### Before the Big Bang? Penrose's Conformal Cyclic Cosmology

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- Our Universe had a beginning. This beginning is called the Big Bang.
- Our Universe, as observed now, is expanding. Moreover, the measurments of cosmological constant, obtained by calibrating cosmological distances using certain type of supernovae, show that it will be expanding forever. Cosmological constant is positive.

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- Universe is the same **everywhere in space** (Copernicus) and is the same **in every direction** (Friedman/ Lemaître/ Robertson/ Walker).
- Friedmann used the **Einstein equations** (with cosmological constant equal to zero) to get a model compatible with these assumptions.
- We have only three models.

#### Copernican principle

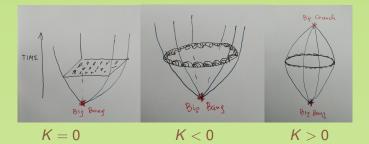
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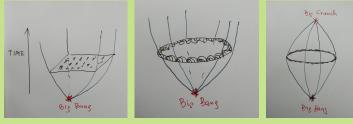
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# Friedman: three models of cosmology satisfying Copernican principle



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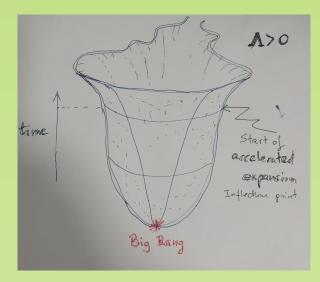
*K* < 0

K > 0

#### Three types of Riemannian geometries:



### If there is a positive cosmological cosntant the picture is a bit different



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- Applying the Second Law to the Universe, we conclude that it should be more and more random during its evolution. Going back in time, it should be more and more special. But looking at the earliest 'photograph' of the Universe - the distribution of the temperature of the Cosmic Microwave Background Radiation on the Sky we see that this distribution is extremally homogeneous. As the Universe was in a totally random stage of maximal entropy.
- One way of resolving this conundrum was to introduce (quite ad hoc) **inflationary cosmological models**.
- Another way was to try to find explanations of this fact before the Big Bang. (e.g. the Italian physicist Gabriele Veneziano who considered string theory based 'pre-Big Bang scenarios' to replace inflation).

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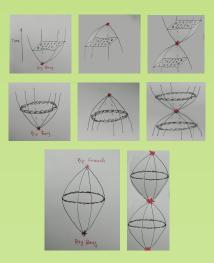
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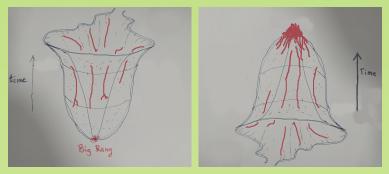
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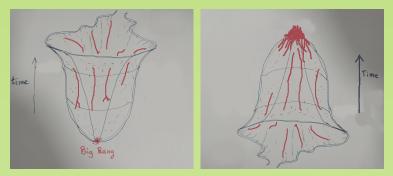
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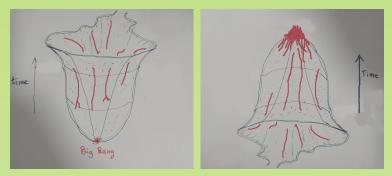
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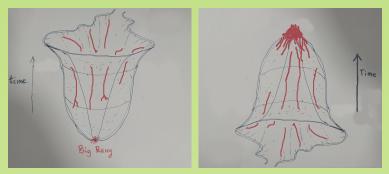
# Atempts of glueing cosmological models: Friedman Universes











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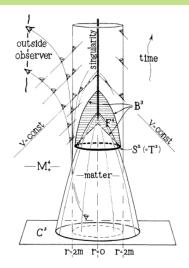


FIG. 1. Spherically symmetrical collapse (one space dimension surpressed). The diagram essentially also serves for the discussion of the asymmetrical case. What is then Penrose's answer for 'what was before the Big Bang'?

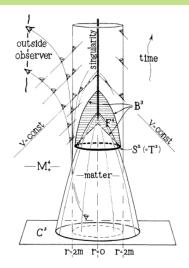
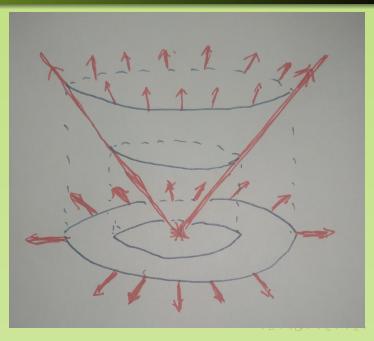


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### 'What was before the Big Bang'?: light cones



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 $E = h\nu$  (Planck) and  $E = mc^2$  (Einstein).

Combining we get <sup>ν</sup>/<sub>m</sub> = <sup>c<sup>2</sup></sup>/<sub>h</sub> = const, or that the time T - the reciprocity of the frequency ν - is

$$T = m^{-1}$$

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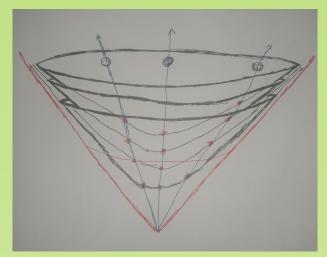
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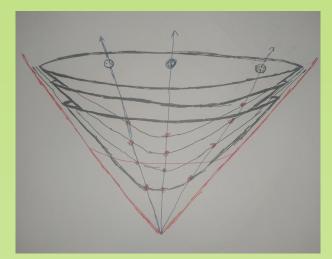
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#### 'What was before the Big Bang'?: measuring time



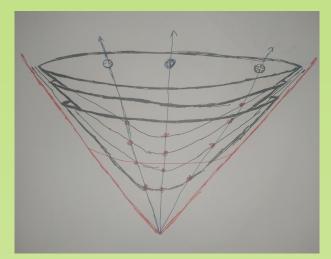
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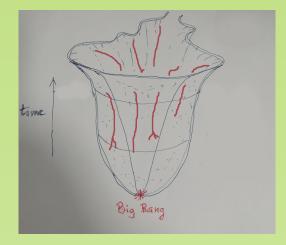
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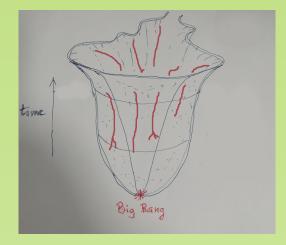
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- It will be that old that stable particles, such as protons will decay (10<sup>34</sup> years), will be that old that even **supermassive black holes** will Hawking-evaporate (google years ~ 10<sup>100</sup> years), all masses vanish, **only massless particles remain**.
- Universe will loose the notion of time!
- Out of the 10 functions defining spacetime structure of the Universe, only 9 will remain.
- Universe will pass from the phase of being equipped with the geometry of a **metric** into the phase when it is equipped with the **conformal geometry only**. The phase of a **conformal** Universe will start. Penrose: very boring era!

- From this moment the Universe will still live infinitely long aproaching asymptotically the **conformally flat** deSitter spacetime.
- Because of the positive cosmological constant
   conformal boundary of the Universe - the hypersurface where all the light rays (and other null geodesics) tend to - will be spacelike.
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- If we strip off the conformal factor from the spacetime metric of the Big Bang it becomes flat, and the hypersurface of the Big Bang will be spacelike.
- So the hypersurface of the Big Bang of The Univesre is conformally flat and spacelike preatty much the same as the last hypersurface of the dying Universe!

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- By chosing conformal factor Ω in a way such that it tends to infinity when the space shrinks to zero we can make the size of the space finite. Conformal stretching.
- One can still choose a conformal factor compatible with the other two choices, so that the entire time of the Universe is strached to a closed interval!

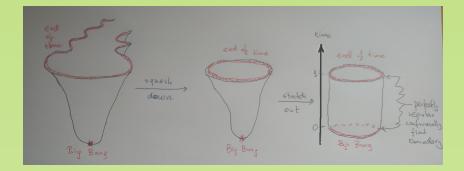
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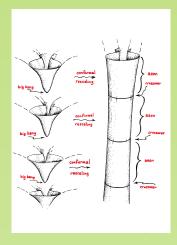
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# 'What was before the Big Bang'?: conformal tricks - the result



# 'What was before the Big Bang'?: Conformal Cyclic Cosmology



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 The Universe consists of eons, each being a time oriented spacetime, whose conformal compactifications have spacelike *I*. The Weyl tensor of the metric on each *I* is zero.

- CCC says **nothing** about this what is the physics in a given eon when the physical age of it **is normal**; **normal** meaning that eon is neither **too young** nor **too old**. CCC tells what is going on when an eon is **either about to die**, **or had just been born**.
- In particular, CCC does not require that the eons have the same history! It is Conformal Cyclic Cosmology, and not Conformal Periodic Cosmology!

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- The Universe consists of eons, each being a time oriented spacetime, whose conformal compactifications have spacelike *I*. The Weyl tensor of the 4-metric on each *I* is zero.
- Eons are ordered, and the conformal compactifications of consecutive eons, say the past one and the present one, are glued together along *I*<sup>+</sup> of the past eon, and *I*<sup>-</sup> of the present eon.
- The vicinity of the matching surface (the wound) of the past and the present eons – this region Penrose calls bandaged region for the two eons – is equipped with the following three metrics, which are conformally flat at the wound:
  - a Lorentzian metric g which is regular everywhere,
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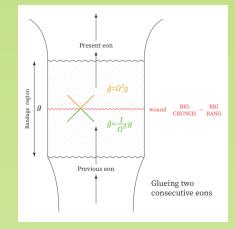
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- The vicinity of the matching surface (the wound) of the past and the present eons – this region Penrose calls bandaged region for the two eons – is equipped with the following three metrics, which are conformally flat at the wound:
  - a Lorentzian metric g which is regular everywhere,
  - a Lorentzian metric *ğ*, which represents the physical metric of the **present eon**, and which is **singular** at the wound,
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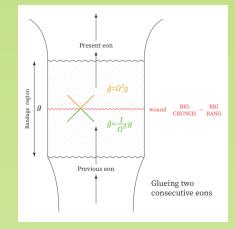
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# Penrose's Conformal Cyclic Cosmology: bandage region



# Penrose's Conformal Cyclic Cosmology: bandage region



- In a bandage region, the three metrics g, ğ and ĝ, are conformally related on their overlaping domains.
- How to make this relation specific is debatable, but Penrose proposes that

 $\check{g} = \Omega^2 g$ , and  $\hat{g} = \frac{1}{\Omega^2} g$ , with  $\Omega \to 0$  on the wound.

- The metric ğ in the present eon is a physical metric there. Likewise, the metric ĝ in the past eon is a physical metric there.
- Of course, the metric ğ in the present eon, and the metric *ĝ* in the past eon, as physical spacetime metrics, should satisfy Einstein's equations in their spacetimes, respectively.

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# Penrose's Conformal Cyclic Cosmology: is it true?

# **CAN WE SEE IT?**

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- There is a class of intrinsically defined
   Lorentz-metric-geometric-objects that are also conformal-geometric-objects.
- Even if the conformal factor of the metric is not defined as in the case of bare conformal geometry - they are good objects of conformal geometry.
- These, in particular, are null geodesics.
- In General Relativity Theory they model worldlines of the massless particles. Such as photons.
- So photons, and more generally radiation carried by massless particles, have no obstacles to traverse the boundaries of eons!
- In principle we could see photons from the previous eon!
- Crazy idea because...

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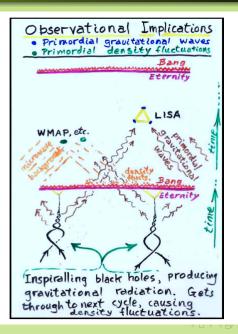
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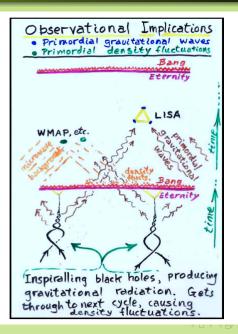
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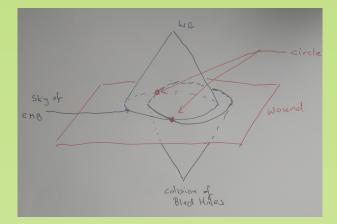
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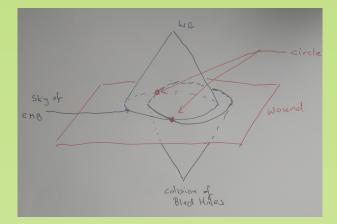
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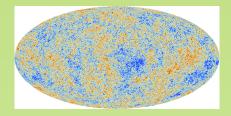
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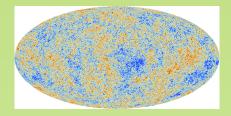


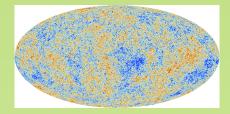


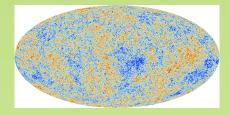


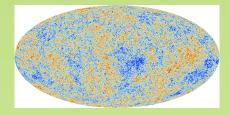




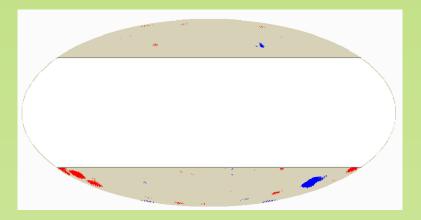






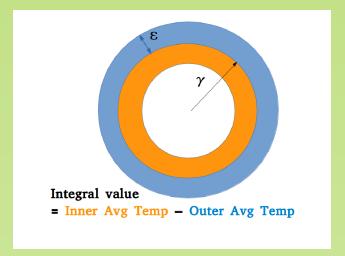


# Exclusion of the Milky Way belt



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# **Ring definition**



# Then

$$I_{(\epsilon,\gamma_k)}(\theta^i,\phi^i) = \sum_{M_-} \frac{\Delta T_m}{N_-} - \sum_{M_+} \frac{\Delta T_m}{N_+}$$

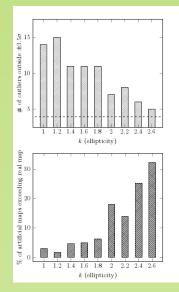
The first sum runs over all points that belong to the inner circle (between γ - ε and γ) and the second sum runs over the outer circle (between γ and γ + ε)

- 300 artificial maps have been created
- the overlap integrals for each γ and each ε were calculated around 960 points on the real maps (WMAP: W2; Planck: masked, noise cleaned 100 GHz) and all artificial maps (with k = 10 grid approximately 12 million points).
- the same was done for nonvanishing ellipticity  $\kappa$ :  $\kappa = 1.2-2.6$

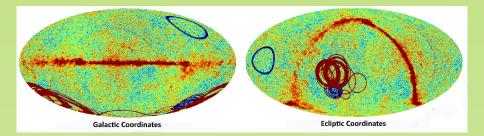
# Results I

- for each γ and each ε the extremal values (positive and negative) of the overlap integrals for circles were found for the real map
- the same was done for nonvanishing ellipticity  $\kappa$ :  $\kappa = 1.2-2.6$  (ellipses oriented in polar coordinates)
- it was determined how many artificial maps have extremal values more positive (more negative) than the extremal values on the real map
- histograms were generated

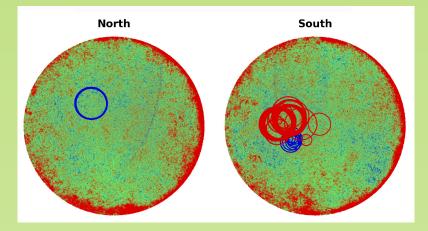
# Histogram for $\gamma = 0.3, \ \epsilon = 0.08$



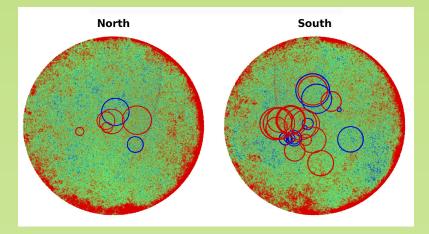
# Location of possible circles



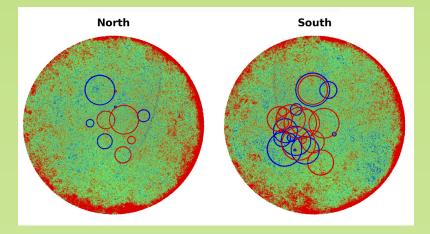
# Location of possible circles $\epsilon = 0.08$



# Location of possible circles $\epsilon = 0.04$



# Location of possible circles $\epsilon = 0.02$



# THANK YOU!