



## Computer Tools for Nuclear Physics

# Microscopic Transport Models (outline)

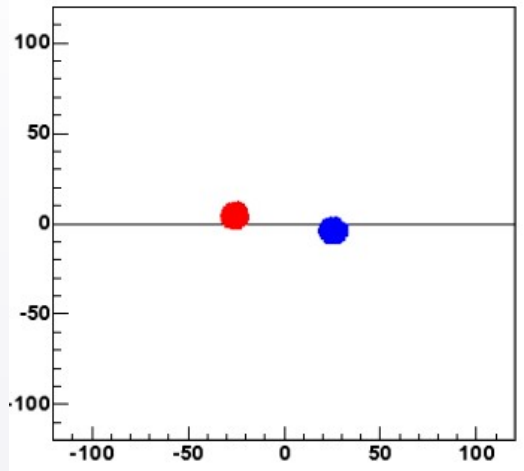
Krzysztof Piasecki

1. Choice of kinematics. Adequate degrees of freedom.
2. Energy of nucleus and nuclear matter
3. BUU transport equation. Cascade approach.
4. QMD family. Interactions between nucleons
5. Soft QCD (strings): LUND model within PYTHIA
6. Summary of model properties and additional info
7. Interlude: parsing text files, managing processes on Linux
8. Characteristics of selected transport models:  
GiBUU, UrQMD, SMASH, PHSD, JAM2/RQMD



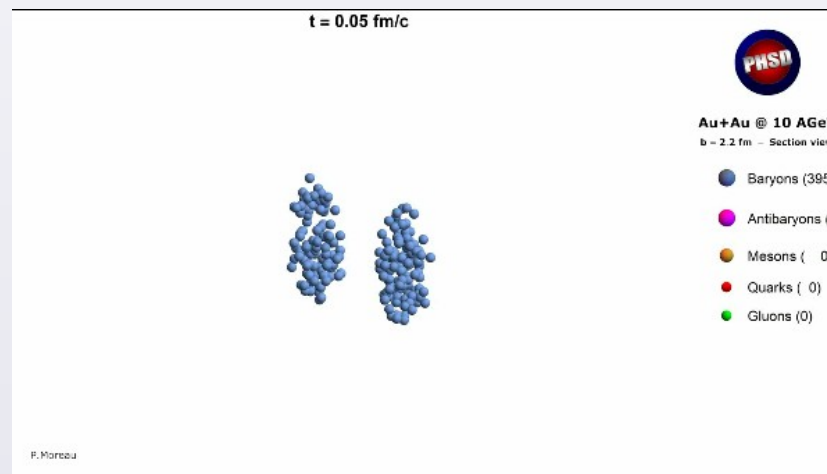
- **QMD** simulation of Au+Au collision at beam kinetic energy  $T_{\text{Beam}} = 15 \text{ MeV/nucleon}$  (15A MeV)

[ [www.fuw.edu.pl/~kpias/rhic/QMD\\_Tb.015\\_b08\\_010.mpg](http://www.fuw.edu.pl/~kpias/rhic/QMD_Tb.015_b08_010.mpg) ]

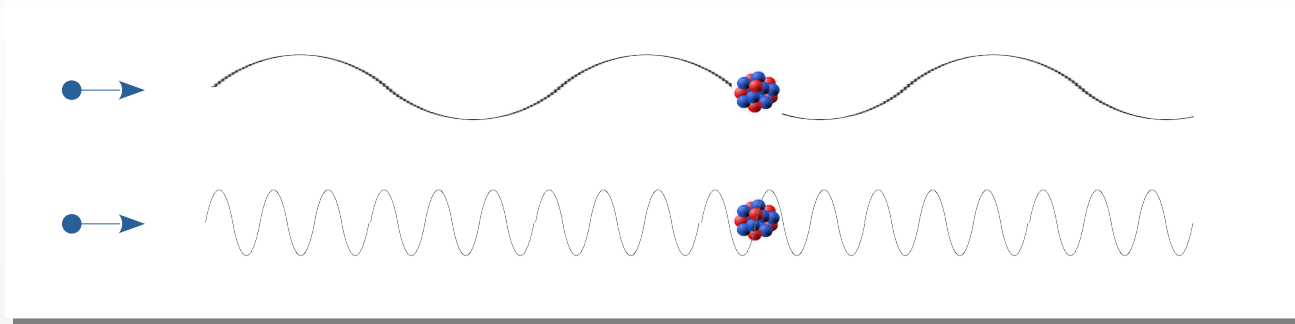


- **PHSD** simulation of Au+Au collision at beam kinetic energy  $T_{\text{Beam}} = 10 \text{ GeV/nucleon}$  (10A GeV)

[ [theory.gsi.de/~ebratkov/phsd-project/PHSD/documents/movie\\_AuAu\\_10AGeV.mp4](http://theory.gsi.de/~ebratkov/phsd-project/PHSD/documents/movie_AuAu_10AGeV.mp4) ]



- Which basic parameters change with beam energy?



$T_{\text{Beam}} / \text{nucleon}$	$\gamma$	$\beta$	$\lambda_{\text{de Broglie}} [\text{fm}]$
5 MeV	1.005	0.10	13
50 MeV	1.05	0.3	4
500 MeV	1.5	0.75	1
5 GeV	6	0.99	0.2
50 GeV	55	0.9998	0.02
500 GeV	530	0.999998	0.002

Mean field sector  
Nucleon "sees" nucleus as a whole

Hadron-hadron sector  
Hadron production in hh channels

Quark-gluon sector

- How to calculate it?

$$T_{\text{Beam}} = m_N c^2 (\gamma - 1) \quad \Rightarrow \quad \gamma = 1 + \frac{T}{m_N c^2} \quad \lambda_{\text{de Broglie}} (N) = \frac{h}{p_N} = \frac{\hbar c \cdot 2\pi}{m_N c^2 \cdot \gamma \beta}$$

$$\beta = \sqrt{1 - \gamma^{-2}}$$

- With increasing beam energy the **relativistic kinematics** becomes more and more relevant (e.g. for  $T_{\text{Beam}} = 500 \cdot A \text{ MeV}$ , coefficient  $\gamma = 1,5$ ).
- Increase of beam energy causes contraction of de Broglie wavelength, and therefore also the objects (so-called **degrees of freedom**) should be adequate to the scale :

At **low energies** the interaction of selected nucleon with nucleus is described by the **potential**, generated by the whole nucleus (so-called **Mean field**) .

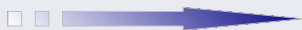
At **higher energies** ( $T_{\text{Beam}} \gtrsim 100 \cdot A \text{ MeV}$ ) the **nucleon-nucleon collisions** (NN) appear. These collisions may lead to production of new hadrons (h) , e.g.:

mesons  $\pi, K, \phi, J/\psi, D \dots$       baryons  $N, \Delta, \Lambda, \Sigma, \Xi \dots$

These hadrons move further within the nuclear matter – and can collide with other hadrons. The occurring process can be **two-body** ( $h_1 h_2 \rightarrow h_3 h_4$ ) , **three-body** ( $h_1 h_2 \rightarrow h_3 h_4 h_5$ ) , ...

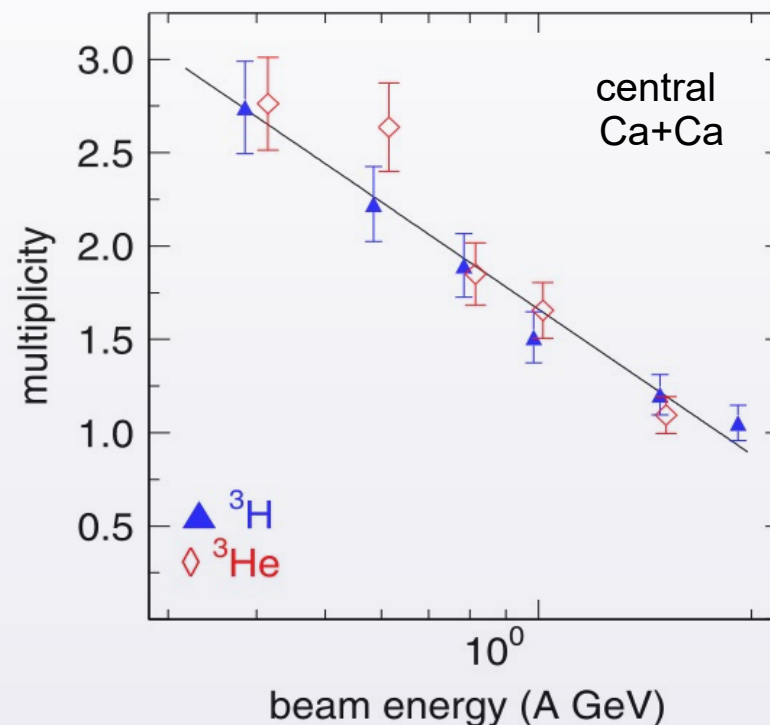
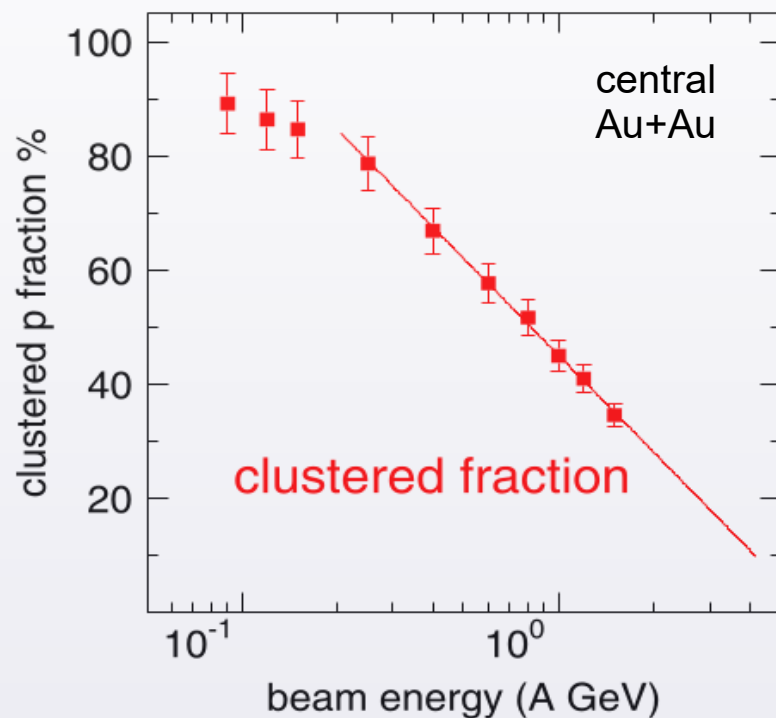
Probabilities of these processes are quantified by **energy-dependent cross sections** .

At **ultrarelativistic energies** ( $T_{\text{Beam}} \gtrsim 5 \cdot A \text{ GeV}$ ) the **quark-gluon** processes appear.



**Selected model framework should be adequate to the beam energy.**

- Proton-neutron (p-n) interaction may lead to the production of **deuteron** (d). Deuteron-neutron (d-n) interaction may create **triton** (t) and deuteron-proton (d-p) create  **$^3\text{He}$** . Etc... These particles are called the **Light Charged Particles (LCP, clusters, small nuclear fragments)**.
- At  $T_{\text{Beam}} \sim 2 \cdot A \text{ GeV}$ , as much as  $\frac{1}{4}$  protons are bound in LCP. Trace amounts of deuterons are seen in LHC.



W.Reisdorf et al.,  
Nucl.Phys. A 848, 366 (2010)

- Usually, if LCP appears in the models, they are assembled from p and n, already after the simulation. A consistent description of production and dynamics of LCP is currently being developed only within **PHQMD** ( [[flagship paper](#)], [[github site](#)] ).

➡ If description of LCP is relevant, one should consider the predictive power of model-candidates.

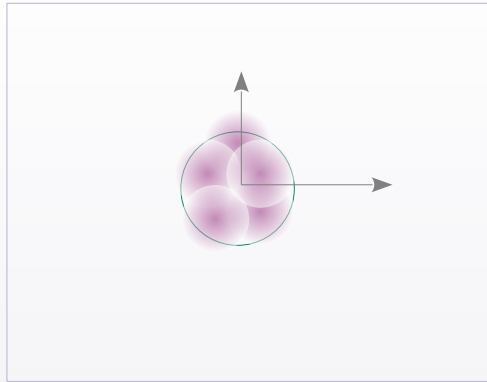
In  $\infty$ 

Nucleons are free,  
 $\vec{p}_i = \vec{0}$ .

$$E_{\text{System}} = \sum_i m_{N,i} c^2$$

$$\frac{E_{\text{System}}}{A} = m_N c^2$$

Nucleus as a whole:

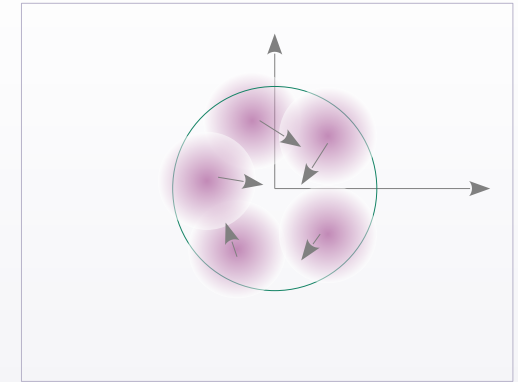


In nucleus' own frame,  
 $\vec{p}_{\text{nucleus}} = \vec{0}$ .

$$E_n = M_n c^2 = \sum_i m_{N,i} c^2 - \underbrace{B_J}_{\text{Definition of } B_J}$$

$$\frac{E_n}{A} = m_N c^2 - \frac{B_{\text{nucleus}}}{A} \approx 8 \text{ MeV}$$

Nucleus as a sum of nucleons:



Pauli exclusion  $\rightarrow$  nucleons must move,  
 $\vec{p}_i \neq \vec{0}$ .

$$E_{\text{nucl.}} = \sum_i e_i$$

$$e_i = \sqrt{(m_{N,i} c^2)^2 + (\vec{p}_i c)^2} + \frac{U_i}{A}$$



In reality the formulae are more complex.

- ① Coulomb interaction must be added ( $\varphi, \bar{A}$ ).
- ② Within QCD with strong interactions, so-called scalar and vector potentials appear, which e.g. change mass of nucleon inside nuclear matter.

$$e_i = \sqrt{(m_{N,i} c^2 - V_S)^2 + (\vec{p}_i c - \vec{V}_W)^2} + V_{W,0}$$

( not by heart :) )

- **Real atomic nucleus:** system of nucleons with finite  $N$  and  $V$  that interacts strongly, weakly and by Coulomb. Nucleons from  $\infty$  fall into the potential well, wherein they acquire kinetic energy (Fermi motion). Energy is decreased by binding energy  $E_B$ . In the **liquid drop model**:

$$E_B = a_V A - a_S A^{2/3} - a_C \frac{Z^2}{A^{1/3}} - a_A \frac{(N-Z)^2}{A} \pm \delta(A, Z)$$

For average **nucleus**:  $E_B / A \approx 8 \text{ MeV}$ .

- **Nuclear matter:** abstract matter built of nucleons, of infinite  $N$  and  $V$ , but finite  $\rho$ . Depth of binding depends on: temperature, density, n/p ratio.

$$E_B(\rho = \rho_0, T = 0) = a_V A \dots - a_A \frac{(N-Z)^2}{A}$$

( $\rho_0 = 0.17 \text{ fm}^{-3}$ , "normal density of nuclear matter")

For symmetric ( $N = Z$ ) **nuclear matter** in normal state:  $E_B / A \approx 16 \text{ MeV}$ .

- During the collision the matter condenses and subsequently expands. How  $E_B / A$  depends on density  $\rho$ ? Two points are fixed:

- ① for  $\rho = 0$  (free nucleons),  $E_B / A = 0 \text{ MeV}$
- ② for  $\rho = \rho_0$  (stable nucleus),  $E_B / A = -16 \text{ MeV}$

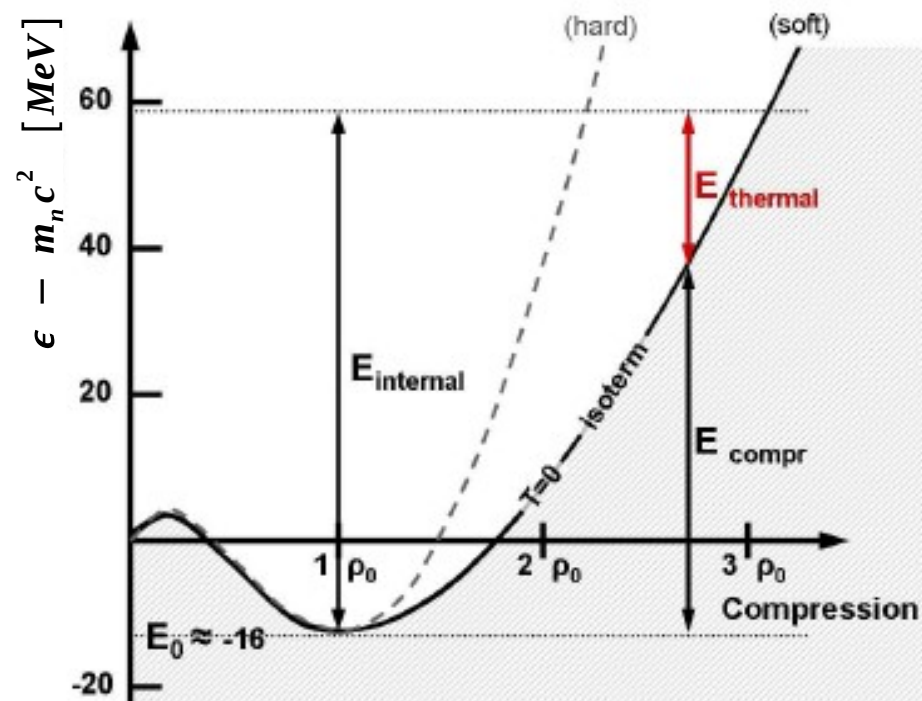
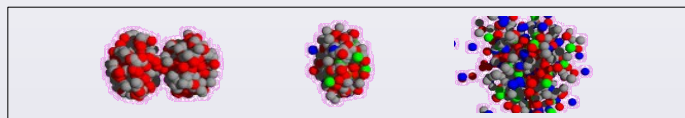
- One can derive models of interactions that aim to reproduce findings [①, ②]. One can also insert into the model some functional dependence that agrees to [①, ②]. The testing ground are the kinematic distributions of particles: if/when model agrees with experiments?

- Nuclear matter equation of state ("EoS") :

$$\epsilon \equiv \frac{E}{A}(\rho, T) = m_n c^2 + \epsilon_{\text{Kin}}(\rho, T=0) + u(\rho, T=0) + \epsilon(\rho, T>0)$$

- It's worth to compare the plot to the dynamics of the nuclear collision. Let's trace it:

$$\rho_0 \rightarrow 3\rho_0 \rightarrow \rho_0$$



- Thermodynamical quantities:

pressure

$$p = \dots = -\rho \left. \frac{\partial \epsilon}{\partial \rho} \right|_{T=0}$$

Bulk modulus

$$\kappa = \dots = +\rho \left. \frac{\partial p}{\partial \rho} \right|_{T=0}$$

- In nuclear studies:

Incompressibility modulus

$$\kappa \equiv 9 \left. \frac{\partial p}{\partial \rho} \right|_{T=0}$$

- In the state of normal nuclear density ( $\rho = \rho_0$ ):

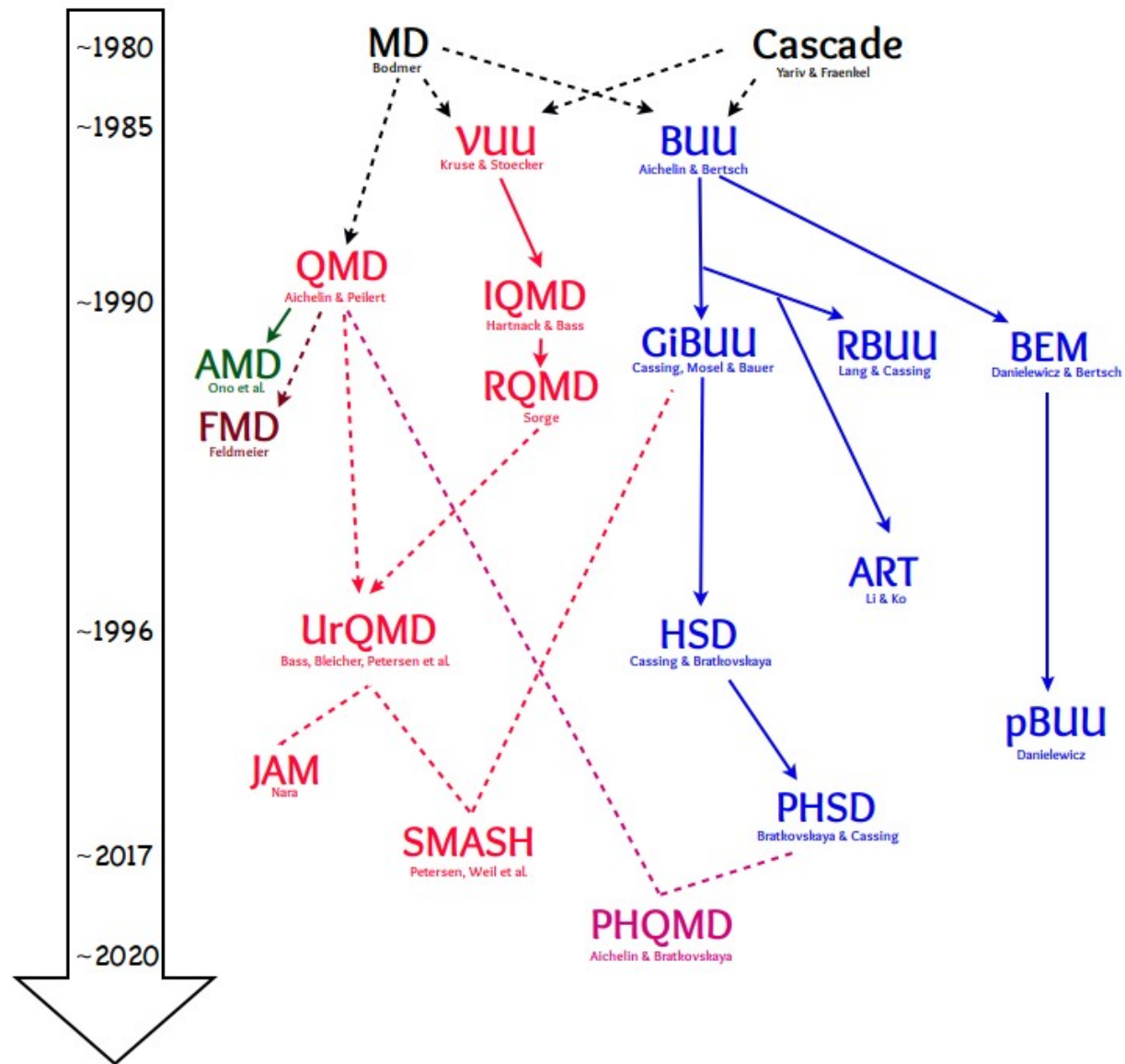
$$\kappa(\rho_0) = \dots = 9 \left. \frac{d^2 \epsilon}{d \rho^2} \right|_{\rho=\rho_0, T=0}$$

(or:  $\sim$ curvature of  $\epsilon$  at  $\rho = \rho_0$ )

- High (low)  $\kappa$  : "hard" ( "soft" ) EoS

Usually in papers: "soft" :  $\kappa \approx 200$  MeV ,  
"hard":  $\kappa \approx 380$  MeV



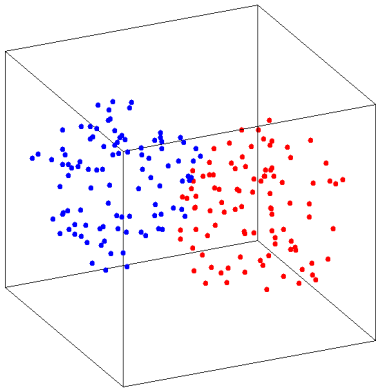


Many models were developed (more than shown above), but many of them inherit the main framework. We shall describe two branches: family of **BUU** and **QMD** models.

- **B**oltzmann – **Ü**hling – **U**hlenbeck transport equation. Exemplary introductions:

B.Serot, J.Walecka, arXiv:nucl/th/9701058 section 7A  
C.Hartnack et al., Eur. Phys. J. A 1, 151 (1998)

- Outline. We consider  $N$  particles moving in the phase space  $(\mathbf{x}^3, \mathbf{p}^3)$ . Their distribution is described by the function  $f(\mathbf{r}, \mathbf{p}, t)$ . Particles are **in a field described by a potential  $U$**  (mean field; it's the BUU's feature).



$$N = \int d^3 \mathbf{r} \int d^3 \mathbf{p} f(\mathbf{r}, \mathbf{p}, t)$$

$$df \equiv \frac{\partial f}{\partial t} dt + \frac{\partial f}{\partial r_i} dr_i + \frac{\partial f}{\partial p_i} dp_i \quad \left\{ \begin{array}{l} \frac{\partial f}{\partial r_i} dr_i = (\nabla_r f) \cdot d\mathbf{r}_i \\ d\mathbf{r} = \mathbf{v} dt \\ d\mathbf{p} = -\nabla_r U dt \end{array} \right.$$

$$\frac{df}{dt} = \frac{\partial f}{\partial t} + \nabla_r f \cdot \mathbf{v} - \nabla_p f \cdot \nabla_r U$$

- Potential  $U$  of the mean field:

$$U = U(\rho) + U_{Coulomb} + U(\vec{p})$$



$$U(\rho) = \alpha \frac{\rho}{\rho_0} + \beta \left( \frac{\rho}{\rho_0} \right)^{\gamma}$$

(nuclear matter "equation of state",  
typical parameterization)

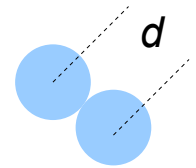
$$U(\vec{p}) = \delta \frac{8}{\rho_0 (2\pi)^3} \int d^3 p' \frac{f(\mathbf{r}, \mathbf{p}')}{1 + \left( \frac{\mathbf{p} - \mathbf{p}'}{\Lambda} \right)^2}$$

(momentum-dependent term of potential  
typical parameterization)

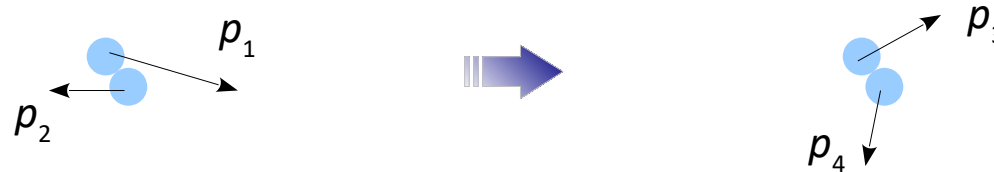
- If  $N = \text{const}$ , we would have:  $\frac{df}{dt} = 0$

- ... but there are also **collisions**. Let's consider a two-body process  $(1,2) \rightarrow (3,4)$ . Probability of collision is described by the cross section  $\sigma$  (more precisely,  $d\sigma/d\Omega$ ). A collision occurs if:

$$d < \sqrt{\frac{\sigma_{NN}}{\pi}}$$



- A collision generates a single loss in cells of momenta  $p_1$  and  $p_2$  for the sake of gain in  $p_3$  and  $p_4$ .



- But one should account for the Pauli exclusion (momenta cells  $p_3$  i  $p_4$  are not always available). It is included probabilistically:

$f(\mathbf{r}, \mathbf{p}, t)$  is a probability of occupation of momentum cell  $p$ .  
 $1 - f(\mathbf{r}, \mathbf{p}, t)$  is a probability that momentum cell  $p$  is free.

Additional term in BUU equation, describing collisions:  $\frac{df}{dt} = I_{coll}$

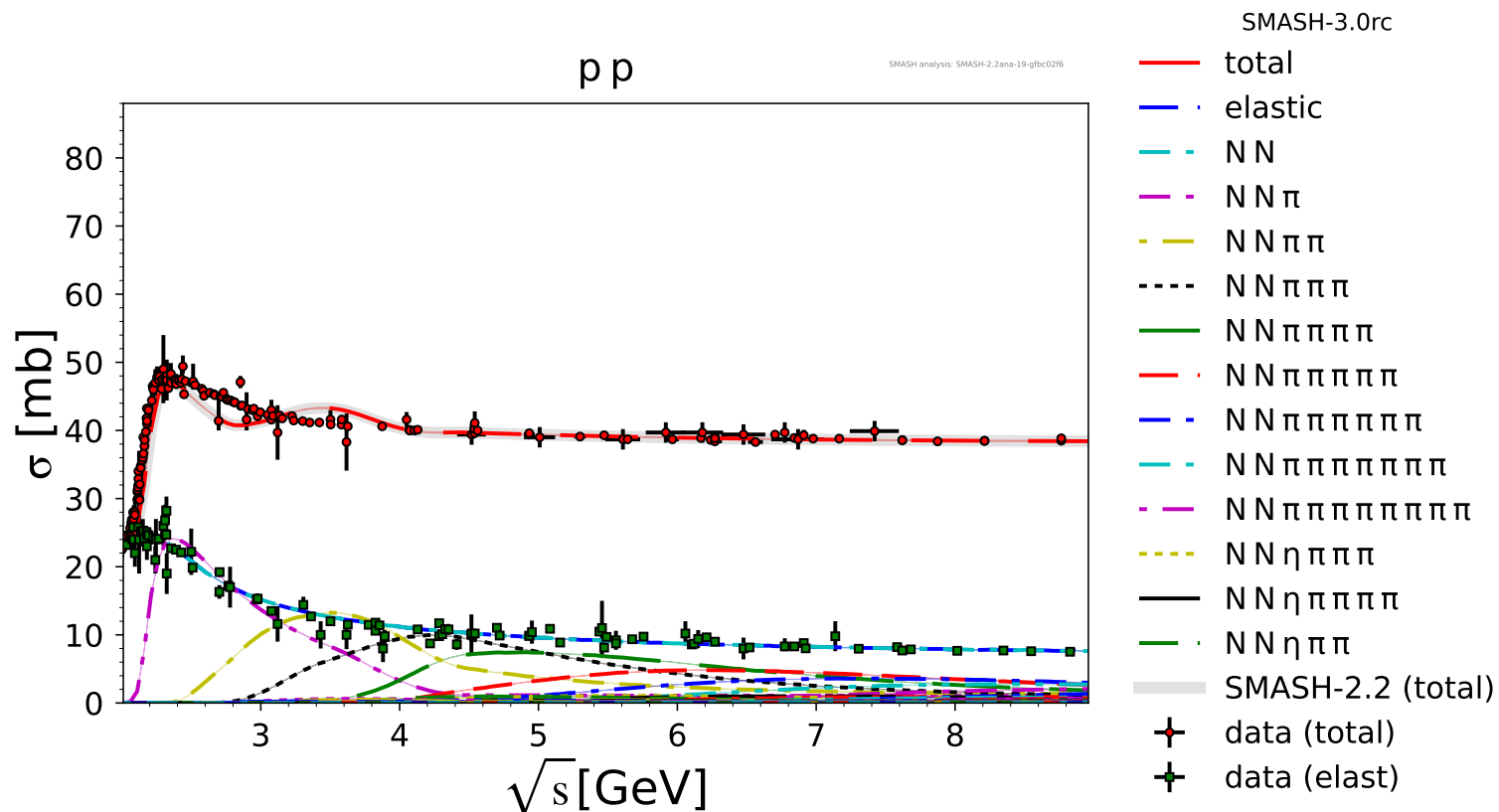
$$I_{coll} = \sum_{\text{reaction channels}} \int \frac{d^3 p_2 d^3 p_3 d^3 p_4}{(2\pi)^6} \frac{d\sigma_{12 \rightarrow 34}}{d\Omega'} \cdot \underbrace{[(1-f_1)(1-f_2)f_3f_4]}_{\text{Gains}} - \underbrace{f_1f_2(1-f_3)(1-f_4)}_{\text{Losses}} \cdot \underbrace{\delta(p_1 + p_2 - p_3 - p_4)}_{\text{Momentum conservation}}$$

- The **BUU** (Boltzmann-Ühling-Uhlenbeck) equation in short:

$$\frac{df}{dt} = I_{coll}$$

- **Production of new particles** is also realized through collisions. Each model has inside a set of reaction channels. Per channel it uses a parametrization of  $\sigma = f(\text{energy})$ . They are usually fits to the experimental databases. Some channels (like string production) are algorithmic.
- For channels experimentally (nearly) impossible to extract (e.g.  $N\Delta \rightarrow X$ ), physics arguments are invoked like: **detailed balance**, **isospin symmetry**, **strangeness balance** etc.
- **Flagship papers of specific models** usually report the relevant formulae and figures of  $\sigma = f(\text{energy})$ .

A nice demonstrator is SMASH's web-based collection of its  $\sigma$  plots [ [here](#) ].  
E.g. here you can see, how Smash assembles the total  $\sigma$  (pp) from subsequent channels in the model.



- For each collision a distribution (of center positions of nucleons)  $f(\mathbf{r}, \mathbf{p}, t)$  *in the initial state* is prepared:

$$f(\mathbf{r}, \mathbf{p}, t) = \sum_{i=1}^{A_{\text{beam}} + A_{\text{target}}} \delta(\mathbf{r} - \mathbf{r}_i) \delta(\mathbf{p} - \mathbf{p}_i)$$

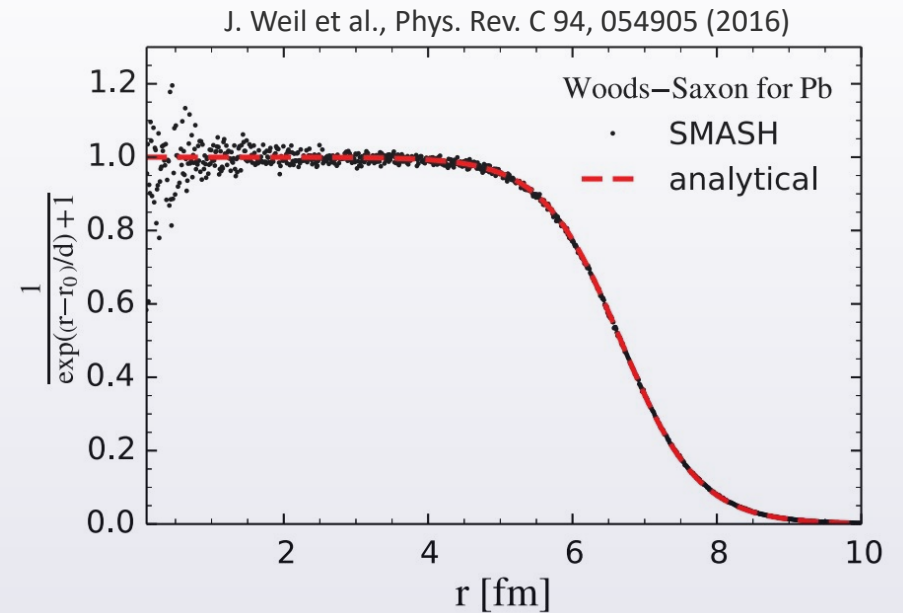
- Initialization of positions**

Usually: **Woods-Saxon** distribution with parameters based on experimental charge distribution

$$\frac{d^3 N}{dr^3} = \frac{\rho_0}{\exp\left(\frac{r-r_0}{d}\right) + 1}$$

TABLE I. This table summarizes the specific parameters used in the Woods-Saxon initialization for some nuclei.

Nucleus	$A$	$r_0$ [fm]	$d$ [fm]
U	238	6.86	0.556
Pb	208	6.67	0.54
Au	197	6.38	0.535
Cu	63	4.20641	0.597



- Initialization of momenta**

Usually: for nucleons away by  $r$  from the center,  $\mathbf{p}$  is pulled randomly from unit sphere, i.e.:  $\mathbf{p} \in [0, p_{\text{Fermi}}(r)]$

$$p_{\text{Fermi}}(\vec{r}) = \hbar \left[ \frac{3}{2} \pi^2 \rho(\vec{r}) \right]^{1/3}$$

Usually, Fermi momentum in the middle of a nucleus  $\approx 270 \text{ MeV}/c$ .

- Motion of a given particle is governed by the *1-body hamiltonian* :

Case of non-relativistic potential:  $H = \sqrt{p^2 + m^2} + U$

Case of relativistic potential:  $H = \sqrt{(\vec{p} - \vec{V}_V)^2 + (m - U_s)^2} + V_0$

- *In consecutive time steps* ( $n$ ) position and momentum of  $i$ -th particle evolves due to:  
(below, for simplicity, non-relativistic approximation)

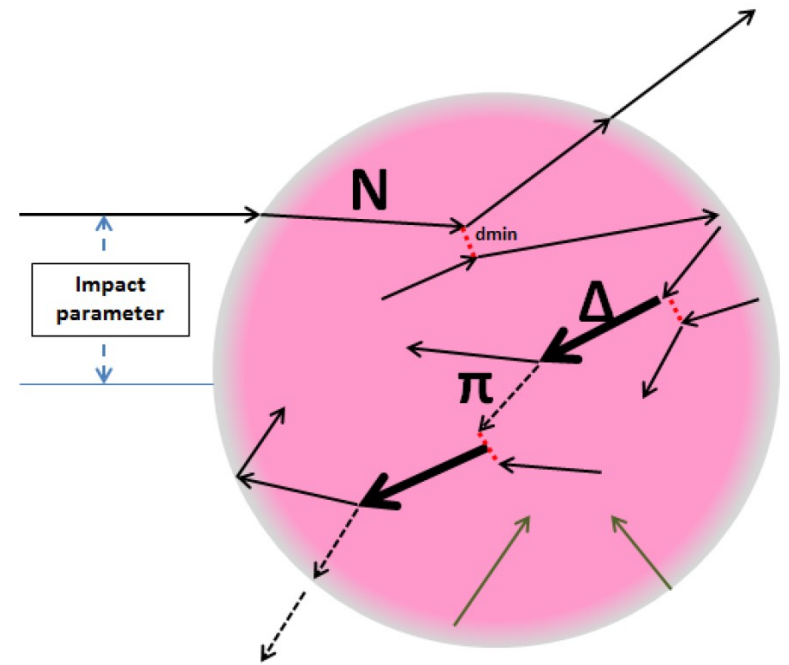
$$\left\{ \begin{array}{l} \dot{\mathbf{r}}_i = \nabla_{\mathbf{p}_i} H \\ \dot{\mathbf{p}}_i = -\nabla_{\mathbf{r}_i} H \end{array} \right. \Rightarrow \left\{ \begin{array}{l} \mathbf{r}_i(n+1) = \mathbf{r}_i(n) + \frac{\mathbf{p}_i(n+\frac{1}{2})}{m} \cdot \Delta t + \nabla_{\mathbf{p}_i} U_i \cdot \Delta t \\ \mathbf{p}_i(n+\frac{1}{2}) = \mathbf{p}_i(n-\frac{1}{2}) - \nabla_{\mathbf{r}_i} U_i(n) \cdot \Delta t \end{array} \right.$$

⊕ collisions: if  $d < d_{\min}$  and no Pauli blocking  $\rightarrow$  then  $\delta(p_1)$  and  $\delta(p_2)$  changes into  $\delta(p_3)$  and  $\delta(p_4)$

- Caution: Within BUU the only field-type (continuous) interaction – is through the mean field.  
No single nucleon–nucleon interactions (except for collisions).  
 $\rightarrow$  BUU usually knows nothing about adjacent nucleons coalescing into LCPs (d, t,  $^3\text{He}$ , ... ).

- **Cascade** is a collective name for various simulation codes (mode in them) that share following features:

- ▷ Sharp sphere **potential** well (**constant** inside target nucleus).  
As  $\vec{F} = -\nabla V \Rightarrow$  no force applied to tracked hadrons when inside nucleus
- ▷ Potential has an **edge** (around nucleus' **skin**)  
 $\Rightarrow$  nucleons are reflected back or tunnelled through
- ▷ **Caution**: the initial positioning is usually not done according to the uniform sphere, but to Woods-Saxon or modified oscillator distribution.
- ▷ Overall **nucleon density stays constant** (not for high-energy Heavy-Ion collisions)
- ▷ Particles follow straight lines. They can do **binary collisions**, but Pauli exclusion is checked.
- ▷ In collisions  $\pi$  or  $\Delta$  can be created.  $\Delta$ s decay into  $[N \pi]$ . Some Cascade codes generate **LCPs**.



[Credit: S. Sharma, Ph.D., Jagiellonian Univ., 2015]

- **Where can these models be useful?**

- ☞ Collisions **initiated by hadrons** ( $p, \pi, \dots$ ) or **light nuclei**, as long as assumption of constant  $\rho$  holds.

- In **QMD** models the objects are the particle wave packets:

e.g. C.Hartnack et al.  
Eur. Phys. J. A 1, 151 (1998)  
[arxiv.org/abs/nucl-th/9811015](https://arxiv.org/abs/nucl-th/9811015)

$$\Psi = \prod_i \psi_i \sim \prod_i \exp \left[ -\frac{(\mathbf{x}_i - \mathbf{r}_i(t))^2}{L} \right] \cdot \exp [i \mathbf{x}_i \mathbf{p}_i(t)]$$

Parameter  $L$  describes the packet size. It is found such that  $\Psi$  describes the density drop at the nucleus' skin.

- An  $i$ -th particle moves in the potential  $\oplus$  collides with neighbours.  
However, the potential is built from a sum of potentials from ' $j$ -th' particles surrounding the ' $i$ -th' one.

**Quantum hamiltonian:**  $\langle H \rangle = \langle T \rangle + \langle V \rangle = \sum_i T_i + \sum_i \sum_{j>i} \int \psi_i^* \psi_j^* V^{ij}(x_1, x_2) \psi_i \psi_j dx_1 dx_2$

**Equation of motion:** 
$$\begin{cases} \dot{\mathbf{r}}_i = \frac{\mathbf{p}_i}{m} + \nabla_{\mathbf{p}_i} \sum_j \langle V_{ij} \rangle \\ \dot{\mathbf{p}}_i = -\nabla_{\mathbf{r}_i} \sum_{j \neq i} \langle V_{ij} \rangle \end{cases}$$
 (in fact, the simulation traces the centroids of wave packets)

- $N_i$ - $N_j$  interactions :**  $V_{ij} = V_{ij}^{\text{Skyrme}} + V_{ij}^{\text{Yukawa}} + V_{ij}^{p\text{-dependent}} + V_{ij}^{\text{Coulomb}} + V_{ij}^{p-n \text{ asymmetry}}$

$$\begin{aligned} = & \left[ t_1 + t_2 \rho^{y-1}(\mathbf{x}_i) \right] \cdot \delta(\mathbf{x}_i - \mathbf{x}_j) + t_3 \frac{\exp \left\{ -|\mathbf{x}_i - \mathbf{x}_j|/\mu \right\}}{|\mathbf{x}_i - \mathbf{x}_j|/\mu} + \\ & + t_4 \ln^2 \left( 1 + t_5 (\mathbf{p}_i - \mathbf{p}_j)^2 \right) \cdot \delta(\mathbf{x}_i - \mathbf{x}_j) + \frac{Z_i Z_j e^2}{\{\mathbf{x}_i - \mathbf{x}_j\}} + t_6 \frac{1}{\rho_0} T_i^3 T_j^3 \cdot \delta(\mathbf{x}_i - \mathbf{x}_j) \end{aligned}$$



- From the [talk](#) of Ch. Hartnack and J. Aichelin (2015), the authors of **IQMD**:

## Definition of the potentials

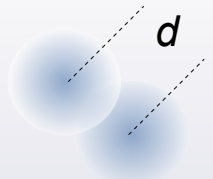
$$\begin{aligned}
 V^{ij} &= G^{ij} + V_{\text{Coul}}^{ij} \\
 &= V_{\text{Skyrme}}^{ij} + V_{\text{Yuk}}^{ij} + V_{\text{mdi}}^{ij} + V_{\text{Coul}}^{ij} + V_{\text{sym}}^{ij} \\
 &= t_1 \delta(\vec{x}_i - \vec{x}_j) + t_2 \delta(\vec{x}_i - \vec{x}_j) \rho^{\gamma-1}(\vec{x}_i) + t_3 \frac{\exp\{-|\vec{x}_i - \vec{x}_j|/\mu\}}{|\vec{x}_i - \vec{x}_j|/\mu} + \\
 &\quad t_4 \ln^2(1 + t_5 (\vec{p}_i - \vec{p}_j)^2) \delta(\vec{x}_i - \vec{x}_j) + \frac{Z_i Z_j e^2}{|\vec{x}_i - \vec{x}_j|} + \\
 &\quad t_6 \frac{1}{\rho_0} T_3^i T_3^j \delta(\vec{r}_i - \vec{r}_j)
 \end{aligned}$$

**Bethe Weizsaecker –mass formula:**

**Volume term** + **Surface term** + **Coulomb term** + **symmetry term**  
**(nucl. eos)**      (+pairing term not included)      **(asy- eos)**

- **Hadron-hadron collision.** Occurs if the centroids between 2 hadrons approach closer than:

$$d < \sqrt{\frac{\sigma_{hh}}{\pi}}$$



For fermions, Pauli exclusion is accounted for.

- By selecting components  $V_{ij}$ :  $V^{\text{Skyrme}} + V^{\text{Yukawa}} + V^{\text{p-dependent}}$ , through the respective convolution one can "reproduce" the equation of state of nuclear matter.

$$U(\rho) = \alpha \frac{\rho_{\text{int}}}{\rho_0} + \beta \left( \frac{\rho_{\text{int}}}{\rho_0} \right)^\gamma + U^{\text{p-dependent}}$$

$$U^{\text{p-dependent}} = \delta \cdot \ln^2(\epsilon \cdot (\Delta p)^2 + 1)$$

$\Delta p$ : particle momentum w.r.t  $\langle p \rangle$  of medium

One can choose the  $V_{ij}$  parameters so that the simulation reproduces given Equation of State, (including "recreation" of the hard/soft scenarios)



	$\alpha$ (MeV)	$\beta$ (MeV)	$\gamma$	$\delta$ (MeV)
S	-356	303	1.17	—
SM	-390	320	1.14	1.57
H	-124	71	2.00	—
HM	-130	59	2.09	1.57

- The **Isospin-QMD (IQMD)** variant :

- ▷ Separate treatment of  $n$ ,  $p$ ,  $\Delta$ ,  $\pi$
- ▷ Possible proton-neutron interactions
- ▷ one can describe the asymmetric ( $n \neq p$ ) part of EoS



IQMD provides the framework for description of binding of nucleons into LCPs (clusters).

- **Fact:** each scalar product of two four-vectors is invariant with respect to Lorentz Transform.

$$p_\mu p^\mu = E^2 - \vec{p}^2 = \text{const} \quad \rightarrow \text{quite obvious, as:} \quad E^2 - \vec{p}^2 = m^2$$

$$\left( \sum_i E_i \right)^2 - \left( \sum_i \vec{p}_i \right)^2 = \text{invariant} \equiv \boxed{s}$$

at the same time:  $\left\{ \begin{array}{l} \sum_i E_i = \text{const} \\ \sum_i \vec{p}_i = \text{const} \end{array} \right. \quad \Rightarrow \quad \text{"s" is not only invariant.}$

It also is the integral of motion  
[ = const(t) ].

- Centre of mass frame (CM): such frame that  $\sum_i \vec{p}_{i,CM} = \vec{0}$

$$s \equiv \left( \sum_i E_{i,CM} \right)^2 - \left( \sum_i \vec{p}_{i,CM} \right)^2 = \left( \sum_i E_{i,CM} \right)^2$$

$$\Rightarrow \quad \sqrt{s} = \sum_i E_{i,CM}$$

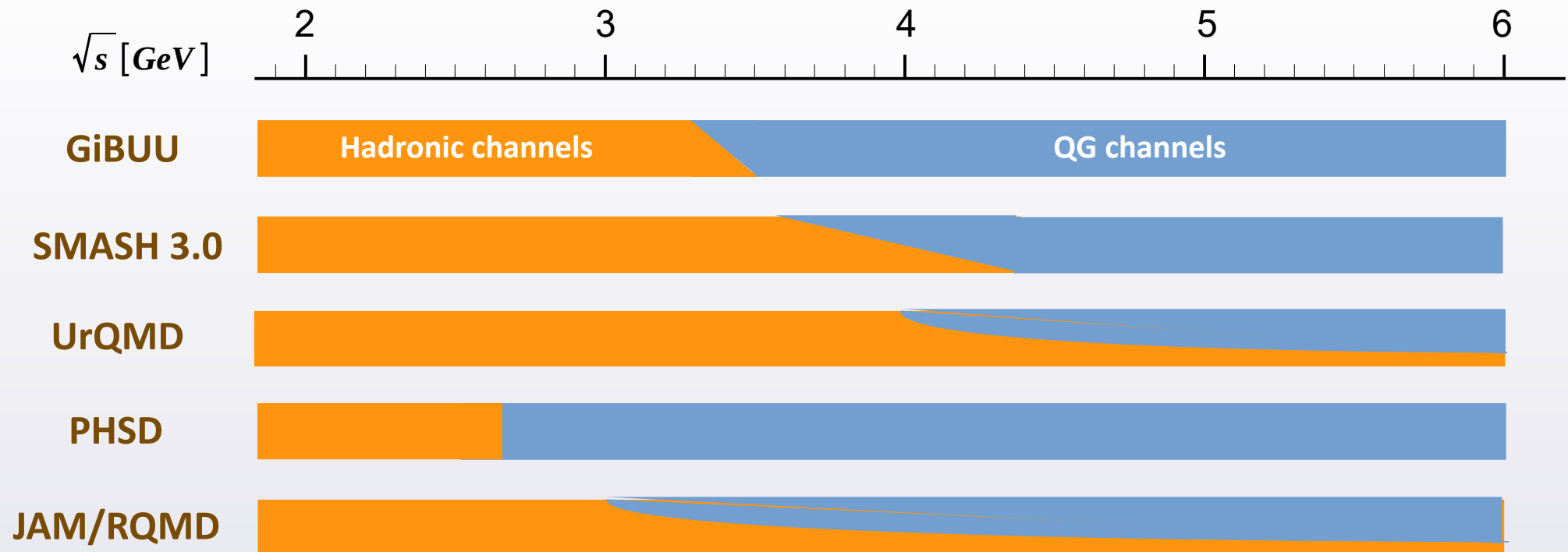
$\sqrt{s}$  is called the "**available energy**". It amounts to the sum of energy of the system in the CM frame.

- Due to shortening of  $\lambda_{\text{de Broglie}}$  with beam  $E$ , with increasing energy we move from the **hadronic sector** to that dominated by **quarks and gluons** (QG). Transport models aim to describe the QG sector too.

Some models propose the insertion of the QGP phase as the initial stage of collision, by transitioning to the **hydrodynamical description**, after which the **hadronization** occurs (QG fluid  $\rightarrow$  hadron gas).

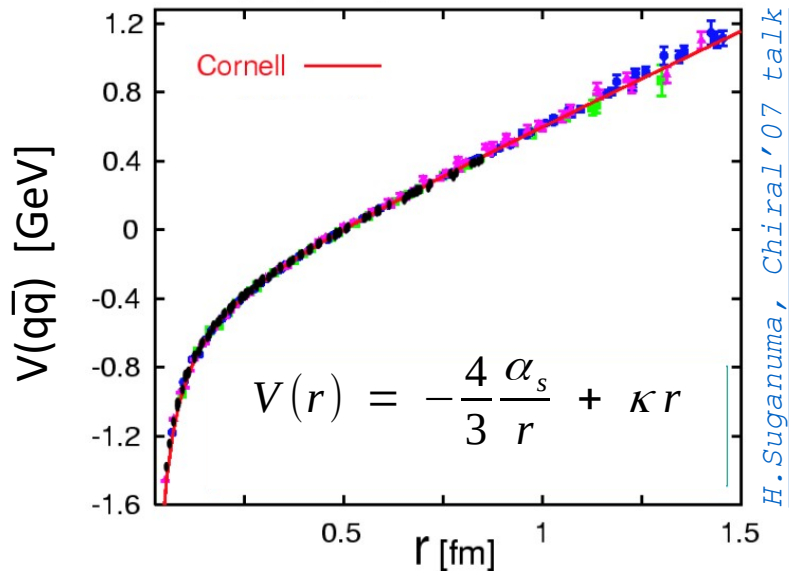
In addition, most of models also at the hadronic stage switch on the QG degrees of freedom. It is possible if in the individual hadron-hadron collision the  $\sqrt{s}$  crosses the threshold value.

- For the baryon-baryon (BB) channels:



- Description of QG channels: so-called "strings". Between 2 quarks a segment is created ("string") with homogeneous energy distribution. This string is divided into portions, which generate hadrons.

- The **QCD potential**:  
attractive strong interaction of  $q\bar{q}$ .



Lines of QCD field are compressed to "tubes" (unlike lines of EM field).

Region between two quarks contains energy with (approximately) flat density distribution.

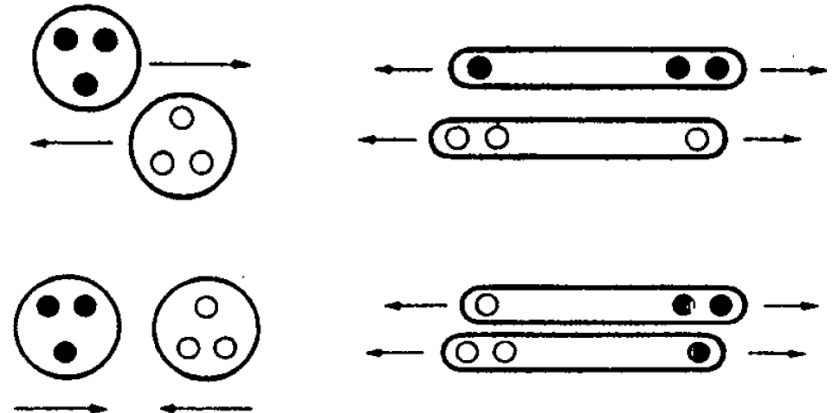
A model object – thin line connecting quarks with linear  $E$  distribution – is called "**string**".

- In HI Coll. modelling, strings appear in the context of each hadron-hadron collision, if  $\sqrt{s}$  exceeds some threshold (a few GeV). But where and how?

▷ Always between selected quarks. Two options:

- ⊙ **Momentum-exchange**:  
two quarks collide and exchange momenta.  
It creates elongation in each hadron (thus, a string).

- ⊙ **Color-exchange**:  
1 quark from  $h_1$  feels 2 quarks from  $h_2$  (1<sup>st</sup> string).  
The remainder interacts likewise (2<sup>nd</sup> string).



H.Schmidt, J.Schukraft,  
J.Phys.G 19, 1705 (1993)

- LUND String Model**

[B. Andersson et al, Phys. Rep. 97, 31 (1983)]

Consider a pair of  $q, \bar{q}$  quarks, for simplicity – massless ones and moving only in Z dimension.

How do they move? (= How the string evolves?)

Hamiltonian:

$$H = |p_1| + |p_2| + \kappa |x_1 - x_2|$$

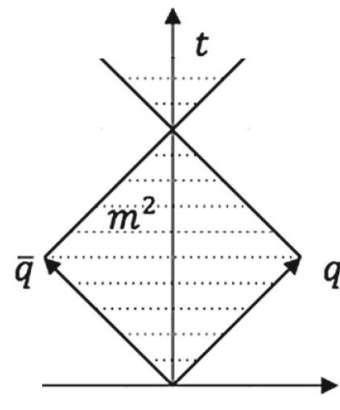
- At some moment it becomes energetically favourable to break the string ("**string fragmentation**") , grab energy from a strip around the breakpoint, and produce from it a new  $q\bar{q}$  pair.

A sketch shows two such **pair production vertices (1, 2)**. But partners move away.

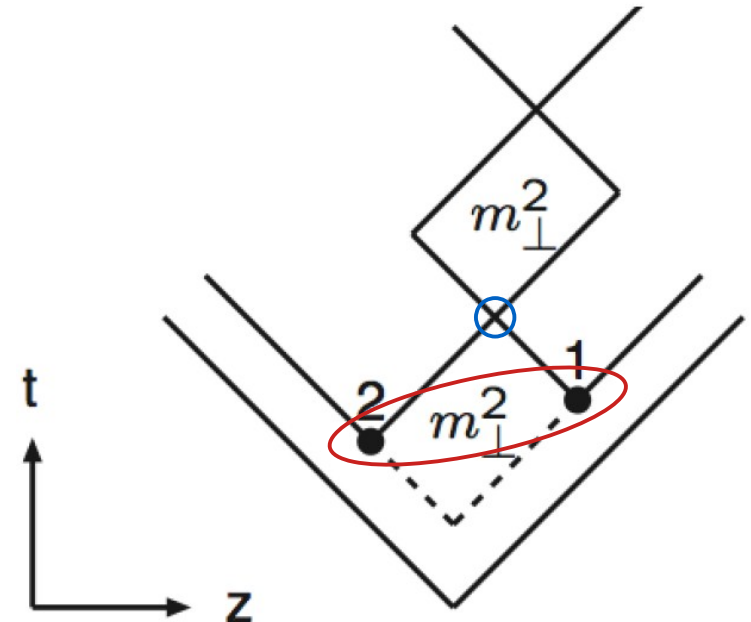
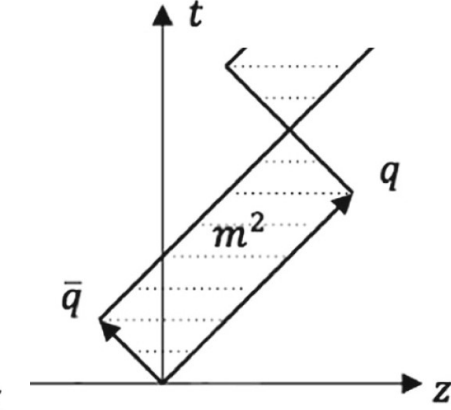
However, right quark from vertex "2" gets bound with left quark from vertex "1". A new hadron is born (**hadronization**). (Time duration of hadron formation process is debated).

Models assume the **first crossing** to be the creation point of a new hadron.

CM Frame



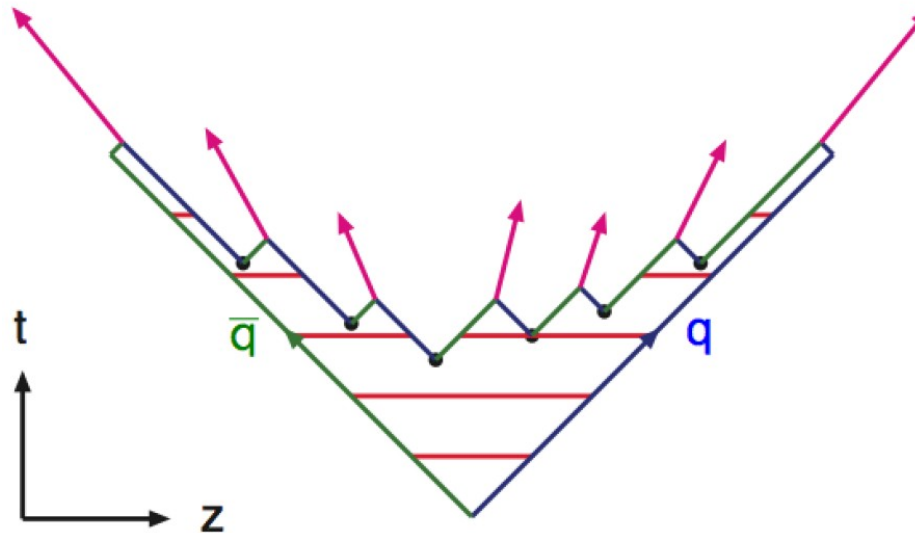
Boosted Frame (Lab)





- Overall picture: many hadrons created from fragmentation of string

[T.Sjöstrand, Pythia talk](#)



- Quantum-mechanically the pair creation is considered as tunneling through the hole after broken string. The concept is also generalized to massive quarks. A **probability for each quark** is derived:

$$P_q \sim \exp\left(-\frac{\pi m_{\perp q}^2}{\kappa}\right) = \exp\left(-\frac{\pi p_{\perp q}^2}{\kappa}\right) \exp\left(-\frac{\pi m_q^2}{\kappa}\right)$$

- Production of quark flavours is in proportion:  $u\bar{u} : s\bar{s} : c\bar{c} \approx 1 : 0.3 : 10^{-11}$
  - $P_T$  spectrum is Gaussian for each quark, and the same for each quark flavour.
- During formation of a new hadron from a pair of quarks, the hadron's  $p_T$  is a sum of constituents.
- A popular implementation of the model is made by **PYTHIA** generator for elementary collisions.  
[\[Homepage\]](#) [\[Interactive Manual\]](#) [\[Tutorial\]](#) [\[Manual Writeup\]](#) .

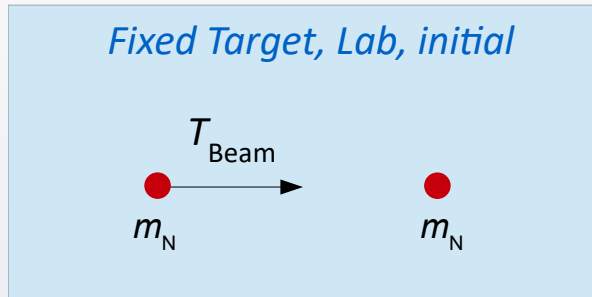
PYTHIA is called by GiBUU, SMASH and JAM2/RQMD models.  
 UrQMD and PHSD have their own string fragmentation approaches.

- Characteristics of main properties of some selected ("currently on market") transport models.

Property	GiBUU	IQMD	UrQMD	JAM2/RQMD	SMASH	PHSD
Relativistic Potential	optionally	n,p : no K : yes	yes	yes	yes	yes
Potential = Mean field	yes	n,p : no K : yes	no	optionally	yes	yes
Potential = sum of nucleon pots.	no	yes	yes	optionally	no	no
Electromagnetic potential	yes	yes	yes for baryons no for $\pi$	optionally	optionally	no
Momentum-dependent potential	yes	yes	no	optionally	optionally	yes
Creation of LCP (clusters)	at end of simulation	at end of simulation	no	at end of simulation	at end of simulation	no
modifications of hadron mass in the medium	yes	yes	no	baryons: yes K, $\pi$ : no	no	yes
Soft QCD region described by "strings"	Pythia	no	Own approach	Pythia	Pythia	Own approach



- For fixed-target collisions, in order to heat up the system (in CM), we provide  $T_{\text{Beam}}$  energy (in Lab). Let's consider the nucleon-nucleon (NN) collision at the fixed target. How to translate  $T_{\text{Beam}} \rightarrow \sqrt{s}$  ?



In **Lab**:  $s \equiv (2m_N + T_{\text{Beam}})^2 - \vec{p}_{\text{Beam}}^2$

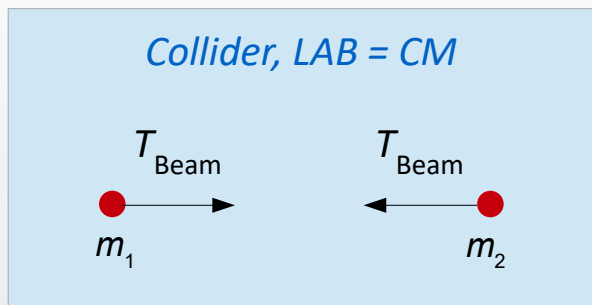
...

$$\sqrt{s} = \sqrt{2 \cdot m_N (2m_N + T_{\text{Beam}})}$$

$\Rightarrow \sqrt{s}$  rises as  $\sqrt{T_{\text{Beam}}}$

E.g. for  $T_{\text{Beam}} = 1 \text{ GeV}$ ,  $\sqrt{s} = 2.3 \text{ GeV}$

- $\sqrt{s}$  is commonly used in the collisions of two opposing beams. Why so?



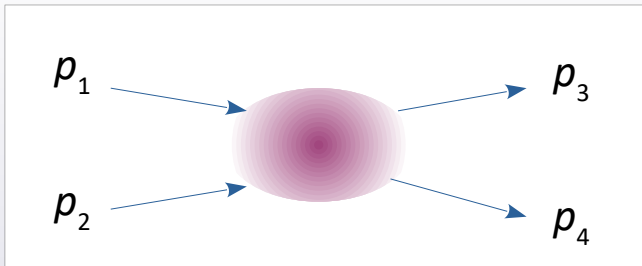
Momenta sum up to  $\vec{0}$ . We obtain:

$$\sqrt{s} = \sum_i E_{i,CM} = 2 \cdot (m_N + T_{\text{Beam}})$$

Nb. in the collider mode it's easier to inject much energy to the system of colliding nuclei:

$$\sqrt{s} \sim T_{\text{Beam}}$$

- Consider process with initially 2 particles with 4-momenta  $p_1, p_2$  and finally also 2, with 4-momenta  $p_3, p_4$ .



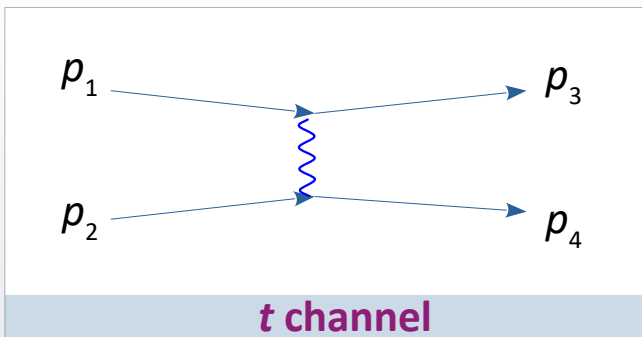
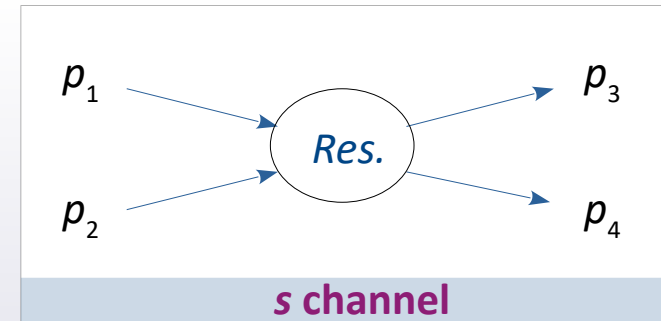
Energy + momentum conservation  $\equiv$  4-momentum conservation.

$$p_1 + p_2 = p_3 + p_4$$

- So it's worth introducing the "**available energy**" :

$$s \equiv (p_1 + p_2)^2 = (p_3 + p_4)^2$$

If a process is the fusion of particles into a resonance, then its mass  $m = \sqrt{s}$ . We say a reaction is in the "**s channel**".



- But the 4-momentum conservation law can be rearranged:

$$p_1 - p_3 = p_4 - p_2$$

and it's worth introducing here "**4-momentum transfer**" :

$$t \equiv (p_1 - p_3)^2 = (p_4 - p_2)^2$$

If a process involves an exchange of a virtual particle, then its squared 4-momentum equals to  $t$ . A reaction is "**in t channel**".

- Example:
 

Process	$\pi^- \Lambda \rightarrow K^- N$	is a "t-channel reaction".
Process	$\pi^- \Lambda \rightarrow \Sigma^{*-} \rightarrow K^- N$	is a "s-channel reaction".

- Simple tools in Bash for previewing text data:

<code>cat [file]</code>	: To display file contents
<code>head -[No. of lines] [file]</code>	: To display first lines of file
<code>tail -[No. of lines] [file]</code>	: To display last lines of file
<code>less [file]</code>	: File reader (handy hotkeys: <code>g</code> <code>G</code> / <code>q</code> )
<code>wc -l [file]</code>	: To count the number of lines
 <code>cat mydata.txt   wc -l</code>	: The <code> </code> ( <i>pipe</i> ) symbol redirects an output A → input B
<code>grep [phrase] [file]</code>	: To search for a (line with) phrase in a file

- Examples:

```
less /etc/os-release
grep PRETTY_NAME /etc/os-release

ln -s ~kpiasecki/soft/test/data.txt .
head -100 data.txt | wc -l
grep "# event" data.txt | grep out | wc -l
```

- Comment:

Shells like Bash offer many text-based tools that e.g. sort, format, replace phrases etc. They allow for manipulation using variables, conditional instructions, loops – including loops over files and directories. One can write "scripts" (codes) and execute them.

Many tutorials on Bash and extensive forums are available on the web. You can find a nice cheat-sheet [here](#). The introduction to Bash within UW Faculty of Physics is e.g. [here](#) and [here](#).

- Running long processes on Linux:

Assume you want to run `MySimuApp`, placed in your directory. You suspect that it would run a long time.

Instead of: `./MySimuApp`

type in this way: `nohup nice ./MySimuApp 1>myLogFile.out 2>&1 &`

- ▷ `nice ...` is the priority manager. **Important** that all the users run longer codes through `nice`: the machine resources will be distributed in a just manner.
- ▷ `1>myLogFile.out` will redirect any message from being printed on the screen → to your Log file  
`2>&1` will redirect any error message to that file.
- ▷ `... &` will allow you to continue using your terminal during the code's running
- ▷ `nohup ...` will completely detach your process from the terminal.  
 Without this, if your terminal is killed, also your process stops immediately.

- [Linux] How to check if your process runs? How to stop it?

- for dynamic list of running processes: `top` or `htop`
- for listing of these process: `ps -u yourLogin --forest`
- to fish the number of your process (PID): `ps -u yourLogin --forest | grep MySimuApp`
- to kill the process identified by given PID (No.): `kill -9 PID`
- to kill the graphical window: `xkill` ← then mouse-click on that window

**Important**: if you think your simulation goes wrong, kill it before rerunning.

- **awk** : a simple, yet powerful tool to **process text files**.
  - ▷ It parses a file **line by line**.
  - ▷ Commands via: **one-liner** or **script-like**.
  - ▷ You can define **variables** and perform **arithmetics + logics** on them. Also, awk has **special variables**.
  - ▷ You can do **if's**, **loops** (while/for) .

- General structure of awk code:

Actions can be done during initialization,  
per every line of file,  
per every line that passes a given filter  
or after the last line processed:

Filter without action will print the whole line:

***condition { action }***

```
BEGIN { action }
      { action }
filter { action }
END   { action }

filter
```

- awk as **one-liner** command : `awk 'filter {command}' filename.txt`

awk invoking **script** with commands: `awk -f mycode.awk filename.txt`

- Nomenclature: **each line = "record"**. Within line, **each word = "field"**

Some **special variables** that awk offers per each line: **NR** = current line number **NF** = No. of fields in current line  
**\$1**, **\$2**, ... = contents of 1<sup>st</sup>, 2<sup>nd</sup>, ...<sup>th</sup> field in a line

- Many tutorials on the web, e.g.:
  - ▷ by AGH [[1](#), [2](#), [3](#)].
  - ▷ by Baeldung [[here](#)]
  - ▷ by Bruce Barnett [[here](#)].
  - ▷ part of FUW's NWP subject [[here](#)]

- **awk (cont).** Download an exemplary transport output: `wget www.fuw.edu.pl/~kpias/ctnp/smash.out`

```
#!/OSCAR2013 particle_lists t x y z mass p0 px py pz pdg ID charge
# Units: fm fm fm fm GeV GeV GeV GeV GeV none none e
# SMASH-2.1.1
# event 0 out 123
40 0.687568 1.38769 23.1843 0.938 1.21816871 0.0609451595 -0.164364771 0.757205986 2112 0 0
40 19.5657 -1.19493 5.98978 0.938 1.15461879 0.627001274 -0.0742496884 0.233788244 2112 1 0
...
```

and try these **one-liners**:

```
awk 'NF==12 && $10==2112' smash.out           : Take lines with 12 words and neutrons. Print lines.
awk 'NR>4 && NR<8 {print $5}' smash.out       : Take lines 5-7. Print 5th field only (masses)
awk 'NF == 12 && $10 == 211' smash.out > pions.dat : Take lines with  $\pi^+$ . Save them in a new file.
```

- You can use **variables** right away (without declaration). They are automatically initialized to empty string / zero. Let's try it within our first **awk script**. Type e.g.: `nano mystat.awk`

```
NF == 12 {
    Num_of_Particles++
    Total_Px += $7
}
END {
    print Num_of_Particles" "Total_Px
}
```

... and run it: `awk -f mystat.awk data.txt`

- Now, let's insert this into the 1<sup>st</sup> line of the script:  
and allow this file to be runnable:  
⇒ We can now run it directly from prompt:

```
#!/usr/bin/awk -f
$ chmod 755 mystat.awk
$ ./mystat.awk data.txt
```

- **If conditional statements.** You can use the C-like syntax.

Imagine we want to select  $\pi^+$ , calculate their  $\langle pz \rangle$  and print just this number.  
Let's encode it in the awk script, under the name `AvgPz.awk` :

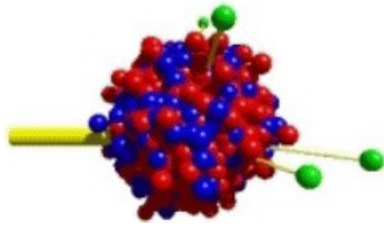
```
NF == 12 {
    if ($10 == 211) {
        NPiPlus++
        Pz_total += $9
    }
}
END {
    Average = Pz_total / NPiPlus
    print Average
}
```

Now, let's run it: `awk -f AvgPz.awk data.txt`

- If you really have to, you can do the same in the one-liner:

```
awk 'NF == 12 { if ($10 == 211) { np++ ; pztot += $9 } } END { avg = pztot/np;
print avg }' data.txt
```

... btw. awk offers much more, including arrays, for loops, functions, analytic math functions, ...  
It can be also embedded in a bash script.



# GiBUU

The Giessen Boltzmann-Uehling-Uhlenbeck Project

- **Home page:** [gibuu.hepforge.org](http://gibuu.hepforge.org)
- Download**
  - Download instructions: [gibuu.hepforge.org/trac/wiki/download](http://gibuu.hepforge.org/trac/wiki/download)
  - Prerequisites: [gibuu.hepforge.org/trac/wiki/tools](http://gibuu.hepforge.org/trac/wiki/tools)
  - Download: [gibuu.hepforge.org/downloads](http://gibuu.hepforge.org/downloads)
- Installation**
  - Compilation instructions: [gibuu.hepforge.org/trac/wiki/compiling](http://gibuu.hepforge.org/trac/wiki/compiling)
- How to run:** [gibuu.hepforge.org/trac/wiki/running](http://gibuu.hepforge.org/trac/wiki/running)
- Help**
  - Tutorial: [gibuu.hepforge.org/trac/wiki/tutorial](http://gibuu.hepforge.org/trac/wiki/tutorial)
  - Presentations: [gibuu.hepforge.org/trac/wiki/Talks](http://gibuu.hepforge.org/trac/wiki/Talks)
  - Animations: [gibuu.hepforge.org/trac/wiki/MovieMain](http://gibuu.hepforge.org/trac/wiki/MovieMain)
- Table of PID codes:** [gibuu.hepforge.org/trac/wiki/ParticleIDs](http://gibuu.hepforge.org/trac/wiki/ParticleIDs)
- Main papers:**
  - O. Buss *et al.* "Transport-theoretical description of Nuclear Reactions",  
Physics Reports 512, 1 (2012), arXiv: 1106.1344



- **On the NPD FUW's training computer:**

```
mkdir gibuu ; cd gibuu  
cp -r /home/kpiasecki/soft/gibuu/ctnp/* .
```

**Let's inspect the input file (c.f. next page), e.g:**

```
less 001_AlAl2.0_test.job
```

**Rich collection of input options** (*please consider them thoughtfully*) :

<http://gibuu.hepforge.org/Documentation/>

**Rich collection of demonstrative input files in this folder:**

`/home/kpiasecki/soft/gibuu/testRun/jobCards/`

**Let's run the simulation** (here: in the background . Log goes into file: `caca_1.91_test.log` )

```
nohup ./GiBUU.x <001_AlAl2.0_test.job 1>alal_2.0_test.log 2>&1 &
```

**Many output files. Among them – file with events containing particles (see next page):**

```
less EventOutput.Real.oscar
```

- Input file** 001\_AlA12.0\_test.job :

```
! file: ./inputOutput/input.f90
&input
  eventtype           =      1
  numEnsembles         =     100
  num_runs_sameEnergy =      5
  numTimeSteps         =     160
  time_max             =     40.0
  printParticleVectorTime = T
  timeForOutput        =      0.
  timeSequence         =     20.
  path_To_Input       = '{...}/buuinput'
  version = 2023
/
{.....}
```

```
! file: ./init/initHeavyIon.f90
&heavyIon
  impact_parameter     = -6.
  impact_profile       = 0
  distance             = 10.
  coulomb              = F
  ekin_lab_Target      = 0.00
  ekin_lab_Projectile  = 2.0
  adjustGridFlag      = T
  cmsFlag              = T
/
! file: ./density/nucleus.f90
&projectile
  projectile_Z= 13, projectile_A= 27
/
! file: ./density/nucleus.f90
&target
  target_Z= 13, target_A= 27
/
{.....}
```

- Output file** EventOutput.Real.oscar :

```
#!OSCAR2013 particle_lists t x y z mass p0 px py pz pdg ID
# Units: fm fm fm fm GeV GeV GeV GeV GeV none none
# File generated by GiBUU (https://gibuu.hepforge.org)
# event 1 out 80
0.000000E+0 7.183791E+0 3.961299E+0 2.780585E+1 9.227111E-1
0.000000E+0 5.118310E+0 -7.210583E-1 2.525251E+1 7.657091E-1
0.000000E+0 2.584306E+0 -1.719659E-1 2.539883E+1 7.726719E-1
0.000000E+0 2.133399E+0 3.397612E-1 2.692126E+1 7.944067E-1
0.000000E+0 6.169842E+0 -1.890743E+0 2.453204E+1 8.264268E-1
....
0.000000E+0 -7.235081E+0 1.162180E+0 -2.613539E+1 7.677036E-1
# event 1 end 0
# event 2 out 80
0.000000E+0 3.456383E+0 6.567166E-1 2.607133E+1 7.648380E-1
0.000000E+0 5.786570E+0 1.426497E-1 2.657666E+1 7.663178E-1
0.000000E+0 6.166525E+0 -3.298759E+0 2.666215E+1 8.635919E-1
....
```

Table of PID codes

1.225751E+0	2.703973E-2	-9.247542E-2	8.011161E-1	2212	100000
1.101021E+0	-5.729713E-3	-1.723748E-2	7.909611E-1	2112	100001
1.088114E+0	-1.631816E-1	-5.991384E-2	7.461942E-1	2112	100002
1.045015E+0	-2.850862E-2	-9.578418E-2	6.717517E-1	2112	100003
1.030645E+0	-6.987948E-2	1.303097E-1	5.971482E-1	2112	100004
1.057389E+0	3.919098E-2	1.860452E-1	-7.017274E-1	2212	103239
8.782891E-1	-6.281280E-3	4.809546E-2	4.290245E-1	2212	100040
1.130114E+0	-1.239606E-1	9.851192E-2	8.153864E-1	2112	100041
1.227330E+0	9.365502E-2	-4.166068E-2	8.660087E-1	2112	100042



# Simulating Many Accelerated Strongly-interacting Hadrons

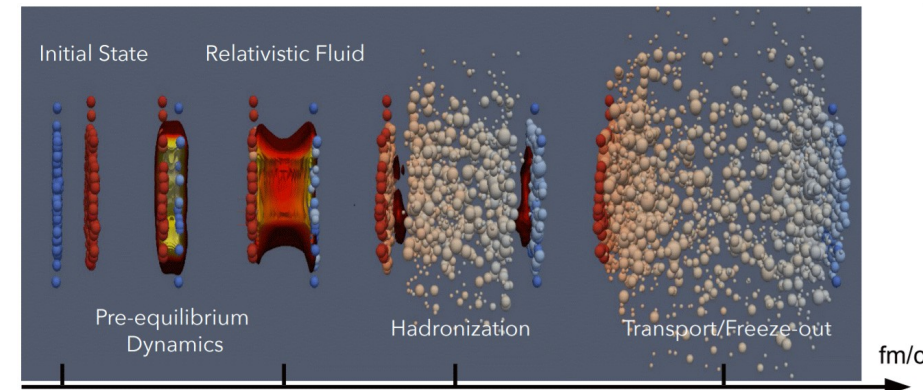
A relativistic hadronic transport approach

• <b>Home page:</b>	<a href="http://theory.gsi.de/~smash/userguide/current">theory.gsi.de/~smash/userguide/current</a> <a href="https://github.com/smash-transport/smash">smash-transport.github.io</a>
<b>Download</b>	<a href="https://github.com/smash-transport/smash">github.com/smash-transport/smash</a>
<b>Installation</b>	<a href="http://theory.gsi.de/~smash/userguide/current/md_README.html">theory.gsi.de/~smash/userguide/current/md_README.html</a>
<b>How to run:</b>	<a href="http://theory.gsi.de/~smash/userguide/current/page_smash_invocation.html">theory.gsi.de/~smash/userguide/current/page_smash_invocation.html</a>
<b>Help</b>	Tutorial: <a href="http://theory.gsi.de/~smash/userguide/current/">theory.gsi.de/~smash/userguide/current/</a> Presentations: D. Oliinychenko (2020) , A. Schäfer (2019) Animations: <a href="https://smash-transport.github.io/img/movie.mp4">smash-transport.github.io/img/movie.mp4</a>
<b>Table of PDG codes:</b>	<a href="https://github.com/smash-transport/smash/blob/master/input/particles.txt">github.com/smash-transport/smash/blob/master/input/particles.txt</a>
<b>Elementary cross sections:</b>	<a href="http://theory.gsi.de/~smash/analysis_suite/SMASH-3.0rc/cross_sections/">theory.gsi.de/~smash/analysis_suite/SMASH-3.0rc/cross_sections/</a>

## • Main papers:

J. Weil *et al.* "Particle production and equilibrium properties within a new hadron transport approach for heavy-ion collisions"  
[Physical Review C 94, 054905 \(2016\)](#),  
arXiv: [1106.1344](#)

H. Petersen *et al.* "SMASH – A new hadronic transport approach"  
[Nuclear Physics A 982, 399 \(2019\)](#),  
arXiv: [1808.06832](#)



- **On the NPD FUV's training computer:**

```
mkdir smash ; cd smash  
cp -r /home/kpiasecki/soft/smash/ctnp/* .
```

**Let's inspect the input file, e.g. :**

```
less config.yaml
```

**Rich collection of input options** *(please consider them thoughtfully) :*

[https://theory.gsi.de/~smash/userguide/current/doxypage\\_input.html](https://theory.gsi.de/~smash/userguide/current/doxypage_input.html)

**Let's run the simulation** **(here: in the background . Log goes into file: `myrun.log` )**

```
nohup nice ./runSmash.sh 1>myrun.log 2>&1 &
```

**File with events containing particles can be found in folder `outdir` :**

```
less outdir/particle_lists.oscar
```

- Input file `config.yaml` :

```
{....}
General:
  Modus:          Collider
  Time_Step_Mode: Fixed
  Delta_Time:     0.1
  End_Time:       40.0
  Randomseed:     -1
  Nevents:        3
  Ensembles:      10

Output:
  Output_Interval: 20.0
  Particles:
    Format:          ["Oscar2013"]
    Extended:        False
    Only_Final:      "Yes"
```

```
Modi:
  Collider:
    Projectile:
      Particles: {2212: 28, 2112: 30} #58Ni
    Target:
      Particles: {2212: 28, 2112: 30} #58Ni
    Impact:
      Sample: "quadratic"
      Range: [0.0, 10.0]

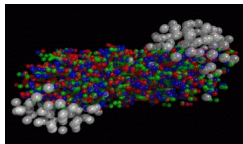
  E_Kin: 1.50
  Calculation_Frame: "center of mass"
  Fermi_Motion: "on"
  Collisions_Within_Nucleus: True

Potentials:
  Skyrme: ...
```

- Output file `particle_lists.oscar` :

```
#!OSCAR2013 particle_lists t x y z mass p0 px py pz pdg ID charge
# Units: fm fm fm fm GeV GeV GeV GeV GeV none none e
# SMASH-1.7
# event 1 in 394
-2.22563 -3.64001 -1.32594 -3.67708 0.938 2.236845 -0.03016814 0.00476330 2.030443 2112 0 0
-2.22563 -5.40173 -3.32581 -2.98890 0.938 2.101389 0.05289568 -0.05137847 1.878977 2112 1 0
-2.22563 -0.84595 -2.10703 -5.13988 0.938 2.523251 0.22803293 0.04328960 2.330897 2112 2 0
...
# event 1 out 394
0 -3.67003 -1.32120 -1.65681 0.938 2.236845 -0.03016814 0.00476330 2.030443 2112 0 0
0 -5.34571 -3.38022 -0.99825 0.938 2.101389 0.05289568 -0.05137847 1.878977 2112 1 0
```

Table of PID codes



# Ultrarelativistic Quantum Molecular Dynamics

- **Home page:**

[itp.uni-frankfurt.de/~bleicher/index.html?content=urqmd](http://itp.uni-frankfurt.de/~bleicher/index.html?content=urqmd)

**Download**

Home page → contact with the authors of the code.

**Help**

Manual:

Presentation:

For version 3.4: [ [Copy](#) ] . For version 4.0 [ [here](#) ]

[M. Bleicher](#) (2018)

**Installation + how to run:**

§4 in Manual

**Table of PID codes:**

[itp.uni-frankfurt.de/~bleicher/content\\_pages/particle\\_list.html](http://itp.uni-frankfurt.de/~bleicher/content_pages/particle_list.html)

- **Main papers:**

S.A. Bass *et al.*

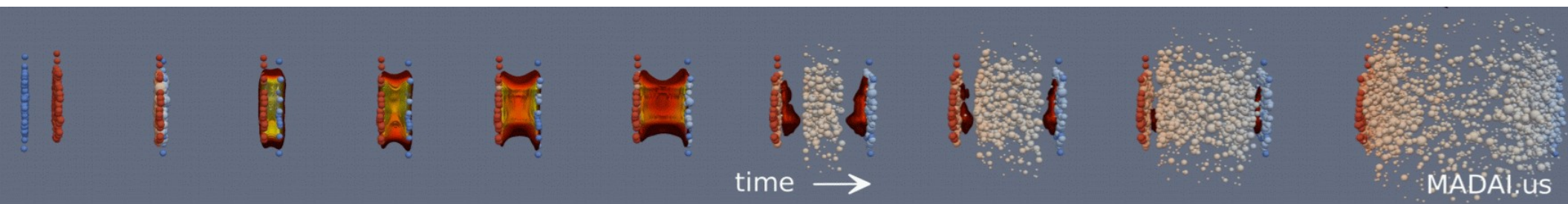
*"Microscopic models for ultrarelativistic heavy ion collisions"*

Progress in Particle and Nuclear Physics 41, 225 (1998), arXiv: [nucl-th/9803035](#)

M. Bleicher *et al.*

*"Relativistic hadron-hadron collisions in the ultra-relativistic quantum molecular dynamics model"*

Journal of Physics G: Nuclear and Particle Physics 25, 1859 (1999), arXiv: [hep-ph/9909407](#)



- **On the NPD FUW's training computer:**

```
mkdir urqmd ; cd urqmd
cp -r /home/kpiasecki/soft/urqmd-3.4/ctnp/* .
```

**Let's inspect these input files :**

```
less runqmd.bash
less inputfile_NiNi1.5
```

**Rich collection of input options is in § 5 of Manual (*please consider them thoughtfully*) :**

[ Manual ]

**Let's perform the simulation (here: in the background. Log goes into file: `mysim.log`)**

```
nohup nice ./runqmd.bash 1>mysim.log 2>&1 &
```

**We've got a collection of files with events:**

Extension f13 :	info on particles at given time(s) [ incl. positions + momenta of last interaction ]
Extension f14 :	info on particles at given time(s) [ basic / extended ]
Extension f15 :	collision history file (binary interaction, decay of resonance, excitation of string)
Extension f16 :	info on decayed particles + surviving particles at last timestep

**Let's take a look :**

```
gedit test.f14 &
```

• **Input file** `inputfile.NiNi1.5` :

```
pro 58 28
tar 58 28
nev 10
imp -10.
elb 1.5
tim 50 20
cto 18 1
eos 0

#f13
#f14
#f15
#f16
f19
f20
```

• **Input file** `runqmd.bash` :

```
{....}
export ftn09=inputfile_NiNi1.5
export ftn13=test.f13
export ftn14=test.f14
export ftn15=test.f15
export ftn16=test.f16
export ftn19=test.f19
export ftn20=test.f20
{....}
```

• **Output file** `test.f14` :

UQMD version: 30400 1000 30400 output\_file 14  
 projectile: (mass, char) 58 28 target: (mass, char) 58 28  
 transformation betas (NN,lab,pro) 0.0000000 0.6665679 -0.6665679  
 impact\_parameter\_real/min/max(fm): 6.28 0.00 10.00 total\_cross\_section(mbarn): 3141.59  
 equation\_of\_state: 0 E\_lab(GeV/u): 0.1500E+0 sqrt(s) (GeV): 0.2517E+0 p\_lab(GeV/u): 0.2250E+0  
 event# 1 random seed: 1600419089 (auto) total\_time(fm/c): 40 Delta(t)\_O(fm/c): 20.000  
 {....}

pvec: r0	rx	ry	rz	p0	px	py	pz	m	ityp	2i3	ch	lcl	ncl	or
119	20			0	0									
73	47	22	4	7	19									
0.20000E+2	0.74819E+2	0.36667E+0	0.10799E+2	0.12222E+2	-0.81322E-2	0.91387E-1	0.80353E+0	0.92473E+0	1	1	1	0	0	0
0.20000E+2	0.34167E+2	0.27792E+0	0.59270E+2	0.11642E+2	0.18126E-1	-0.53284E-1	0.68819E+0	0.93800E+0	1	1	1	79	1	0
0.20000E+2	0.78149E+0	-0.30699E+2	0.10397E+2	0.13424E+2	0.88550E-1	0.91699E-2	0.97368E+0	0.92038E+0	1	1	1	0	0	0
{....}														
119	40			0	0									
83	54	22	7	7	19									
0.40000E+2	0.74819E+1	0.36667E+0	0.24239E+2	0.12282E+1	-0.81322E-2	0.91318E-1	0.80353E+0	0.92437E+0	1	1	1	0	0	0

Diagram illustrating the PID code structure:

```

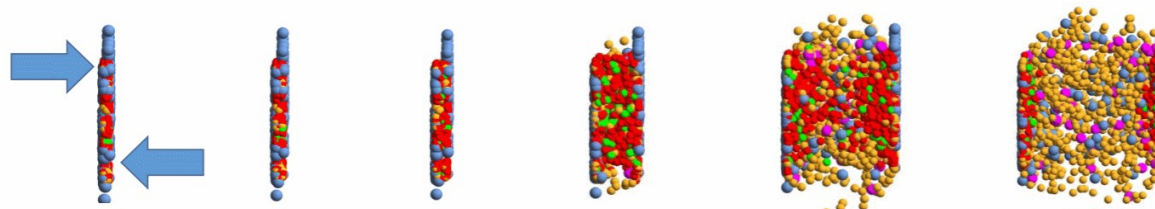
graph TD
    A[Table of PID codes] --> B[2 x I3 (isospin)]
    B --> C[charge]
    C --> D[ityp]
    D --> E[2i3]
    E --> F[ch]
    F --> G[lcl]
    G --> H[ncl]
    H --> I[or]
  
```





## Parton-Hadron-String Dynamics Transport approach

- **Home page:** [theory.gsi.de/~ebratkov/phsd-project/PHSD/](http://theory.gsi.de/~ebratkov/phsd-project/PHSD/)
- Download**      *[contact with authors]*      [theory.gsi.de/~ebratkov/phsd-project/PHSD/index4.html](http://theory.gsi.de/~ebratkov/phsd-project/PHSD/index4.html)
- Installation + how to run:**      § 1.2 of Manual.
- Help**      Manual:      [ Copy ]  
                  Presentations:      E. Bratkovskaya, [Home page](#)  
                  Animations:      [Au+Au @ 10A GeV](#) , [Au+Au @ 35A GeV](#) , [Pb+Pb @ 158A GeV](#)
- Table of PID codes:**      Tables 1.1 i 1.2 in [Manual](#)
- **Main papers:**
  - ⊙ PHSD:  
     W. Cassing, E.L. Bratkovskaya "Parton transport and hadronization from the dynamical quasiparticle point of view",  
     [Physical Review C 78, 034919 \(2018\)](#),    arXiv: [0808.0022](#)
  - ⊙ HSD:  
     W. Cassing, E.L. Bratkovskaya "Hadronic and electromagnetic probes of hot and dense nuclear matter"  
     [Physics Reports 308, 65 \(1999\)](#),    arXiv: [1808.06832](#)



- **On the NPD FUW's training computer:**

```
mkdir phsd ; cd phsd  
cp -r /home/kpiasecki/soft/phsd/ctnp/* .
```

**Let's inspect the input file, e.g. :**

```
less inputPHSD
```

**Rich collection of input options is in § 1.4 of Manual** (*please consider them thoughtfully*) :

[ Manual ]

**Let's run the simulation** (here: in the background. Log goes into file: `mysim.log` )

```
nohup nice ./phsd 1>mysim.log 2>&1 &
```

**We've got a collection of files with events.**

**In between, the file `phsd.dat` with subsequent events containing particles :**

```
less phsd.dat
```



- **Naming.** The model was first published in 1999 as **JAM**. It focused on the region of  $T_{\text{Beam}} \sim 10\text{A GeV}$ , so details of binding energy (EoS) were not so important. Since  $\sim 2019$  the EoS has been carefully modelled and the code was named **RQMD.RMF**. In 2022 the code was ported to C++. The name is "**JAM2**" and "**RQMD.RMF**" is its variant.
- **Home page:** [\[ GitLab \]](#) (Jam2) [\[ link \]](#) for old Jam1
- Download & Installation** [\[ GitLab \]](#) (Jam2)
- Help.** Short Manual (txt) [\[ GitLab \]](#)  
For Jam1: old but explains a lot: [\[ Copy \]](#)
- Table of PID codes:** [\[File 1\]](#) , [\[File 2\]](#) (retrieved pages) or Appendix A in old Manual.
- **Main papers:**
  - ⊙ RQMD.RMF approach:
 

Y. Nara, "Sensitivity of the excitation functions of collective flow to relativistic scalar and vector meson interactions in the relativistic quantum molecular dynamics model RQMD.RMF"  
[Physical Review C 100, 054902 \(2019\)](#), arXiv: [1906.03537](#)
  - ⊙ JAM (1<sup>st</sup> paper):
 

Y. Nara et al. "Relativistic nuclear collisions at 10A GeV energies from p+Be to Au+Au with the hadronic cascade model"  
[Physical Review C 64, 024901 \(1999\)](#), arXiv: [nucl-th/9904059](#)

- **On the NPD FUW's training computer:**

```
mkdir jam2 ; cd jam2
cp -r /home/kpiasecki/soft/jam2/ctnp/* .
```

**Let's inspect the input file, e.g. :**

```
less jam.inp
```

**Collection of input options** (*please consider them thoughtfully*) :

[ [This short Manual](#) ]

(for Jam1, see § 4.6 of [this Manual](#))

**Let's run the simulation** (here: in the background . Log goes into file `mysim.log` )

```
nohup nice ./runjam.sh 1>mysim.log 2>&1 &
```

**We've got the file `phase.dat.gz` with subsequent events containing particles. Unzip & view:**

```
gzip -d phase.dat.gz
less phase.dat
```

- Input file `jam.inp` :

```
Main:numberOfEvents = 10
Random:seed = 3668752

Cascade:TimeStepSize = 0.10
Cascade:TimeStep = 200

MeanField:mode=14
MeanField:potentialType = 3
MeanField:EoS= 32 # =31:NS1, =32:NS2 ...
MeanField:gaussWidth = 2.0
```

```
111:mayDecay = off      ! pi0
221:mayDecay = off      ! eta
...
Beams:beamA = 197Au
Beams:beamB = 197Au
Beams:eCM = 4.5

#Beams:beamA = 208Pb
#Beams:beamB = 208Pb
#Beams:eLab = 158

Beams:bmin = 4.6
Beams:bmax = 9.4
```

- Output file `phase.dat` :

Table of PID codes

#	2000	0.82165	0.67597	1.35698	2								
#	1	223	25	21	9.10	36	58	43					
1	2112	1	9.3960E-2	-7.4691E-2	4.6286E-3	-9.9425E-2	1.3700E+0	-7.8427E+0	3.5348E+0	-1.6458E+1	3.0200E+1	3.0200E+1	
1	2112	1	9.3960E-2	-4.2849E-2	2.0180E-2	-8.9590E-2	1.3145E+0	-6.7592E+0	9.4156E+0	-1.7980E+1	3.0200E+1	3.0200E+1	
1	2212	1	9.3960E-2	-1.1528E-2	2.2750E-2	-8.4282E-2	1.2676E+0	-7.5301E+0	5.3435E+0	-1.6708E+1	3.0200E+1	3.0200E+1	
1	2112	5	9.3957E-2	3.0711E-2	2.4778E-2	-2.6403E-2	1.0527E+0	4.7449E+0	5.2862E+0	-4.7811E+0	3.0200E+1	3.0200E+1	
{...}													
1	111	8	1.3498E-1	1.4090E-1	-1.5388E-1	-1.4472E-1	2.8757E-1	2.5947E+0	-5.0680E+0	-8.0321E+0	3.0200E+1	3.0200E+1	
#	2	227	78	62	7.12	85	152	124					
1	2212	1	9.3960E-1	-2.1659E-2	1.1828E-1	-5.13744E-1	1.0776E+0	-6.4530E+0	4.1473E+0	-9.0628E+0	3.0200E+1	3.0200E+1	
1	2212	1	9.3960E-1	4.0508E-2	-1.0861E-1	-7.09055E-1	1.1827E+0	6.2874E-2	-6.4578E-1	-1.1831E+1	3.0200E+1	3.0200E+1	
		↕		↕									
		mass		$p_x$	$p_y$	$p_z$	$E$						