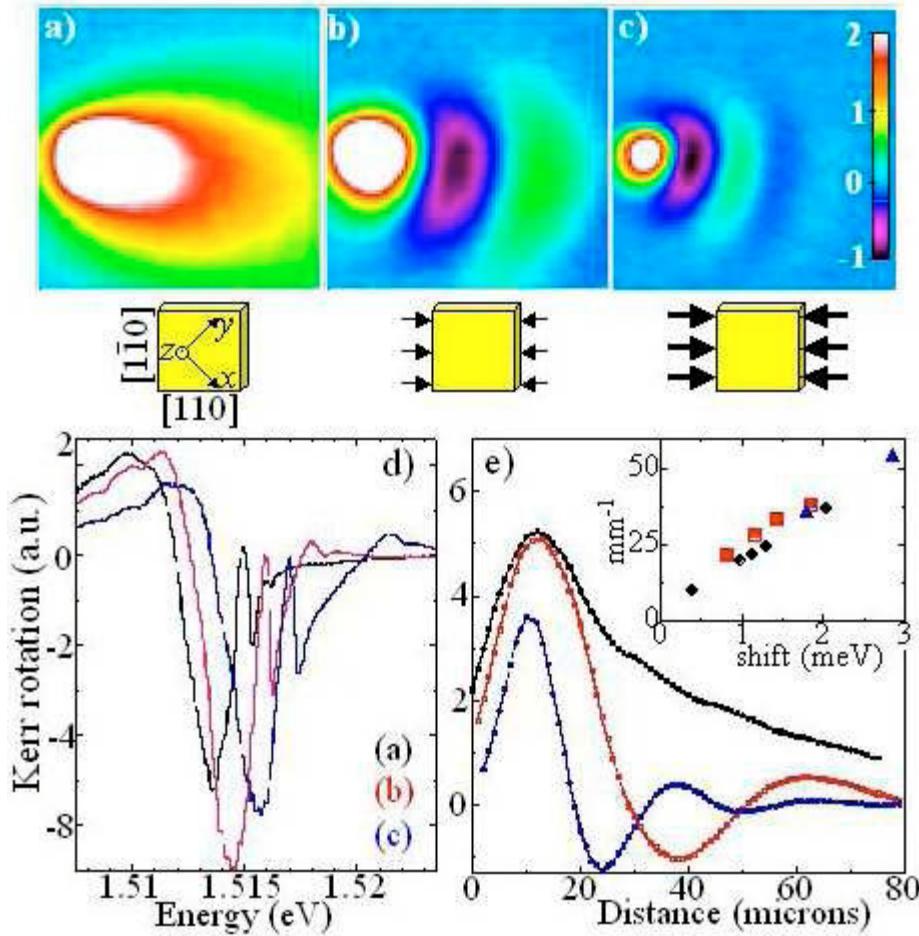
# Spin flow imaging by Kerr rotation



- Spin diffusion
- Spin drift and diffusion

S. A. Crooker and D. L. Smith, PRL **94**, 236601 (2005)

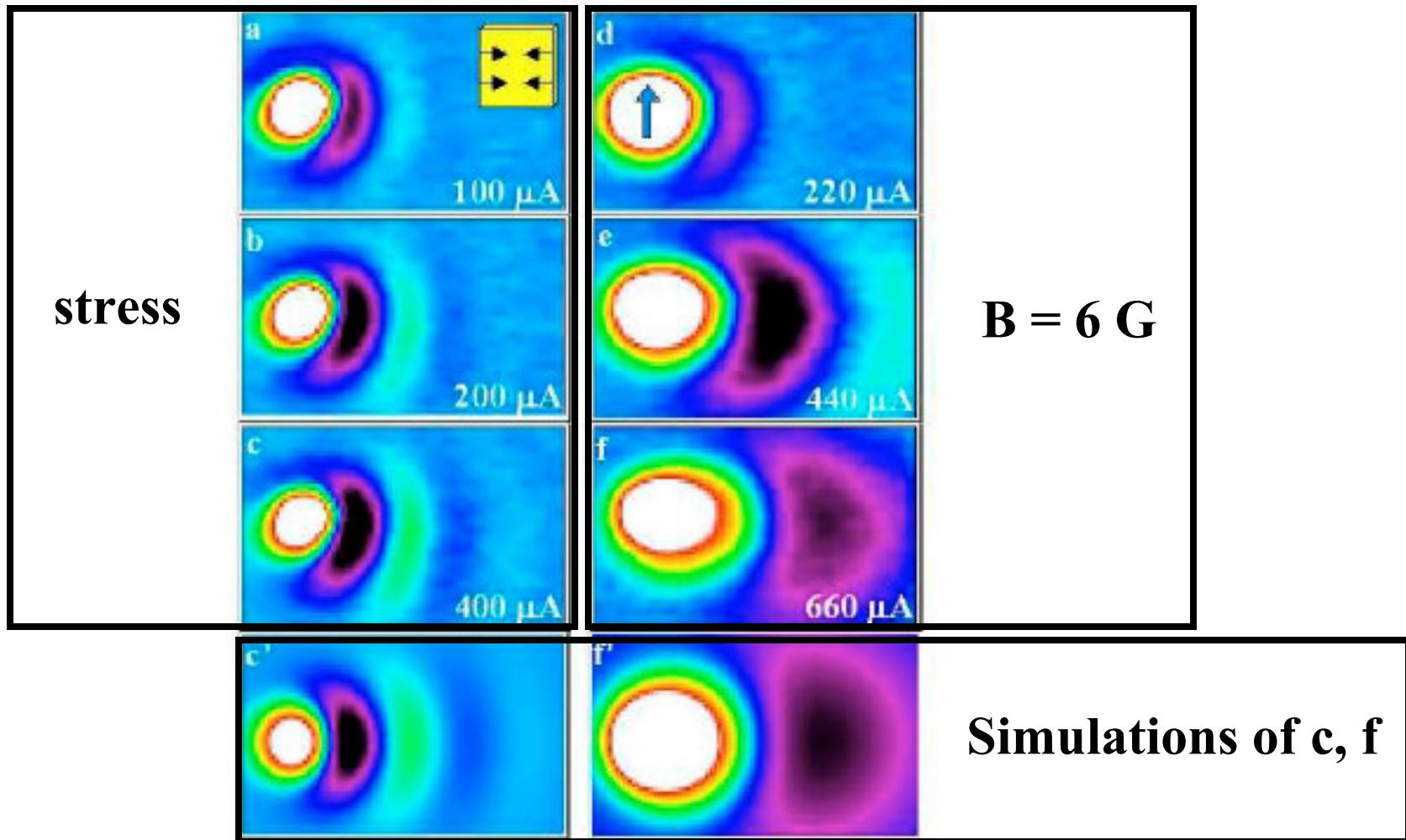
# Uniaxial stress



$H_S = c_3 \sigma \cdot \varphi$ ,  
where  $\varphi \propto |\mathbf{k}|$   
depends on shear strain;

$H_S$  has similar symmetry  
to Rashba Hamiltonian  
 $H_R \propto \sigma \cdot (\mathbf{k} \times \mathbf{E}_z)$

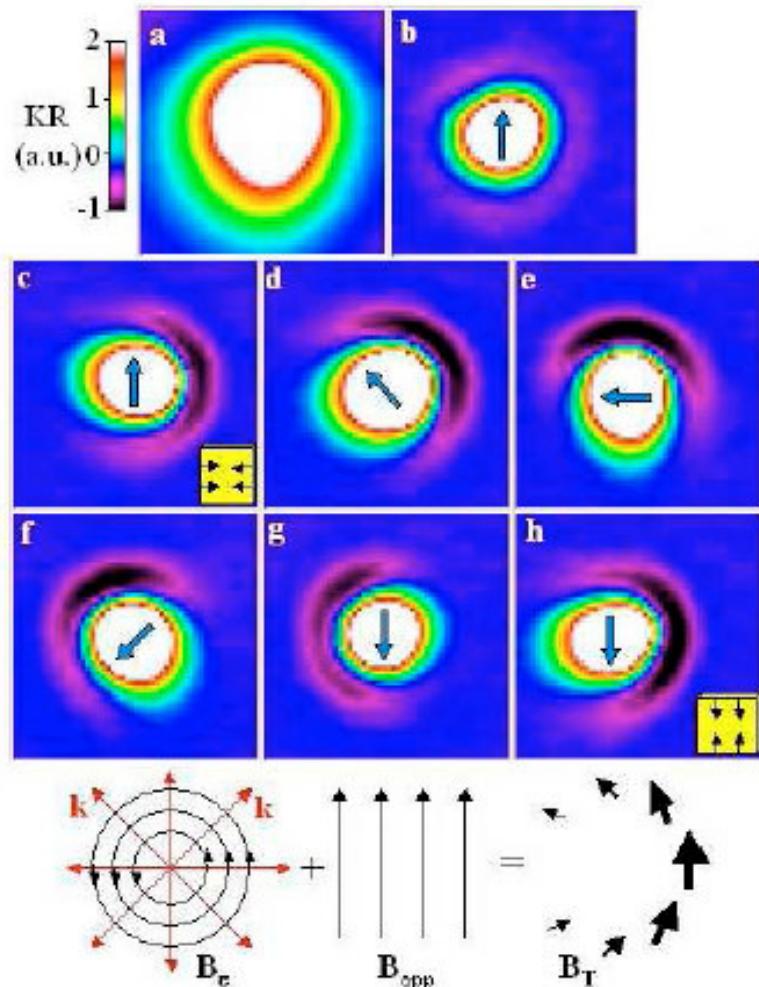
# Stress compared with magnetic field



50 $\times$ 80  $\mu\text{m}$  images of 2D spin flow at 4K with increasing  $|\mathbf{k}|$  (current)

S. A. Crooker and D. L. Smith, PRL **94**, 236601 (2005)

# Stress combined with magnetic field



50×50  $\mu\text{m}$  images of 2D spin diffusion ( $E=0$ ) at 4K.

- (a) Stress=0,  $B_{\text{app}}=0$ .
- (b) Stress=0,  $B_{\text{app}}=16$  G oriented along [1-10] as shown.
- (c)  $B_{\text{app}}=16$  G, with [110] uniaxial stress. Spins diffusing to the right precess, while those diffusing to the left do not. Thus  $B_\varepsilon$  is chiral for radially-diffusing electrons (see diagram).
- (d-g) Maintaining [110] stress,  $B_{\text{app}}$  is rotated by 180 degrees in-plane.
- (h) Stress is switched to [1-10], reversing chirality of  $B_\varepsilon$ .

# Conclusions

- Magneto optics enables us to see spins of carriers and magnetic ions in bulk semiconductors and quantum structures
- Spin energy, polarization, temporal evolution and spatial distribution can be measured
- Parameters related to spin can be determined, such as g-factor, relaxation time, diffusion length, ion-carrier coupling constants, Curie temperature, etc.

