# How the green light was given for gravitational wave search

Paweł Nurowski

Center for Theoretical Physics Polish Academy of Sciences

Simons Center for Geometry and Physics 14 December 2016 Einstein and Rosen story









3 Towards green lights: 1957-1962



#### Gravitational waves: Einstein and Rosen 1937 - plane waves are unphysical

#### ON GRAVITATIONAL WAVES.

BY

#### A. EINSTEIN and N. ROSEN.

#### ABSTRACT.

The rigorous solution for cylindrical gravitational waves is given. For the convenience of the reader the theory of gravitational waves and their production, already known in principle, is given in the first part of this paper. After encountering relationships which cast doubt on the existence of *rigorous* solutions for undulatory gravitational fields, we investigate rigorously the case of cylindrical gravitational waves. It turns out that rigorous solutions exist and that the problem reduces to the usual cylindrical waves in euclidean space.

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#### Einstein A, Rosen N, *On* gravitational waves, Journ. of Franklin Institute, 223, (1937).

has the same sign. Progressive waves therefore produce a secular change in the metric.

This is related to the fact that the waves transport energy, which is bound up with a systematic change in time of a gravitating mass localized in the axis x = 0.

Note.—The second part of this paper was considerably altered by me after the departure of Mr. Rosen for Russia since we had originally interpreted our formula results erroneously. I wish to thank my colleague Professor Robertson for his friendly assistance in the clarification of the original error. I thank also Mr. Hoffmann for kind assistance in translation.

A. EINSTEIN.

### People: Albert Einstein (14.3.1879-18.04.1955)



## People: Nathan Rosen (22.3.1909-18.12.1995)



#### Historian: Daniel Kennefick



## Einstein Versus the *Physical Review*

A great scientist can benefit from peer review, even while refusing to have anything to do with it.	th for tic
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Daniel Kennefick	th
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Daniel Kennefick is a visiting assistant professor of physics at the University of Arkansas at Fayetteville and an editor with the Einstein Papers Project at the California Institute of Technology.

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this matter.

On 30 July, Tate replied that he regretted Einstein's decision to withdraw the paper, but stated that he would

September 2005 Physics Today 43

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- The result mentioned in the letter to Born was submitted to the Physical Review on 1st June 1936 in a paper under the title 'Do Gravitational Waves Exist?' coauthored by Rosen.
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• Einstein and Rosen made an ansatz on something that they belived to be a **plane wave**; the ansatz was:

$$g = e^{2\phi} (\mathrm{d}\tau^2 - \mathrm{d}\xi^2) - u^2 (e^{2\beta} \mathrm{d}\eta^2 + e^{-2\beta} \mathrm{d}\zeta^2)$$

- then the Einstein equations Ric(g) = 0 imposed on the unknown functions  $\beta$  and  $\phi$  reduced to:  $\phi' = u\beta'^2$  and  $u\beta'' + 2\beta' u^2\beta'^3 = 0$ .
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#### Daniel Kennefick look at the logbook of Phys. Rev. from 1936:



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## Gloom and doom period: 1937-1956

## **RED LIGHTS!**

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- Obes the so defined plane wave exist as a solution to the full Einstein system?
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## People: Hermann Bondi (1.11.1919-10.9.2005)



H. Bondi with P. Bergman (Warsaw 1962)



H. Bondi with L. Infeld (Warsaw 1962)

#### Bondi 1957 - Einstein and Rosen not right

#### Plane Gravitational Waves in General Relativity

POLARIZED plane gravitational waves were first discovered by N. Rosen<sup>1</sup>, who, however, came to the conclusion that such waves could not exist because the metric would have to contain certain physical singularities. More recent work by Taub<sup>3</sup> and McVittie<sup>3</sup> showed that there were no unpolarized plane waves, and this result has tended to confirm the view that true plane gravitational waves do not exist in empty space in general relativity. Partly owing to this, Scheidegger<sup>4</sup> and I<sup>5</sup> have both expressed the opinion that there might be no energycarrying gravitational waves at all in the theory. It is therefore of interest to point out, as was first. Bondi H, *Plane gravitational waves in General relativity*, Nature, 179, (25.5.1957)

It is therefore of interest to point out, as was first shown by Robinson<sup>6</sup> and has now been independently proved by me, that Rosen's argument is invalid and that true gravitational waves do in fact exist. Moreover, it is shown here that these waves carry energy, although it has not yet been possible to relate the intensity of the wave to the amount of energy carried.

gravitational waves will be published elsewhere. H. Bondi

King's College, Strand,

London, W.C.2. March 24.

- <sup>1</sup> Rosen, N., Phys. Z. Sovjet Union, 12, 366 (1937). See also, Einstein, A., and Rosen, N., J. Franklin Inst., 223, 43 (1937).
- <sup>3</sup> Taub, A. H., Ann. Math., 58, 472 (1951).
- <sup>4</sup> McVittle, G. C., J. Rational Mech. and Analysis, 4, 201 (1955).
- <sup>4</sup> Scheidegger, A. E., Rev. Mod. Phys., 25, 451 (1953). See also Brdička, M., Proc. Roy. Irish Acad., 54, 137 (1951).
- \* Bondi, H., various contributions to discussions at the International Conference on Gravitation, Chapel Hill, N.C., 1957.
- \* Robinson, I. (to be published shortly).
- <sup>\*</sup> Pirani, F. A. E., Phys. Rev., 105, 1089 (1957).
- \* Lichnerowicz, A., "Théories relativistes de la gravitation et de l'électromagnétisme" (Paris, 1955).

## People: Felix Pirani (2.2.1928-31.12.2015)



## People: Ivor Robinson (7.10.1923-27.05.2016)



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H. Bondi with I. Robinson (Warsaw 1962) I. Robinson with A. Trautman (Trieste 1985)
#### Bondi, Pirani, Robinson 1958

Gravitational waves in general relativity III. Exact plane waves

> By H. BONDI\* AND F. A. E. PIRANI† King's College, London

> > and I. Robinson

Lately of University College of Wales, Aberystwyth

(Communicated by W. H. McCrea, F.R.S.-Received 18 October 1958)

Plane gravitational waves are here defined to be non-flat solutions of Einstein's empty spacetime field equations which admit as much symmetry as do plane selectromagnetic waves, namely, a 5-parameter group of motions. A general plane-wave metric is written down and the properties of plane wave space-times are studied in detail. In particular, their charactertration as "plane" is justified further by the construction of "andwish waves" bounded on both sides by (null) hyperplanes in flat space-time. It is shown that the passing of a sandwish waves produces a valative acceleration in free test particles, and inferred from this that such waves transport energy. Bondi H, Pirani F A E, Robinson I *Gravitational waves in General relativity III. Exact plane waves*, Proc. R. Soc. London, ser. A, 251, (18.10.1958)

- motivated by the analogy with electromagnetism, where plane waves have a 5-dimensional group of symmetries they defined a plane wave in the full GR theory as a solution to the equations Ric(g) = 0, which has precisely
   5-dimensional group of symmetries
- inspecting **Petrov**'s list of solutions to Ric(g) = 0 with high symmetries they found a unique class of solutions that have 5 symmetries; the class is given in terms of **one free complex function** f = f(u), **differentiable in a real variable** u; the real and imaginary part of f is related to the **amplitude** and **polarization** of the wave, which therefore can be **modulated**
- this enables to produce waves of a sandwich type; they have shown that a sandwich wave falling on a system of test particles affects their motion, concluding that plane waves carry energy.

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## Bondi, Pirani, Robinson 1958



FIGURE 1. Arrangement of co-ordinate systems around sandwich wave.

- (1) What is a definition of a plane gravitational wave in the full theory? SOLVED!
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was in *Einstein spaces which are mapped conformally on each* other, Mathem. Annalen, 94, (1925). Actually he had more general solution depending on a complex function  $f = f(u, \zeta)$  holomorphic in complex variable  $\zeta$ . This solution is called **pp-wave**. Plane wave is a special case! Totally **overlooked by the physicists!** 

#### Einstein spaces which are mapped conformally on each other.

Von

H. W. Brinkmann in Cambridge (Mass., U.S.A.).

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 $ds^2 = 2dx dy + 2d\varphi d\theta + m d\varphi^2.$ 

To this we apply the final equation (41b) which gives us  $\frac{\partial^2 m}{\partial x \partial y} = 0$  so that  $m = X(x, \varphi) + Y(y, \varphi).$ 

The only surviving components of the Riemann tensor are here

$$R_{x \varphi \varphi x} = \frac{1}{2} \frac{\partial^2 X}{\partial x^2}, \qquad R_{y \varphi \varphi y} = \frac{1}{2} \frac{\partial^2 Y}{\partial y^2}$$

so that the  $V_4$  is Euclidean if and only if

 $X = a_1 x + b_1$ ,  $Y = a_2 y + b_2$ ,

where  $a_1$ ,  $b_1$ ,  $a_2$ ,  $b_2$  are functions of  $\varphi$ .

Thus we can go on constructing Einstein spaces that can be mapped upon Einstein spaces in more and more ways.

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#### Closer to the green: Pirani 1957

## Pirani F A E, Invariant Formulation of Gravitational Radiation Theory, Phys. Rev. 105, (18.10.1956)

PHYSICAL REVIEW

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FEBRUARY 1, 1957

#### Invariant Formulation of Gravitational Radiation Theory

F. A. E. PIRANI

Department of Mathematics, King's College, Strand, London, England (Received October 18, 1956)

In this paper, gravitational radiation is defined invariantly within the framework of general relativity theory. The definition is arrived at by assuming (a) that gravitational radiation is characterized by the Riemann tensor, and (b) that it is propagated with the fundamental velocity. Therefore a gravitational wave front should appear as a discontinuity in the Riemann tensor across a null 3-surface; the possible form of this discontinuity is here calculated from Lichnerowicz's continuity conditions.

The concept of an observer who follows the gravitational field is defined in terms of the eigenbivectors of the Riemann tensor. It is shown that the 4-velocity of this observer is timelike for one of Petrov's three canonical types of Riemann tensor, but null for the other two types. The first type is identified with the absence of radiation, the other two with its presence. This constitutes the definition. It is shown that the difference between the no-radiation type and one of the radiation types can be made to correspond to the discontinuity possible across a null 3-surface; this demonstrates the consistency of the wave front and following-the-field concepts.

A covariant approximation to the canonical energy-momentum pseudo-tensor is defined, using normal coordinates, which are given a physical interpretation. It is shown that when gravitational radiation is present, the approximate gravitational energyflux cannot be removed by a local Lorentz transformation, which supports the definition of radiation.

It is proved that, as would be demanded of a sensible definition, there can be no gravitational radiation present in a region of empty space-time where the metric is static.

- Pirani had an idea that radiative solutions of the Einstein's equations should be characterized by the properties of the curvature tensor *Riemann(g)* of the metric g;
- he postulated that the proper condition on *Riemann(g)* is that in a radiative spacetime **it is algebraically special**, according to the **Petrov classification**
- Pirani did not know all **Petrov types**, which were spelled out in full generality by **Roger Penrose**, few years later; he did not made his statement precise: it was **unclear which Petrov type he attributes to gravitational radiation**
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#### Pirani 1957 - Petrov classification

Table 4.3.	The roots of the	algebraic equation	(4.18) and	their multiplicities
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The corresponding multiplicities of the principal null directions are symbolically depicted on the right of this table.

Type	Roots $E$	Multiplicities	
I	$\frac{\sqrt{\lambda_2+2\lambda_1}\pm\sqrt{\lambda_1+2\lambda_2}}{\sqrt{\lambda_1-\lambda_2}}$	(1,1,1,1)	V.
D	$0, \infty$	(2,2)	$\square$
11	$0,\pmi\sqrt{\tfrac{3}{2}\lambda}$	(2,1,1)	$\mathbb{Z}$
III	$0, \infty$	(3,1)	
N	0	(4)	$\hat{\blacksquare}$

Nowadays, due to our **next hero**, we know that a gravitational wave is of Petrov type N far from the sources (asymptotically).

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## People: Andrzej Trautman





A. Trautman with S. Chandrasekhar (Warsaw 1973)

#### Green lights: Trautman 1958

BULLETIN DE L'ACADÈMIE POLONAISE DES SCIENCES Série des sci. math., astr. et phys. — Vol. VI, No. 6 1958

THEORETICAL PHYSICS

Boundary Conditions at Infinity for Physical Theories

#### A. TRAUTMAN

Presented by L. INFELD on April 12, 1958

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The purpose of this paper is to formulate boundary conditions for scalar and Maxwell theories in a form which exhibits their physical meaning and is proper to a generalization for the gravitational case. BULLETIN DE L'ACADÉMIE POLONAISE DES SCIENCES Série des sci. math., astr. et phys. - Vol. VI, No. 6 1338

THEORETICAL PHYSICS

Radiation and Boundary Conditions in the Theory of Gravitation

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• [1] Trautman A, *Boundary conditions at infinity for physical theories* Bull. Acad. Polon. Sci., 6, (12.04.1958)

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- apropriately reformulate boundary conditions for radiative solutions of the relativistic wave equation for a scalar field known as Sommerfeld's radiation conditions (Courant, Hilbert, Methods of Mathematical Physics, vol.2, p. 315)
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 In it Trautman defines the boundary conditions for a radiative spacetime in full GR theory. This is a definition of gravitational radiation. This is in [2], on p. 409, equations (9) and (10).

> We generalize the conditions of Fock along the lines presented in the preceding paper. First, introduce a null vector field k, defined as follows. Let  $n^*$  be a unit space-like vector lying in  $\sigma$ , perpendicular to the "sphere" r = const., and pointing outside it. We put  $k^* = n^* + t^*$ , where t denotes a unit time-like vector normal to  $\sigma$ , such that  $t^* > 0$

> Now, we formulate the following boundary conditions to be imposed on gravitational fields due to isolated systems of matter: there exist co-ordinate systems and functions  $h_{\mu\nu} = O(r^{-1})$  such that

(9) 
$$g_{\mu\nu} = \eta_{\mu\nu} + O(r^{-1}), \quad g_{\mu\nu,\varrho} = h_{\mu\nu}k_{\varrho} + O(r^{-2})$$

(10) 
$$(h_{\mu\nu} - \frac{1}{2} \eta_{\mu\nu} \eta^{\rho\sigma} h_{\rho\sigma}) k^{*} = O(r^{-2})$$

These conditions correspond to Sommerfeld's "Ausstrahlungsbedingung"; we obtain the "Einstrahlungsbedingung" assuming n to be a normal pointing inward the sphere r = const. Relations (9), (10) are

- the metric coefficients behave as g<sub>μν</sub> = η<sub>μν</sub> + O(1/r), with r being one of the coordinates x<sup>μ</sup> interpreted as an affine parameter along geodesics escaping to infinity (spatial or null)
- metric's first derivatives behave as  $g_{\mu\nu,\rho} = v_{\mu\nu}k_{\rho} + O(1/r^2)$ with a null vector  $k^{\mu}$ , and with  $v_{\mu\nu} = O(1/r)$
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#### Trautman 1958 - remarks on boundary conditions

#### Lichnerowicz:

Let us take an isolated system of masses ( $T_{\mu\nu} = 0$  outside a bounded 3-region) and assume the existence of co-ordinates such that [5]

 $g_{\mu r} = \eta_{\mu r} + O(r^{-1}), \quad g_{\mu r, \varrho} = O(r^{-2}),$ 

where r denotes the distance measured along geodesics from a fixed point on a space-like  $\sigma$ . Eqs. (6) have a double meaning: they constitute a sy-

#### Trautman:

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#### Trautman 1958 - reformulation of Einstein's equations

a statistical terms  $T_{\mu\nu}$  does not by itself lead to an integral conservation law. However, if we introduce an energy-momentum pseudotensor of the gravitational field  $t_{\mu}^{*} = (\delta_{\mu}^{*} \oplus g^{*}_{\mu\nu}) \delta_{\mu}^{*} g^{*}_{\mu\nu}) 2\varkappa$ , then the sum  $T_{\mu}^{*} + t_{\mu}^{*}$  is divergenceless by virtue of Einstein's equations \*). Einstein's tensor density  $\mathfrak{G}_{\mu}^{*} = \sqrt{-g} (E_{\mu}^{*} - \frac{1}{2} \delta_{\mu}^{*} R)$  can namely be written in the form

(1) 
$$\mathfrak{G}_{\mu}^{*} \equiv \varkappa (\mathfrak{t}_{\mu}^{*} + \mathfrak{U}_{\mu}^{\lambda_{\mu}}, \iota),$$

where the "superpotentials"  $\mathfrak{U}_{\mu}^{\ *\lambda}$  are given in [1]

(2) 
$$2 \varkappa \mathfrak{U}_{\mu}^{\,\nu\lambda} = \sqrt{-g} g^{\sigma[\sigma} \delta^{\nu}_{\mu} g^{\lambda] r} g_{\sigma\sigma,\tau} = -2 \varkappa \mathfrak{U}_{\mu}^{\,\lambda\nu}$$

If the Einstein equations

$$G_{\mu\nu} = -\varkappa T_{\mu}$$

are satisfied, then Eqs. (1) and (2) imply

(4) 
$$\mathfrak{T}_{\mu}^{\nu} + t_{\mu}^{\nu} = \mathfrak{U}_{\mu}^{\nu^{2}}, \quad \text{thus} \quad (\mathfrak{T}_{\mu}^{\nu} + t_{\mu}^{\nu})_{,\nu} = 0.$$

The functions t<sub>n</sub>" are not components of a tensor density (equivalence principle) and many physicists (e. g., Schrödinger [2]) have raised doubts

• uses **Freud potential** 2-form  $\mathcal{F}$ , to split the Einstein tensor  $E = Ric(g) - \frac{1}{2}Rg$  into  $E = d\mathcal{F} - 8\pi t$  so that **the Einstein** equations  $E = 8\pi T$  take the form

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The functions  $t_{i}$  are not components of a tensor density (equivalence principle) and many physicists (e.  $x_r$ , Schrödinger [2]) have raised doubts as to their physical meaning. Einstein [3] and P. Klein [4] formulated some conditions which enable us to consider the integrals

5) 
$$P_{\mu}[\sigma] = \int_{\sigma} (\mathfrak{X}_{\mu}^{*} + \mathfrak{t}_{\mu}^{*}) dS_{\nu} = \int_{S} \mathfrak{U}_{\mu}^{*\lambda} dS_{\nu\lambda}$$

as representing the total energy and momentum of the system: matter and gravitational field. These conditions can be summarized as follows.

#### shows that

- $P_{\mu}(\sigma)$  is finite and
- well defined, i.e. that it does NOT depend on the coordinate systems adapted to the chosen boundary conditions, [2], pp. 409-410; he finds the most general coordinate system (BMS group)

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#### Trautman 1958 - 4-momentum of a gravitational system

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#### Trautman 1958: precursor of BMS group

Let us take a co-ordinate transformation  $x^{*} \rightarrow x^{\prime *} = x^{*} + a^{*}(x)$ (11)fulfilling  $a^{v} = o(r), \quad a_{v,u} = b_{v}k_{u} + O(r^{-2})$ (12)where  $a_r = \eta_{r\mu} a^{\mu}, \quad b_r = O(r^{-1}),$ and  $a_{r,uo} = b_{r,u}k_o + O(r^{-2}), \quad b_{r,o} = O(r^{-1}).$ (13)From (13) follows the existence of functions  $c_r = O(r^{-1})$  such that

(14) 
$$b_{r,\mu} = c_r k_{\mu} + O(r^{-2})$$
.

Co-ordinate transformations (11) satisfying (12) and (13) preserve the form of our boundary conditions; this can be easily seen from the transformation formulae for  $g_{\mu\nu}$  and  $h_{\mu\nu}$ :

(15) 
$$\begin{array}{c} g'_{\mu\nu}(x') \simeq g_{\mu\nu}(x) + b_{\mu}k_{\nu} + b_{\nu}k_{\mu}, \\ h'_{\nu\nu}(x') \simeq h_{\nu\nu}(x) + c_{\mu}k_{\nu} + c_{\nu}k_{\mu}. \end{array}$$

Computing the superpotentials in both co-ordinate systems and taking into account the relations (9)-(15) we obtain

 $\mathfrak{U}_{a}^{rd}k_{a}^{\prime}n_{1}^{\prime} = \mathfrak{U}_{a}^{rd}k_{a}n_{2} + O(r^{-3}).$ 

- calculates precisely how much of the gravitational energy *p*<sub>μ</sub> = *P*<sub>μ</sub>(σ<sub>1</sub>) - *P*<sub>μ</sub>(σ<sub>2</sub>) contained between the spacelike hypersurfaces σ<sub>1</sub> (initial one) and σ<sub>2</sub> (final one) escapes to infinity - or, in nowadays Penrose's terminology - to scri, [2], p.410-411, equations (16)-(17).
- shows that p<sub>0</sub> is NON-negative, [2], p. 411, remark after (17). Weak proof, because he is only able to prove p<sub>0</sub> ≥ 0.

4. The total energy and momentum  $p_{\mu}$  radiated between two hypersurfaces  $\sigma$  and  $\sigma'$  is given by (7), or by

$$p_{\mu} = P_{\mu}[\sigma] - P_{\mu}[\sigma'] = \int_{\Sigma} t_{\mu}^{s} dS$$

 $(T_{\mu\nu} \text{ vanishes on } \Sigma)$ . The boundary conditions enable the estimation of  $p_{\mu}$ ; we have, indeed,

(16) 
$$\mathbf{t}_{\mu}^{\nu} = \tau k_{\mu} k^{\nu} + O(r^{-3}),$$

where

(17) 
$$4\varkappa\tau = h^{\mu\nu}(h_{\mu\nu} - \frac{1}{2}\eta_{\mu\nu}\eta^{\rho\sigma}h_{\rho\sigma}).$$

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- (4) What is a definition of a gravitational wave with nonplanar front in the full theory? SOLVED!
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#### Robinson, Trautman 1960: example of peeling

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#### SPHERICAL GRAVITATIONAL WAVES\*

Ivor Robinson Department of Physics, University of North Carolina, Chapel Hill, North Carolina,

and

A. Trautman Institute of Physics, Polish Academy of Science, Warsaw, Poland<sup>†</sup> (Received March 7, 1960; revised manuscript received March 24, 1960)

If these equations are satisfied, the curvature tensor may be written as

 $R_{ijkl} = \rho^{-3} D_{ijkl} + \rho^{-2} III_{ijkl} + \rho^{-1} N_{ijkl},$ 

where  $D_{ijkl}$ ,  $\Pi_{ijkl}$ , and  $N_{ijkl}$  are tensors of type I degenerate, type III, and type II null, respectively. They are covariantly constant on any ray of constant  $\sigma$ ,  $\xi$ ,  $\eta$ .

The solution is degenerate type I if m is non-

Further consequences: Syracuse 1961

In 1961 P. Bergmann, A. Trautman, R. Penrose, J. Goldberg, R. Sachs, E. T. Newman, E. Schucking, and others met in Syracuse NY (nowadays it would be called one year postdoc), where a lot of the development happened.

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- Penrose introduced **conformal compactifications**, **Penrose diagrams**, and **scri** as a proper place to analyze radiation
- Goldberg and Sachs generalized observation of RT that their spacetimes, whose main feature was that they admit a shearfree congruence of null geodesics, are algebraically special. This led to the Goldberg-Sachs theorem
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I am grateful to the Department of Mathematics of King's College for affording me its hospitality and providing the facilities for the delivery of these lectures, and to Professor H. Bondi and Dr. F.A.E. Pirani for numerous discussions during my stay there. Most of the work reported in the lectures was carried out under a research fellowship of the Institute of Physics of the Polish Academy of Sciences. I am grateful to Professor L. Infeld and Doctor J. Plebański for guiding this work and for invaluable advice and encouragement at every stage.

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A TT		
ΪΪΙ.	Equations of motion and gravitational radiation	1
Lecture IV.	Three problems of general relativity	3
	1. Propagation of gravitational disturbances	
	<ol> <li>Conservation laws and symmetry properties of space-time</li> </ol>	
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## THANK YOU!

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