

## Table of Contents and Schedule of Presentations

NTC	Ted Carnevale
MLH	Michael Hines
WWL	Bill Lytton
TJS	Terry Sejnowski

Hands-on exercises are tagged by an asterisk \* in the Page column.  
 Times shown are approximate, except for lunch.

### Saturday, 6/21

#### Morning session

Time	Speaker	Title	Page
9:00 AM	MLH	Welcome to the NEURON summer course	7
9:15	TJS	Lost in parameter space: the art of modeling	
10:45	Coffee Break		
11:00	NTC	Introduction to modeling with NEURON	9
11:30	NTC	Example: single compartment	11 *
12:15	End of morning session		
12:30	Lunch		

#### Afternoon session

1:30	NTC	Fundamental concepts	13
2:00	MLH	Hodgkin–Huxley axon	17 *
2:45	Coffee Break		

3:00	NTC	Elementary project management	19
3:30	NTC	Ball–stick model	19 *
5:00		End of afternoon session	

## Sunday, 6/22

### Morning session

Time	Speaker	Title	Page
9:00 AM	Q & A		
9:15	MLH	Numerical methods: accuracy, stability, speed	21
10:00	NTC	An outline for coding NEURON models	33
10:30	Coffee Break		
10:45	WWL	The hoc programming language	37 *
12:15		End of morning session	
12:30	Lunch		

### Afternoon session

1:30	NTC	Model control: arbitrary forcing functions	51 *
2:30	NTC	Model control: simulation families	53 *
3:30	Coffee Break		
3:45	MLH	The Extracellular and Linear mechanisms	55 *
5:00		End of afternoon session	

**Monday, 6/23**  
**Morning session**

Time	Speaker	Title	Page
9:00 AM	Q & A		
9:15	MLH	NMODL: the NEURON Model Description Language	57 *
10:30		Coffee Break	
10:45	MLH	Kinetic scheme: potassium channel	65 *
12:15		End of morning session	
12:30		Lunch	

**Afternoon session**

1:30	MLH	Optimizing a mechanism	75 *
2:30	NTC	ModelDB: a resource for reproducibility in computational neuroscience	83 *
3:15		Coffee Break	
3:30	MLH	Kinetic scheme: calcium pump	89 *
5:00		End of afternoon session	

**Tuesday, 6/24**  
**Morning session**

Time	Speaker	Title	Page
9:00 AM	Q & A		
9:15	MLH	Variable time steps and parameter discontinuities: pulse stimulus	93 *

10:30	Coffee Break		
10:45	NTC	Networks 1: synapses	101 *
12:15		End of morning session	
12:30	Lunch		

**Afternoon session**

1:30	MLH	Networks 2: network construction	113 *
3:00		Coffee Break	
3:15	WWL	Networks 3: inhibitory synchronizing network	121 *
5:00		End of afternoon session	

**Tuesday evening: “graduation dinner”**

6:30	TBA
------	-----

**Wednesday, 6/25****Morning session**

Time	Speaker	Title	Page
9:00 AM		Q & A	
9:15	MLH	The standard run system	143
10:30		Coffee Break	
10:45	NTC	Initialization	145 *
12:15		End of morning session	
12:30	Lunch		

## Afternoon session

1:30	NTC	Working with morphometric data	153 *
2:00	NTC	NEURON's tools for analyzing electrotonus	155 *
3:15		Coffee Break	
3:30		Review discussion	
4:45		Evaluation form	
5:00		End of afternoon session	

**Survey**

**last page**

*Bound separately:*

### **NEURON: Selected Preprints**

Chapters from the latest draft of The NEURON Book



# THE NEURON SIMULATION ENVIRONMENT

M.L. Hines  
N.T. Carnevale  
W.W. Lytton  
T.J. Sejnowski

Supported by NINDS



## The What and the Why of Neural Modeling

The moment-to-moment processing of information in the nervous system involves the propagation and interaction of electrical and chemical signals that are distributed in space and time.

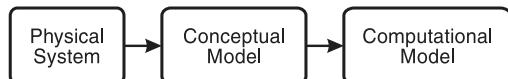
Empirically-based modeling is needed to test hypotheses about the mechanisms that govern these signals and how nervous system function emerges from the operation of these mechanisms.

## Topics

1. How to create and use models of neurons and networks of neurons
2. How NEURON works
3. How to specify anatomical and biophysical properties
4. How to control, display, and analyze models and simulation results
5. How to enhance NEURON with user-defined biophysical mechanisms

## From Physical System to Simulation

### Simulation for Insight



**Conceptual Model**  
a simplified representation  
of a complex system

**Computational Model**  
an accurate representation  
of this approximation

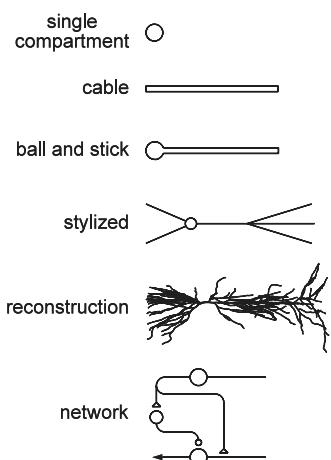
Physical System	Model	NEURON Simulation
		<code>create soma, dendrite connect dendrite(0), soma(1)</code>
CA1 pyramidal cell	ball and stick	hoc code

Figures

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## Hierarchies of Complexity

### Structure



The NEURON Simulation Environment

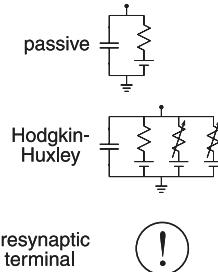
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Figures

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## Hierarchies of Complexity

### Mechanism



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Figures

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## Fundamental Concepts in NEURON

Signals	Driving Force	Flux	What is conserved
Electrical	voltage gradient	current	charge
Chemical	concentration gradient	solute	mass

The NEURON Simulation Environment

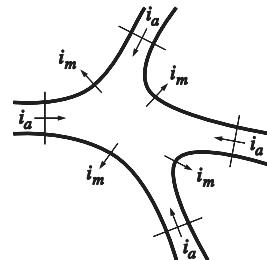
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Figures

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## Conservation of Charge

total current leaving = total current entering



$$Cm \frac{dV_m}{dt} + i_{ion} = \sum i_a$$

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## Example: Single Compartment

Lipid bilayer (no ionic channels)

Membrane with linear ion channels  
(passive leak conductance).

```
oc> insert pas ↴
```

```
oc> e_pas = 0 ↴
```

Virtual molecular biology!

Project goals:

- Run simulation, changing stimulus intensity and duration
- Insert a membrane mechanism
- Adjust graphical displays of simulation results
- Adjust dt and Points plotted / ms



Figures

Page 1

## Fundamental Concepts

What equations are being solved?

How to separate the biology from computational details?

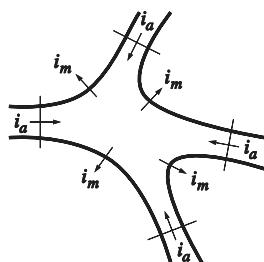
"It's all about conceptual control . . . "

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## Conservation of Charge

total current leaving = total current entering



$$Cm \frac{dV_m}{dt} + i_{ion} = \sum i_a$$

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Figures

Page 3

## The Simulation Equations

$$c_j \frac{dv_j}{dt} + i_{ion,j} = \sum_k \frac{v_k - v_j}{r_{jk}}$$

$v_j$  membrane potential in compartment  $j$

$i_{ion,j}$  net transmembrane ionic current in compartment  $j$

$c_j$  membrane capacitance of compartment  $j$

$r_{jk}$  axial resistance between the center of compartment  $j$  and the center of adjacent compartment  $k$

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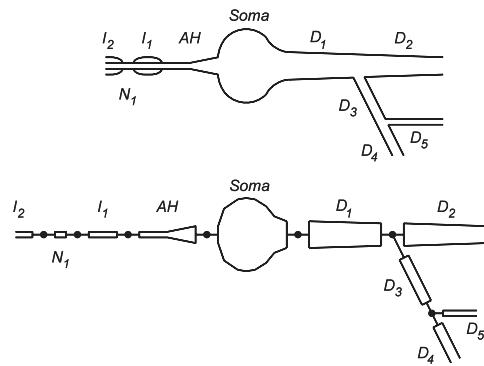
Figures

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## Separating Anatomy and Biophysics from Purely Numerical Issues

### Section

a continuous length of unbranched cable



The NEURON Simulation Environment

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Syntax: `create sectionname`

Example: `create soma, dend [3]`

creates one section named `soma`  
and an array of three sections named  
`dend[0], dend[1], and dend[2]`

Assigning anatomical and biophysical attributes:

```
soma {
    L = 50      // [um] length
    diam = 50   // [um] diameter
    insert hh
    // Hodgkin-Huxley mechanism
}
for i=0,2 dend[i] {
    L = 200
    diam = 2
    insert pas // passive channels
}
```

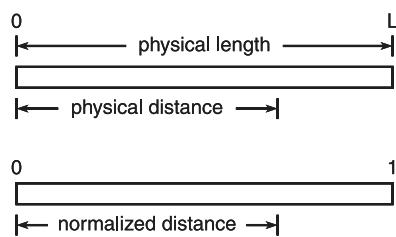
## Range Variables

Name	Meaning	Units
diam	diameter	[ $\mu\text{m}$ ]
cm	specific membrane capacitance	[ $\mu\text{F}/\text{cm}^2$ ]
g_pas	specific conductance of the <i>pas</i> mechanism	[siemens/ $\text{cm}^2$ ]
v	membrane potential	[mV]

## Range

The normalized position along the length of a section (“normalized arc length”).

$0 \leq \text{range} \leq 1$  (any variable name can be used to represent range, e.g. `x`)



Syntax:

`sectionname.rangevar(range)`

returns or sets the value of `rangevar` at the location corresponding to `range`

Examples:

`dend.v(0.5)`

returns membrane potential at the middle of a section. Shortcut: `dend.v`

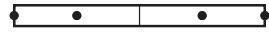
`dend for (x) print x*L, v(x)`

prints the physical distance and `v` at each point in `dend` where `v` was calculated. The results appear in the NEURON interpreter window.

**nseg**

the number of points in a section where membrane current and potential are computed

`nseg = 1` 

`nseg = 2` 

`nseg = 3` 

Example: `axon {nseg = 3}`  
or `axon.nseg = 3`

To test spatial resolution

`forall {nseg = nseg * 3}`  
and repeat the simulation.

**Units**

Category	Variable	Units
Time	$t$	[ms]
Voltage	$v$	[mV]
Current	$i$	[mA/cm <sup>2</sup> ] (distributed) [nA] (point process)
Concentration	various	[mM]
Specific capacitance	$c_m$	[ $\mu$ F/cm <sup>2</sup> ]
Length	diam, L	[ $\mu$ m]
Conductance	$g$	[S/cm <sup>2</sup> ] (distributed) [ $\mu$ S] (point process)
Cytoplasmic resistivity	$R_a$	[ $\Omega$ cm]
Resistance	$R_i()$	[ $10^6 \Omega$ ]



# Physical System



From <http://www.mbl.edu>

## Model

### Hodgkin-Huxley cable equations

$$\frac{D}{4R_a} \cdot \frac{\partial^2 V}{\partial x^2} = C_m \frac{\partial V}{\partial t} + \bar{g}_{na} m^3 h \cdot (V - E_{na}) + \bar{g}_k n^4 \cdot (V - E_k) + g_l \cdot (V - E_l)$$

$$\begin{aligned} \frac{dm}{dt} &= -\alpha_m m + \beta_m \cdot (1 - m) & \alpha_m &= \frac{.1(V+40)}{1-e^{-1(V+40)}} & \beta_m &= 4e^{-(V+65)/18} \\ \frac{dh}{dt} &= -\alpha_h h + \beta_h \cdot (1 - h) & \alpha_h &= .07e^{-0.05(V+65)} & \beta_h &= \frac{1}{1+e^{-1(V+35)}} \\ \frac{dn}{dt} &= -\alpha_n n + \beta_n \cdot (1 - n) & \alpha_n &= \frac{.01(V+55)}{1-e^{-1(V+55)}} & \beta_n &= .125e^{-(V+65)/80} \end{aligned}$$

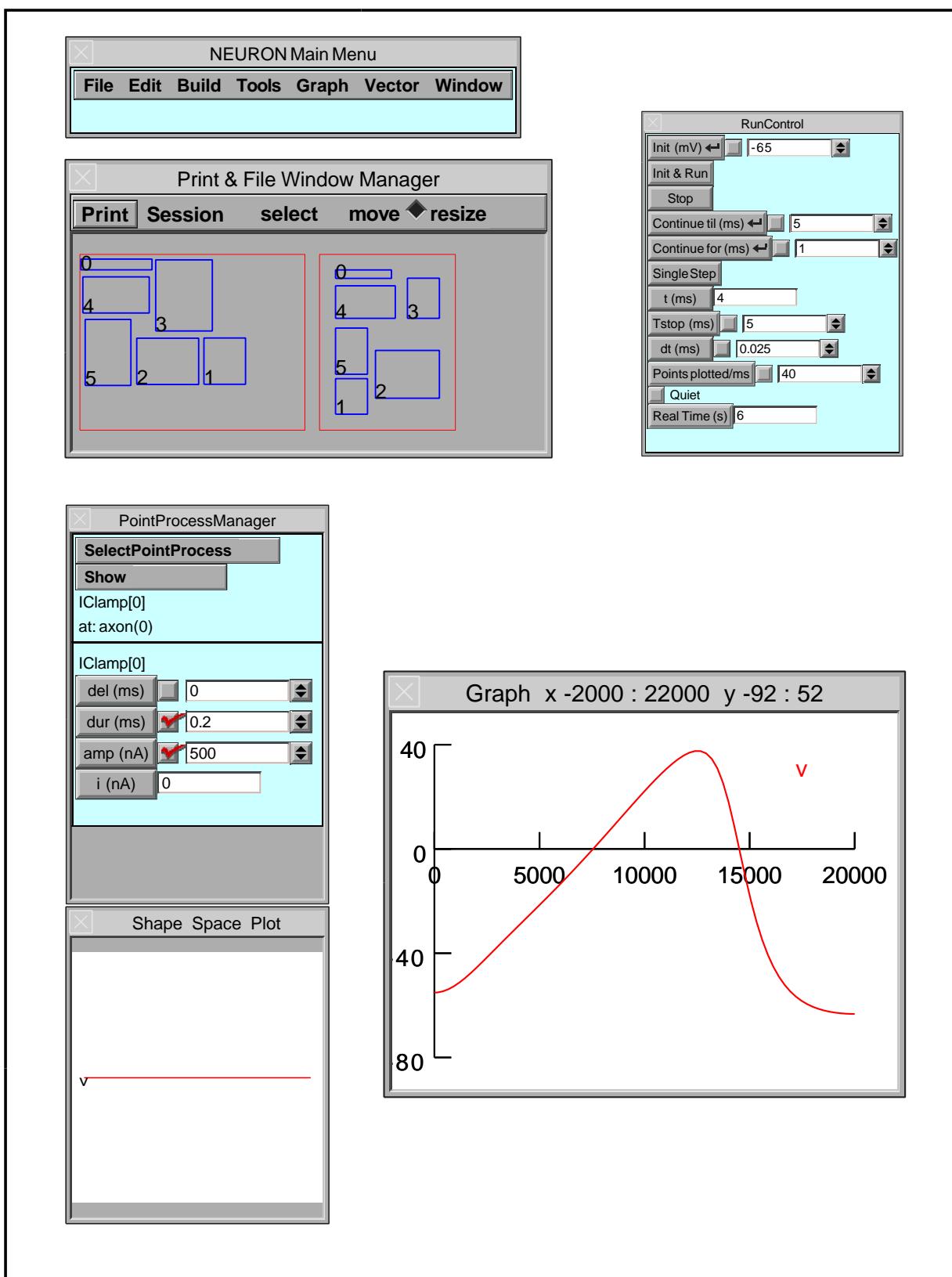
## Simulation

### Representation

```
create axon
axon {
    nseg = 50
    diam = 100
    L = 20000
    insert hh
}
```

**Run NEURON with above spec.**

Exercises



## Elementary Project Management

Keep  
 specification of the model  
 separate from  
 specification of the interface  
 in order to  
 maximize clarity and reduce effort

## Elementary Project Management

continued

`modelfile.hoc`  
 “The organism”  
 Intrinsic properties of the model:  
 topology, anatomy, biophysics.

`start.ses`  
 Eventually will contain custom interface  
 (synapses, electrodes, graphs,  
 run control, etc.)  
 Initially empty or an innocuous statement  
`print "ready"`

`init.hoc`  
 The administrative wrapper  
`load_file("nrngui.hoc")`  
`load_file("modelfile.hoc")`  
`load_file("start.ses")`

## Elementary Project Management

continued

Usage

1. Execute `init.hoc`
  - UNIX: `nrngui init.hoc`
  - MSWin: double click on `init.hoc`

This brings up NEURONMainMenu
2. Customize interface
  - Attach synapses and electrodes
  - Set up graphs and run control
3. Save interface to `start.ses`

The next time you run `init.hoc`,  
 the interface you saved in `start.ses`  
 is automatically retrieved.

## Example: Ball - Stick model

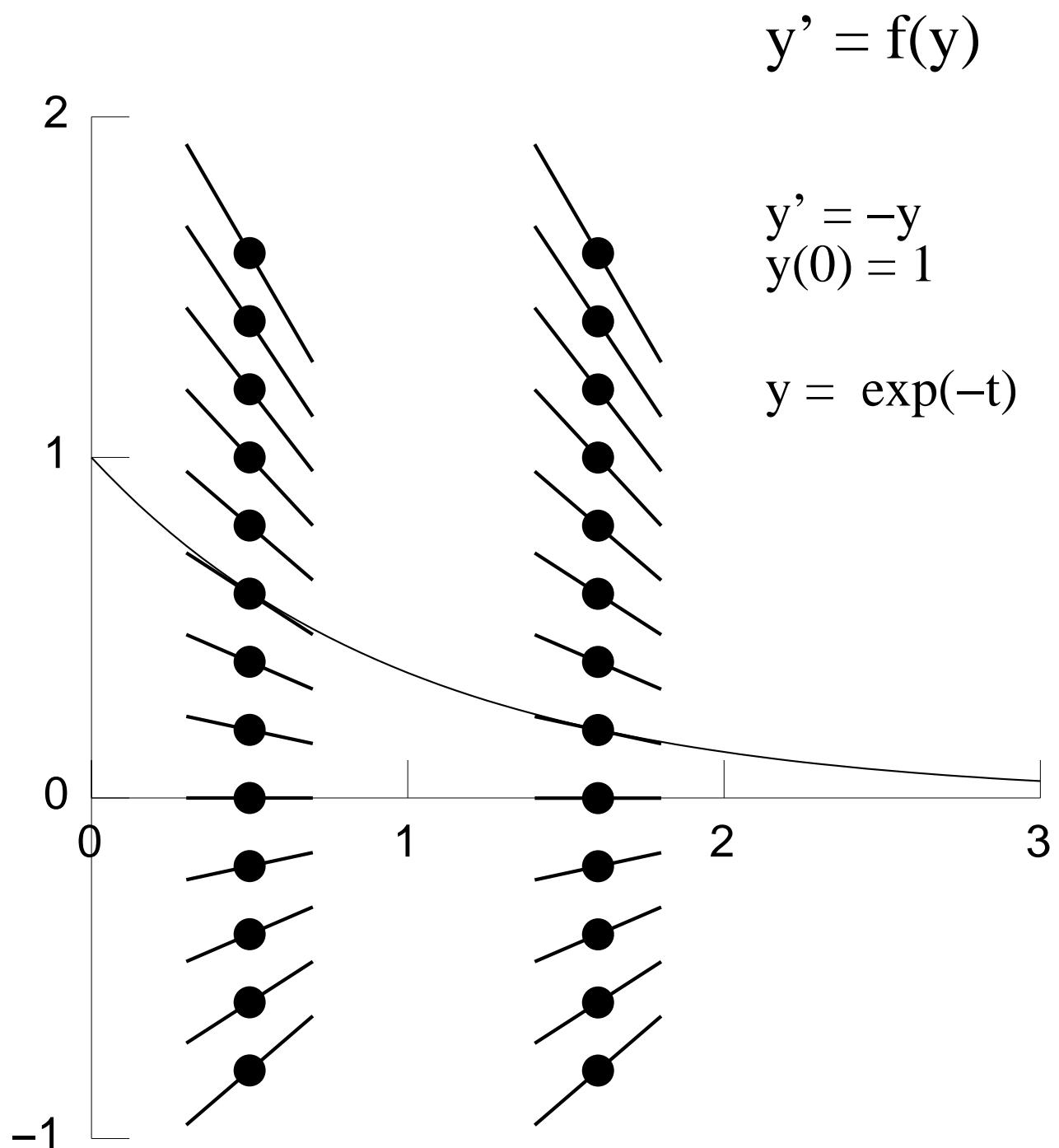
Physical system: pyramidal neuron  
 enormously complicated dendritic tree

Model: isopotential soma with dendritic cylinder

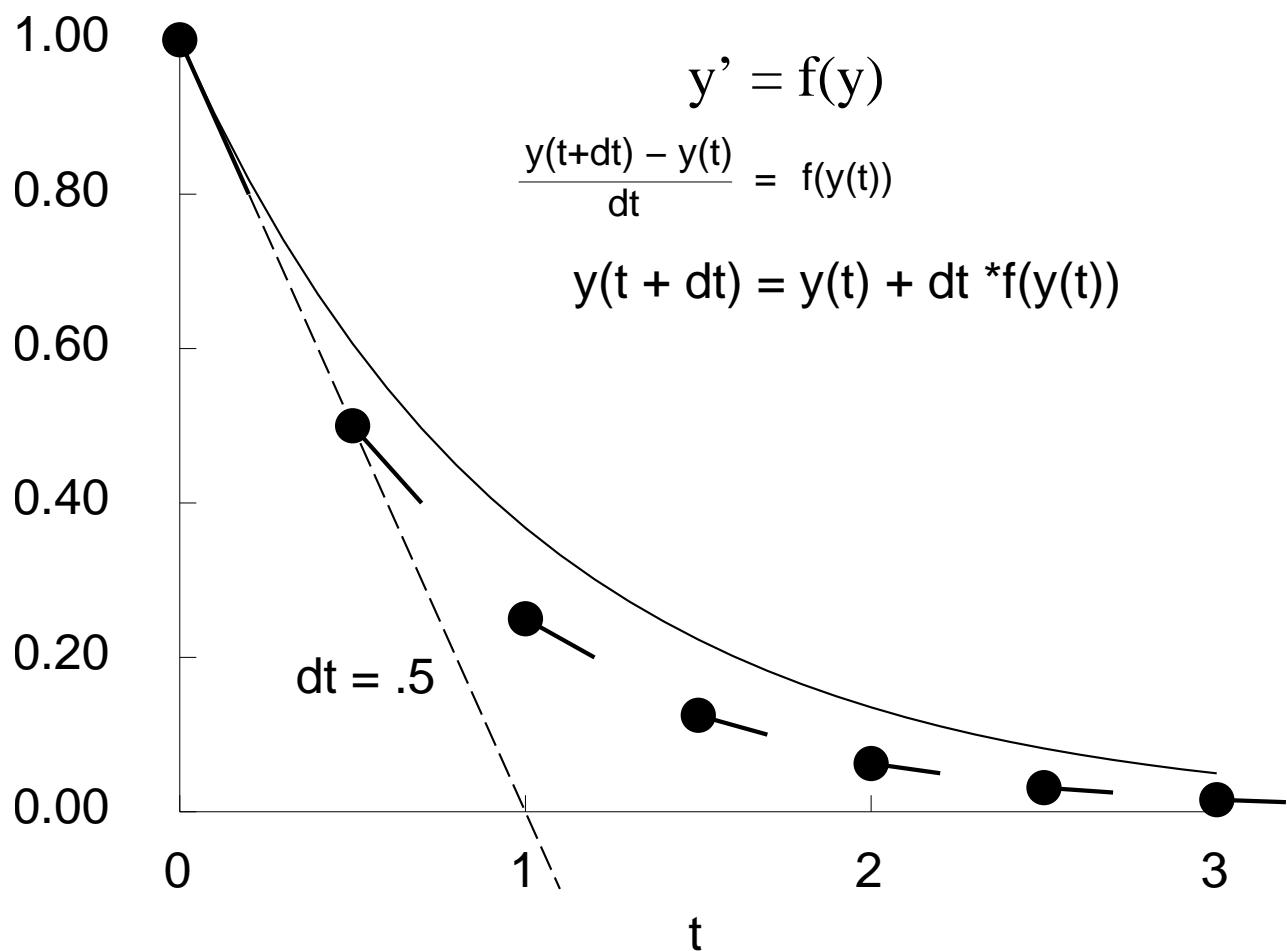
Project goals:

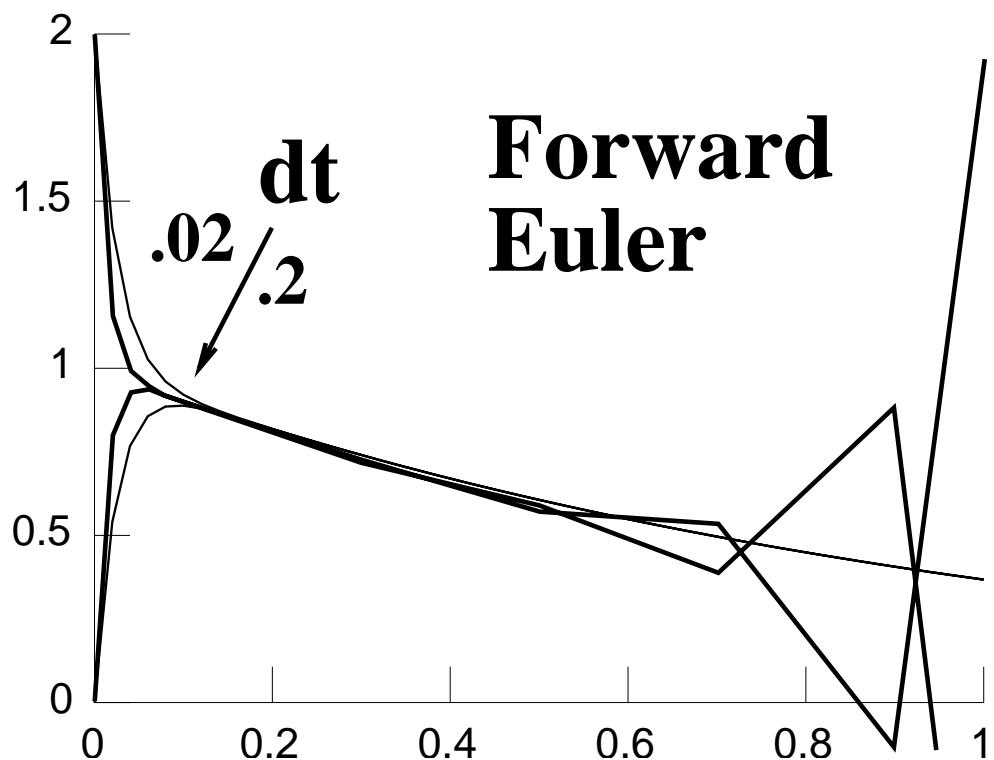
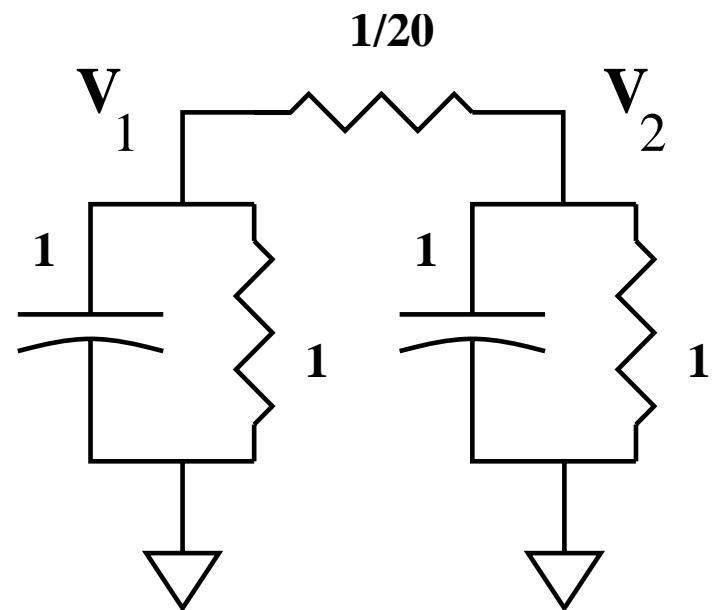
- Create the model and custom GUI from scratch.
- Learn how to use the CellBuilder.
- Use session files to save and retrieve the user interface (elementary project management).
- Test the simulation:
  - structural integrity
  - spatial grid
  - time steps



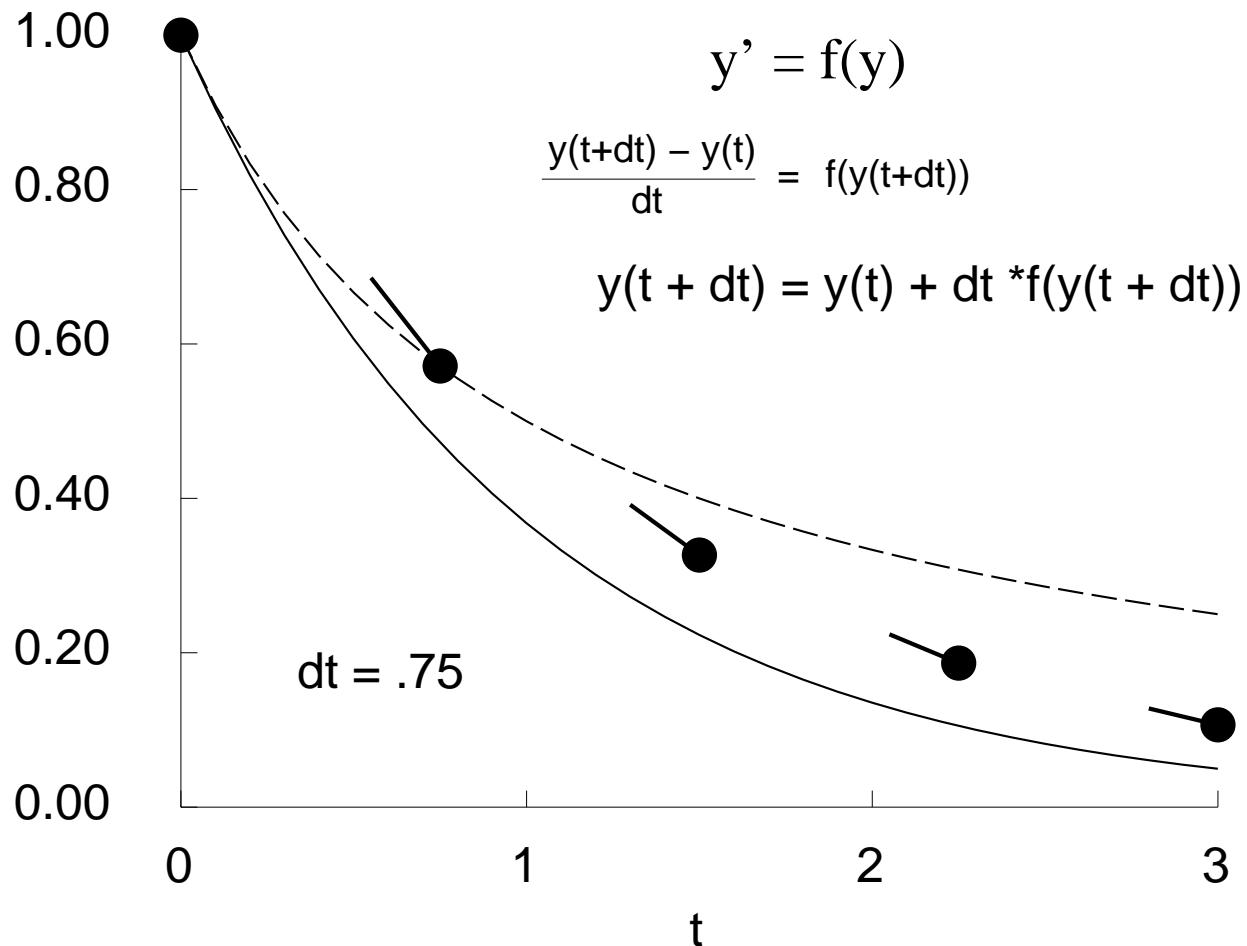


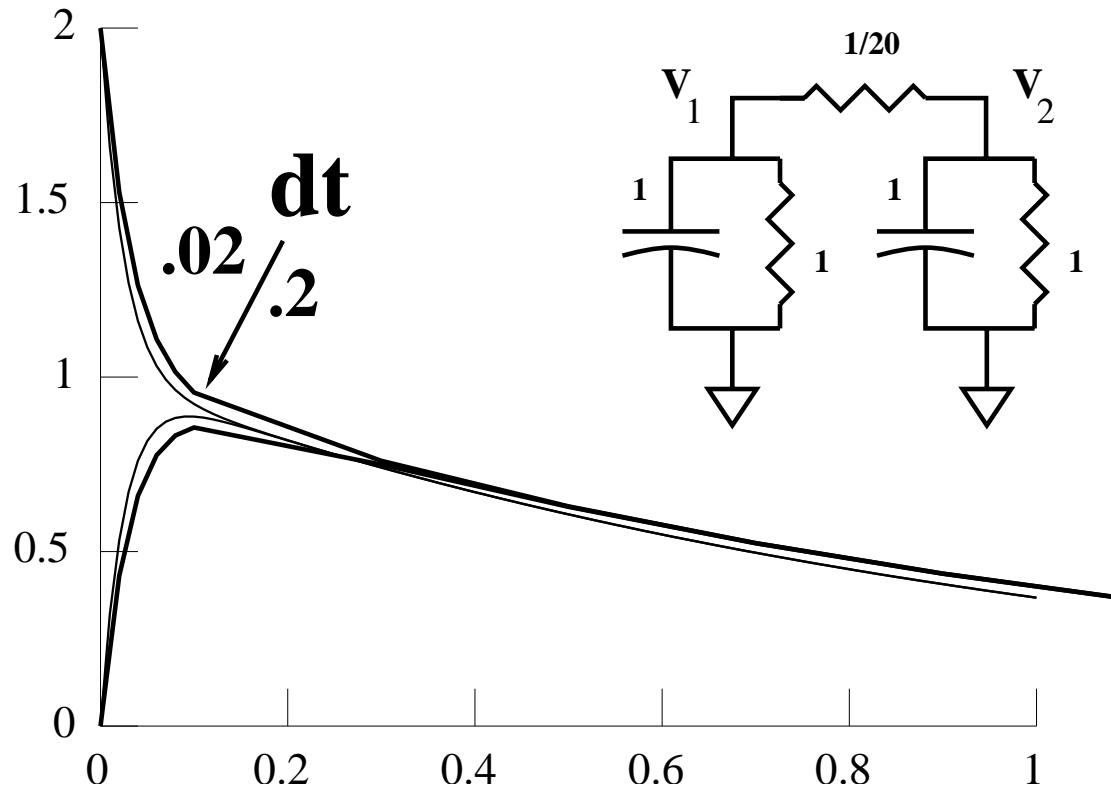
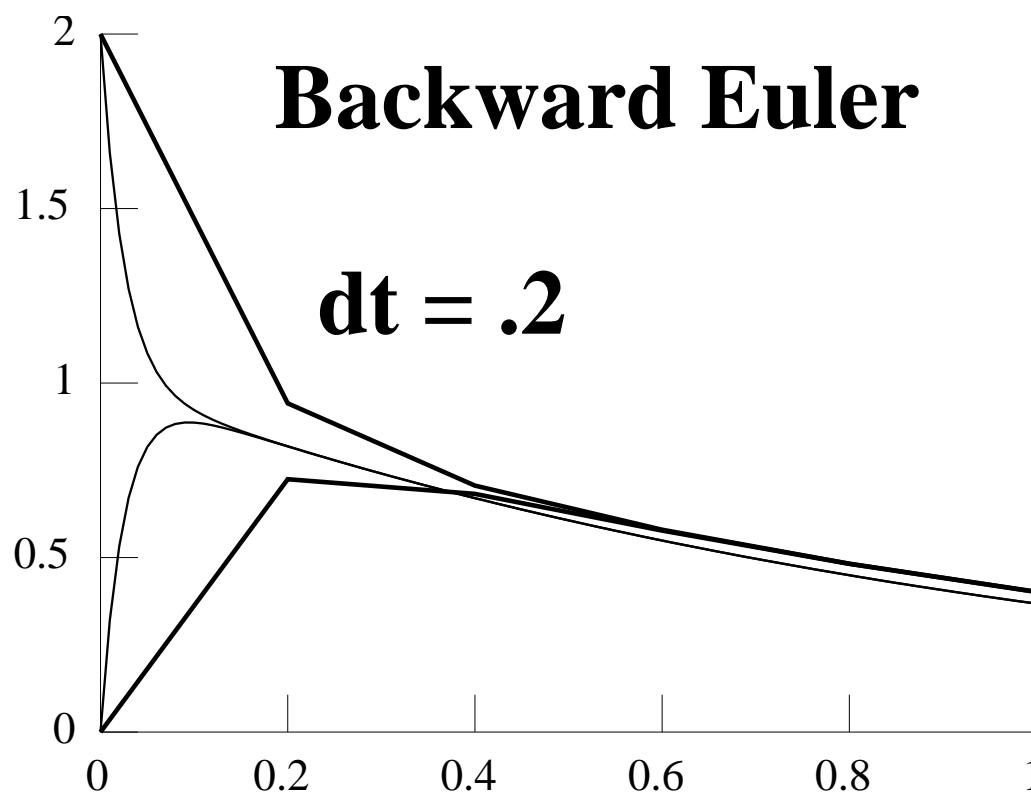
# Forward Euler



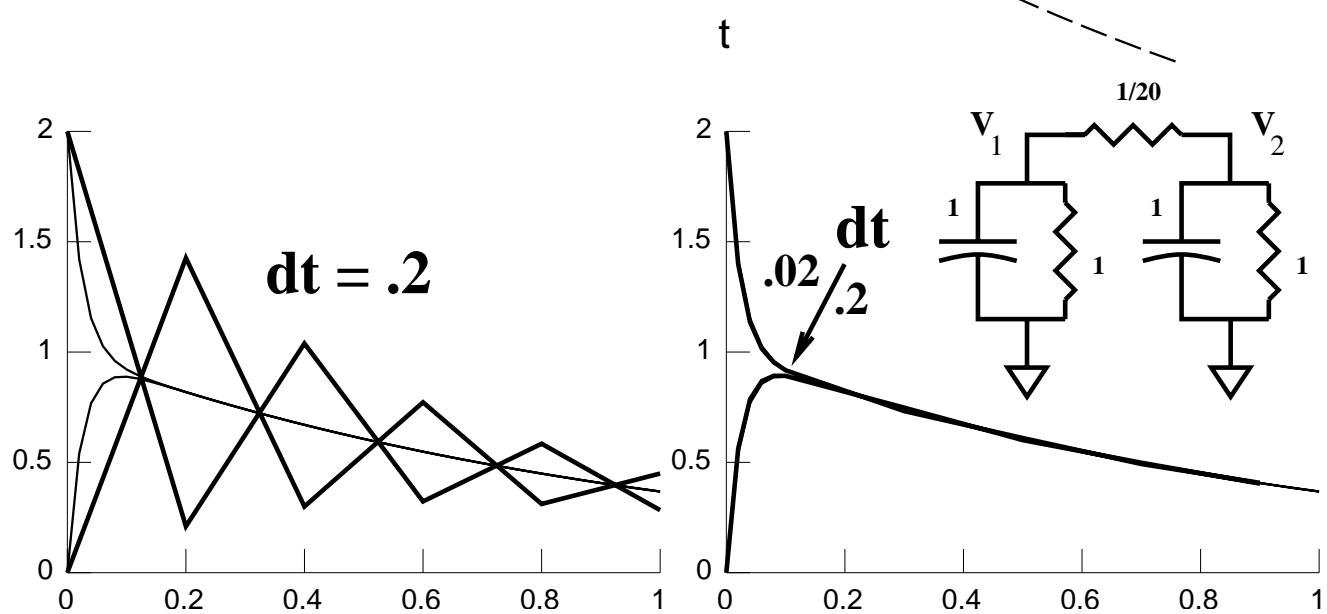
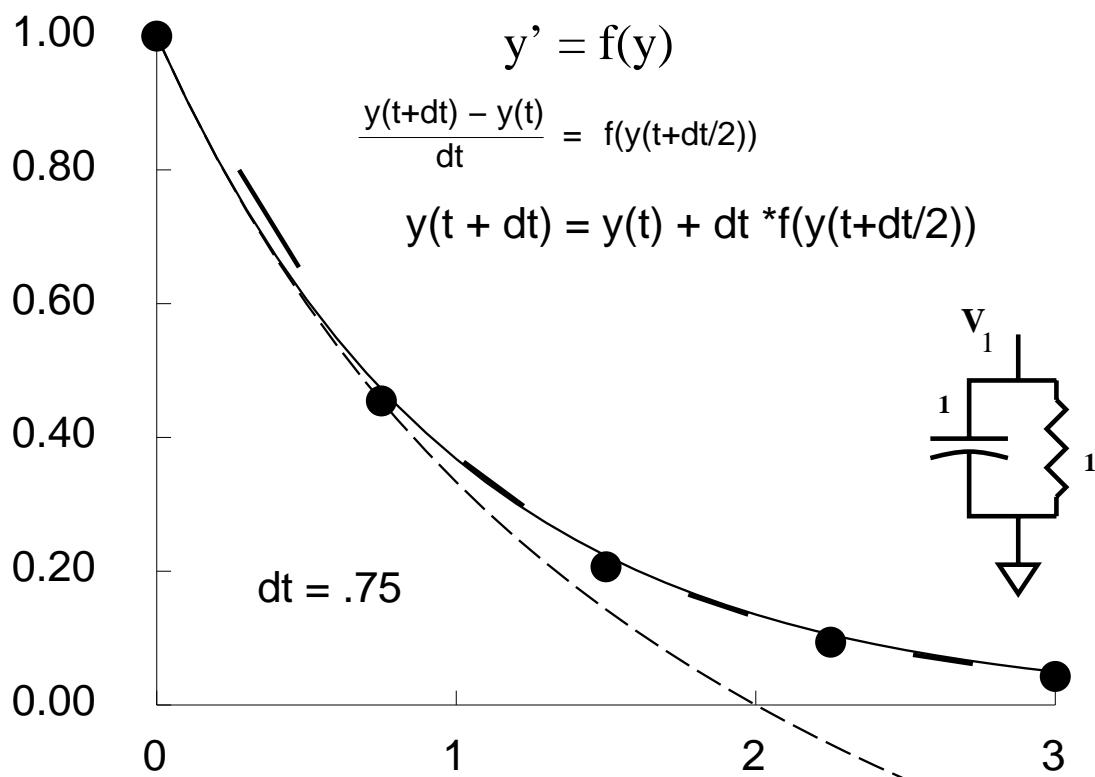


# Backward Euler

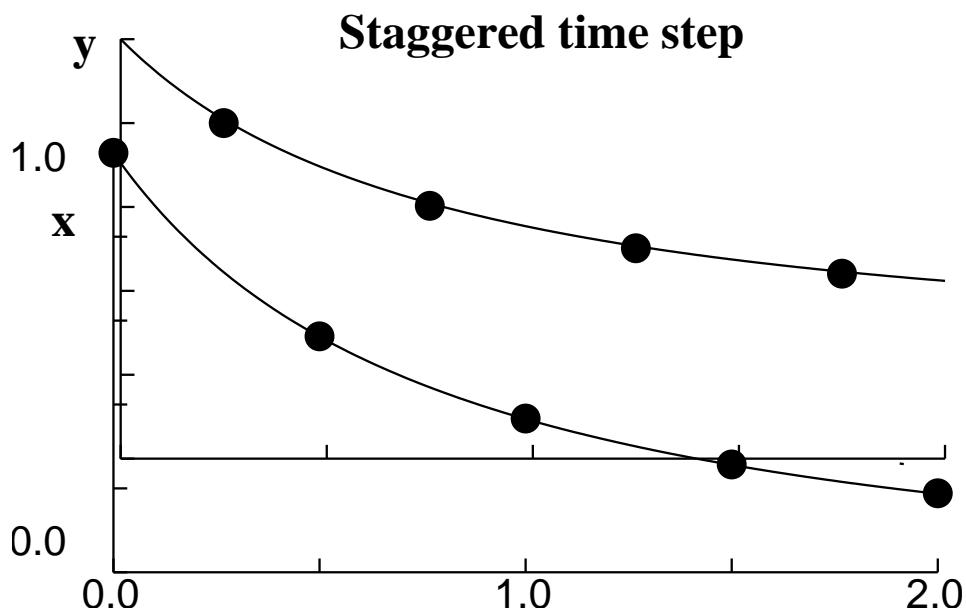
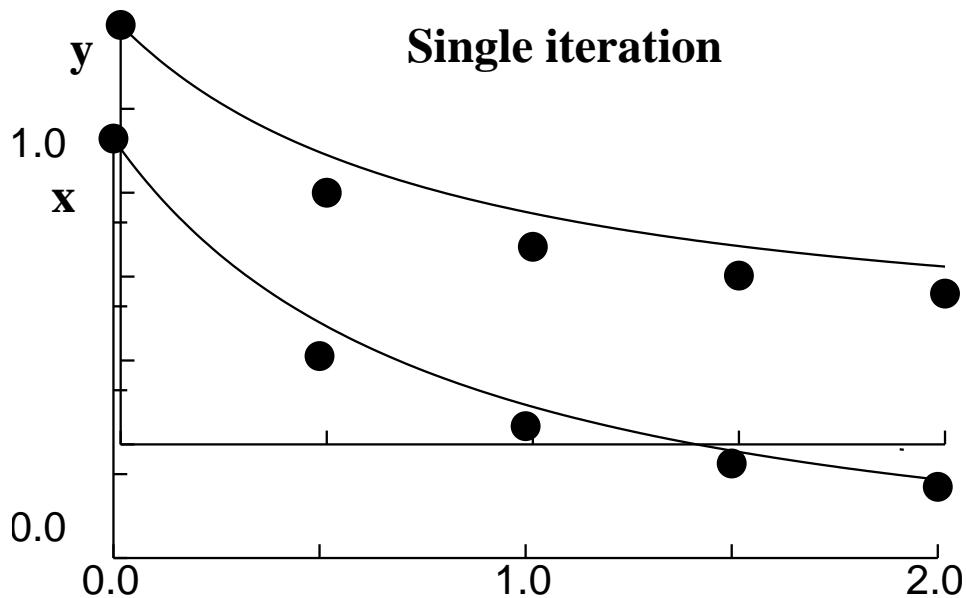


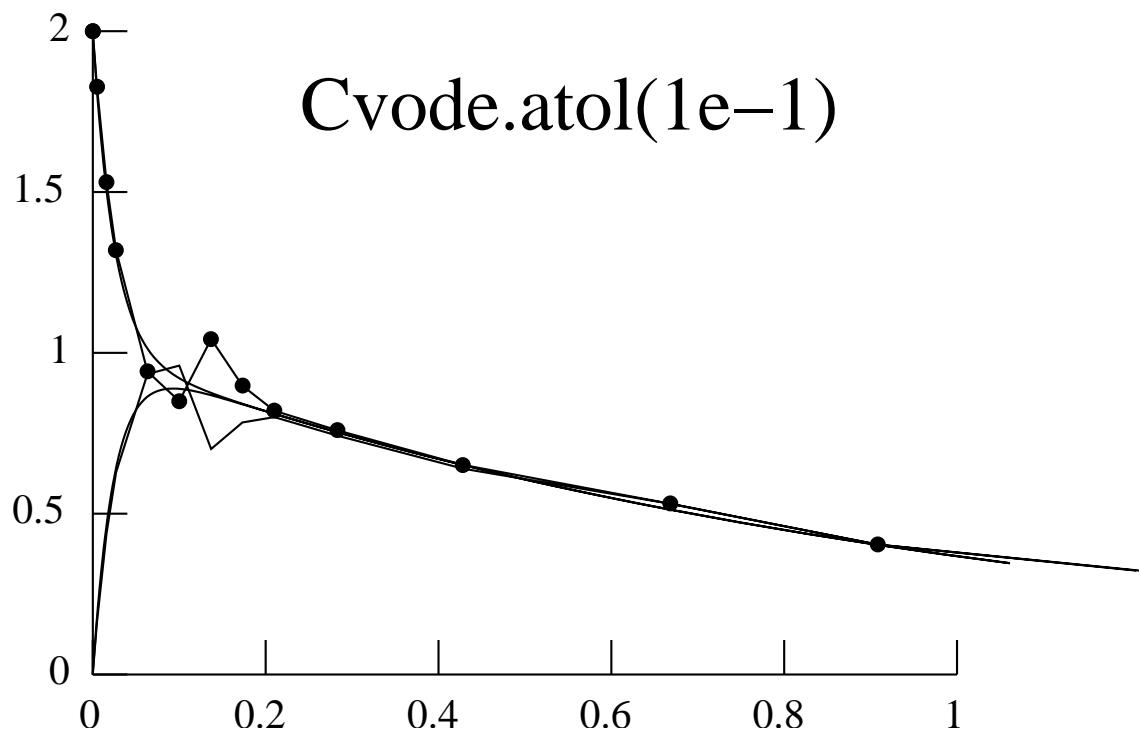
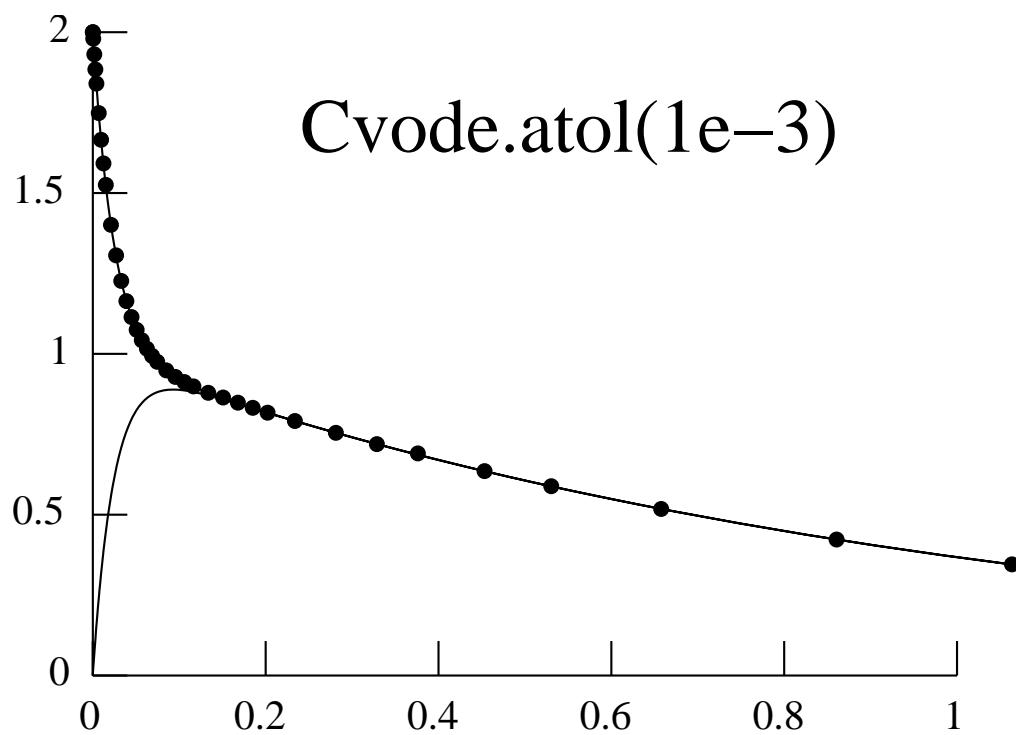


# Crank–Nicholson

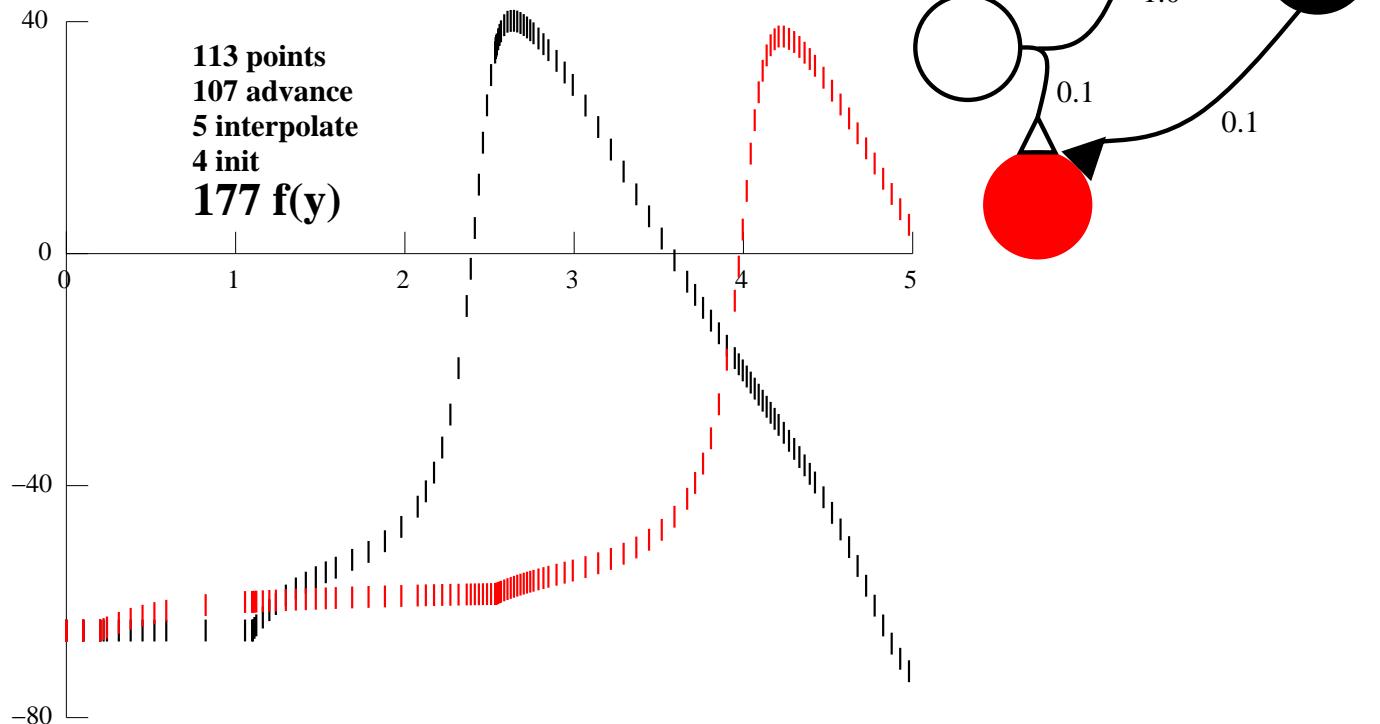


$$\begin{aligned}x' &= -1.4xy \\y' &= -xy\end{aligned}$$



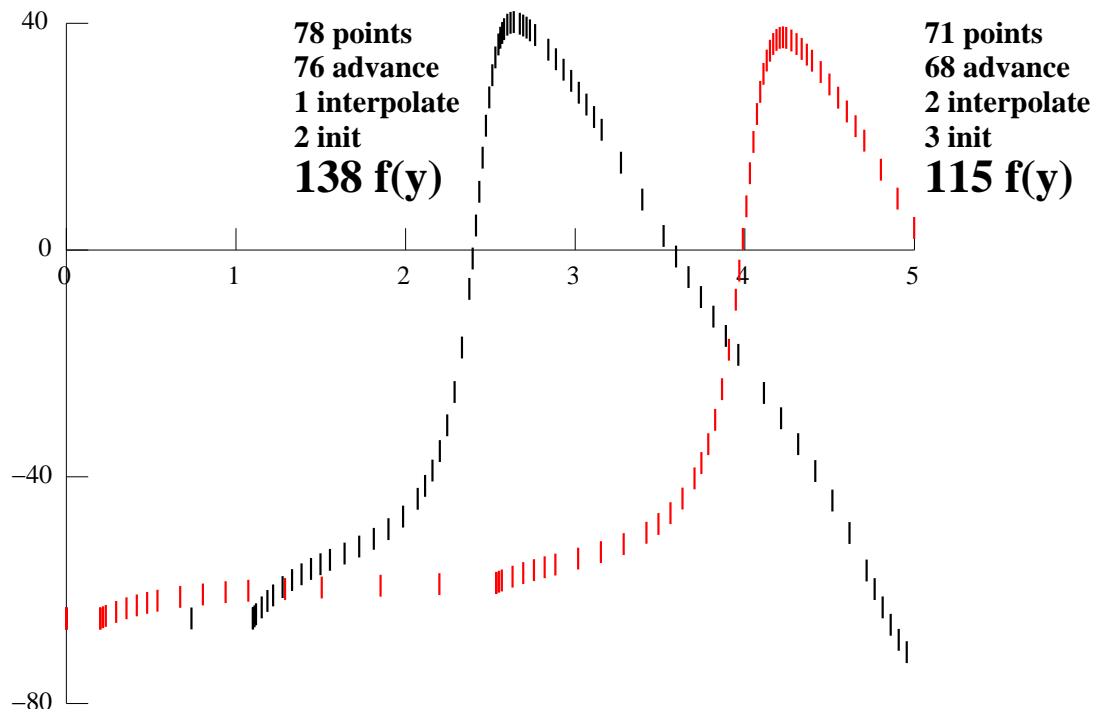


## Global Step



$$(177*8)/(138*4 + 115*4) = 1.4$$

## Local Step



# One integrator instance per cell

**t0**      **t<sub>—</sub>**    **tn**

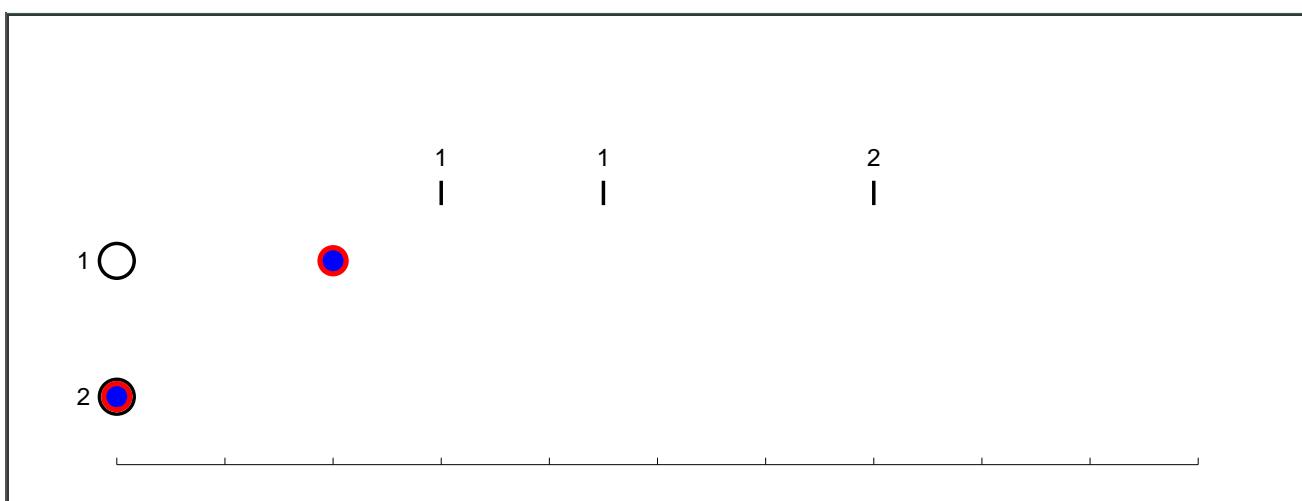
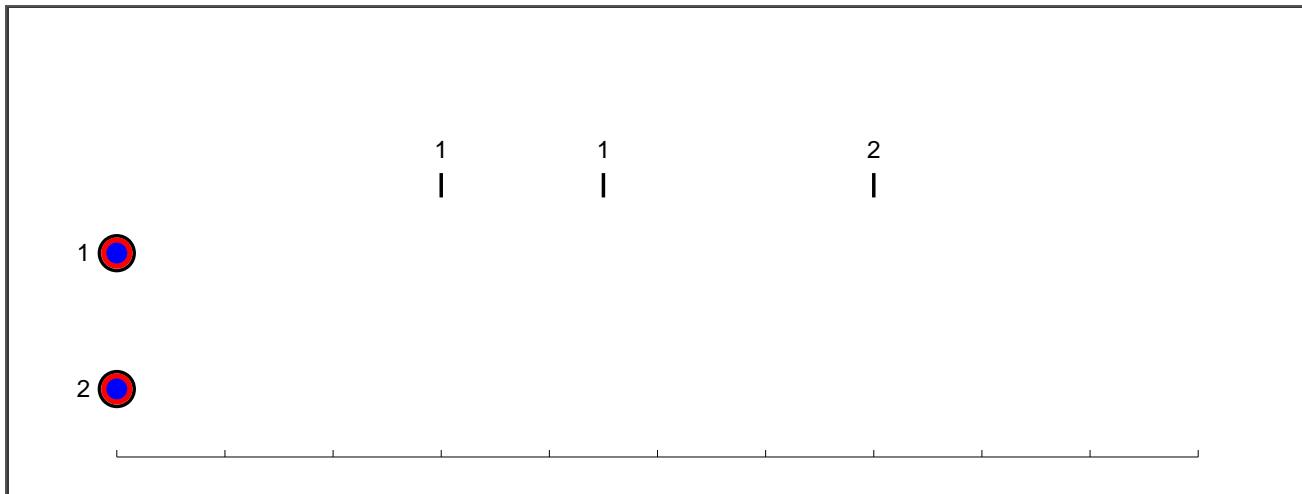


The diagram consists of three circles arranged horizontally. The first circle, labeled 't0', is empty with a black outline. The second circle, labeled 't\_—', is filled with blue. The third circle, labeled 'tn', is filled with red.

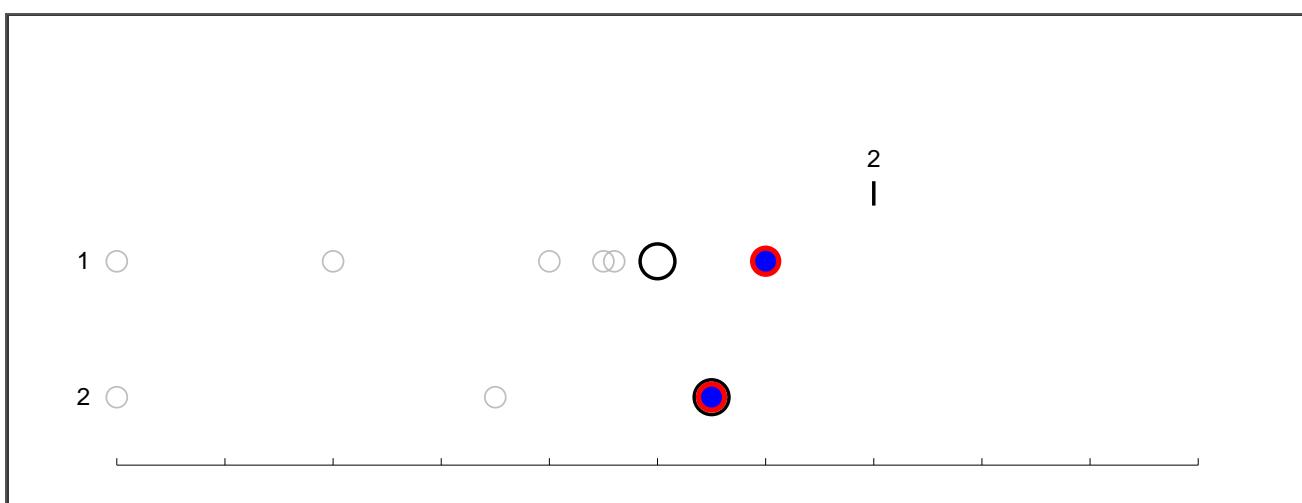
# advance

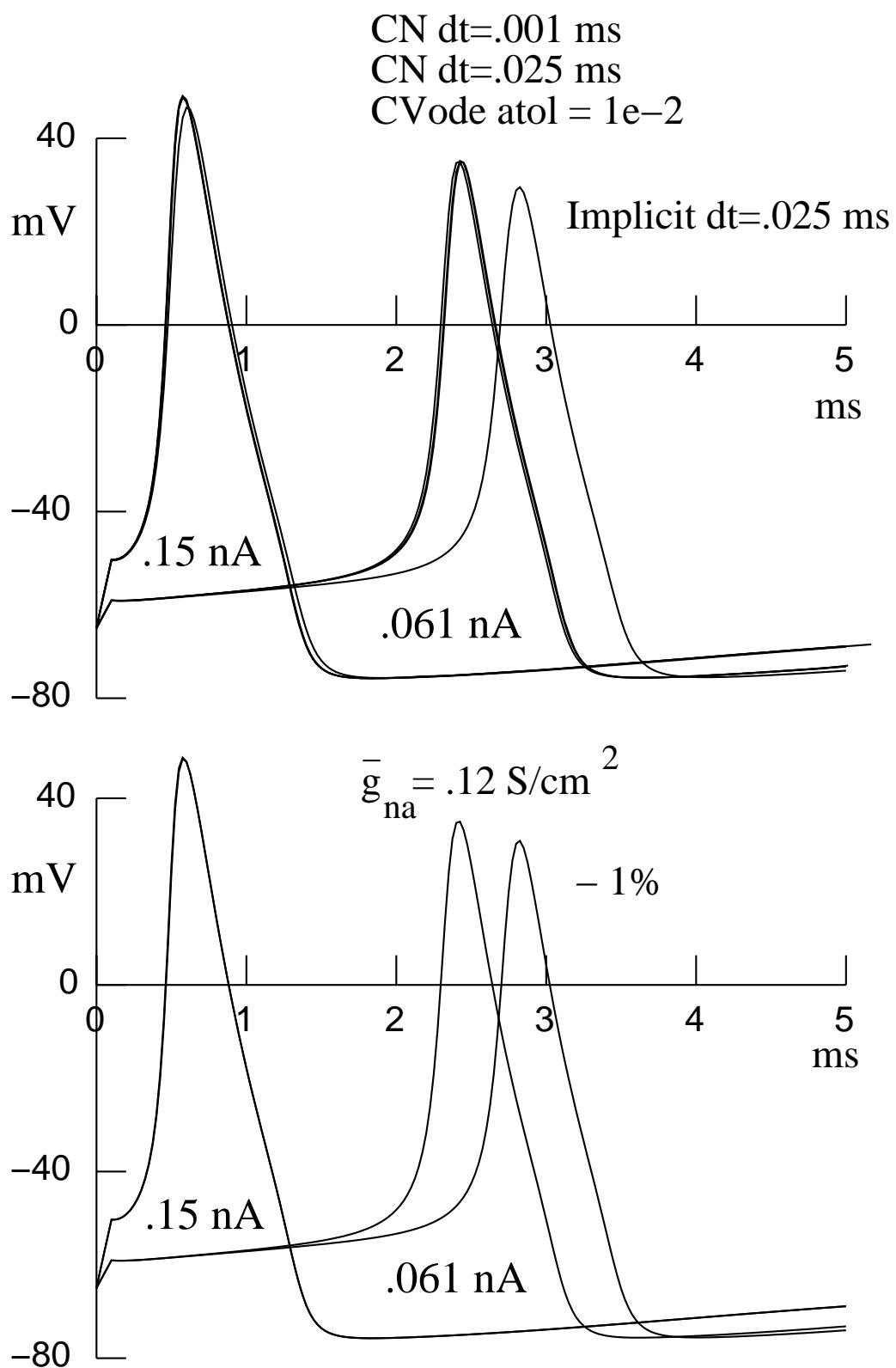
○ ● ● interpolate

# init



• • •





## An Outline for Coding NEURON Models

- Creating a model
  - by writing hoc code
  - and using the graphical interface
- User interface
  - session files
- Tests
  - structural integrity
  - spatial grid
  - time steps

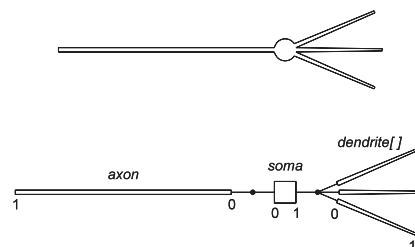
## Creating a Model with hoc

1. Establish model topology
2. Assign properties
3. Attach synapses and electrodes
4. Control simulation time course

### 1. Establish model topology

- Make the pieces (sections) create
- Assemble the pieces connect
- Specify the default section access

### Example



```
// make the pieces
create soma, axon, dendrite[3]

// assemble them
connect axon(0), soma(0)
for i=0,2 {
  connect dendrite[i](0), soma(1)
}

// specify default section
access soma
```

## 2. Assign properties

- Compartmentalization  
nseg
- Anatomical properties  
L, diam
- Biophysical properties  
insert

```

soma {
    nseg = 1
    L = 50      // [um] length
    diam = 50   // [um] diameter
    insert hh   // Hodgkin-Huxley currents
}

axon {
    nseg = 20
    L = 1000
    diam = 1
    insert hh
}

for i=0,2 dendrite[i] {
    nseg = 5
    L = 200
    diam(0:1) = 10:3 // taper
    insert pas        // passive membrane
}

forall Ra = 60 // [ohm cm]

```

## Range variables

Vary continuously in space  
along the length of a section

Examples: v, cm, diam

## Section variables

Pertain to an entire section

Examples: Ra (cytoplasmic resistivity),  
L, nseg

## Global variables

Same across all sections

Examples: celsius,  
t and dt (fixed time step integration)

## 3. Attach synapses and electrodes

```

objref stim      // create it
// put it in middle of soma
soma stim = new IClamp(0.5)
stim.del = 1    // [ms] delay
stim.dur = 0.1  // [ms] duration
stim.amp = 60   // [nA] amplitude

```

#### 4. Control simulation time course

```
dt = 0.05 // [ms] integration time step
tstop = 5 // [ms]
finitialize(-65) // initialize Vm,
                  // state variables, and time

proc integrate() {
    // show starting time & initial somatic Vm
    print t, v(0.5) // soma is default section

    while (t < tstop) {
        fadvance() // advance solution by dt

        // function calls to save or plot results
        // might go here, e.g.
        // print t, v(0.5)
    }
}
```

#### Custom initialization

```
proc init() {
    // set Vm to -65 mV in all sections
    forall v = -65

    // set Vm to -70 in "basal"
    basal v = -70

    // set t to 0
    // & initialize all mechanisms
    // using the assigned v values
    finitialize()

    // make all assigned variables consistent
    // (currents, conductances,
    // & equilibrium potentials)
    fcurrent()
}
```

#### Distributed Mechanisms

Examples:

- ion buffers
- voltage-gated ion channels

```
soma insert hh
```

#### Point Processes

Examples:

- synapses
- clamps, spike detectors

Object syntax

```
objref stim
soma stim = new IClamp(0.5)
stim.del = 1 // [ms]
stim.dur = 0.1 // [ms]
stim.amp = 60 // [nA]
```



# NEURON: the HOC programming language

Bill Lytton

SUNY - Downstate  
Brooklyn, NY

NEURON: the HOC programming language – p.1/2

## TOC

- 2. HOC is the interactive language for NEURON
- 3. Numbers
- 4. Functions & operators: pluses and minuses      5. NB:  $x=5$  vs  $x==5$       6. Assignments
- 7. Block of code    8. Conditionals and controls    9. Procedures and functions (proc and func)
- 10. Number arguments to procedures:    11. Strings    12. Objects    13. Simulation commands
- 14. Sim - stim      15. Sim - running      16. Vectors      17. What have we recorded?
- 18. Can analyze signals using vectors      19. Quick & dirty graphics      20. Graphing a vector
- 21. Find spikes      22. Check results graphically      23. Now can calculate means etc.
- 24. Other useful vector functions    25. Putting up buttons    26. Reading and writing files

NEURON: the HOC programming language – p.27/2

## Talk to the simulator

- Similar to C or Perl but DON'T use semicolons
- HOC=Higher Order Calculator (Kernighan)
- oc is an object-oriented augmentation

NEURON: the HOC programming language – p.2/2

## Numbers

- Integers are handled internally with full precision: 5 same as 5.0
- Can declare an array of numbers: double x[10]
- but vectors are usually better
- Scientific notation uses 'e' or 'E'
- `oc>5e3`  
5000  
`oc>5E3`  
5000

NEURON: the HOC programming language – p.3/2

# Functions & operators: pluses and minuses

- Functions: sin, cos, tan, sqrt, log, log10, exp
- Arithmetic operators: + - / %  
oc> $5+3$  // put comment after double slash
- 8
- Logical operators: && || !
- Comparison operators: == != < >  
oc> $5==5$
- 1
- NB: x=5 vs x==5

NEURON: the HOC programming language – p.4/21

## NB: x=5 vs x==5

- oc>x = 5 + 7 /\* another way to comment \*/
- oc>x==12
- 1
- oc>x==(5+8)
- 0
- OC>x
- 12

NEURON: the HOC programming language – p.5/21

# Assignments

- `x = x+1`
- `x += 1`
- `x *= 2`
- NO: `x++ (C but not in HOC)`

NEURON: the HOC programming language – p.6/2

# Block of code

- A section of code that gets executed together
- Can be used in a conditional or a procedure
- Statements surrounded by curly brackets – no separator
- Confusing: { `x = 7 print x x = 12 print x` }  
7  
12
- Better on individual lines:  
`{ x = 7  
print x  
x = 12  
print x }`

NEURON: the HOC programming language – p.7/2

## Conditionals and controls

- Decides whether or how often to execute a block
- if (5==5) { print "yes" } else { print "no" }
- did I mention?: 'if (x=5)' – you mean 'if (x==5)'
- while (x<=7) { print x x+=1 }
- for x=1,7 print x
- for (x=1;x<=7;x+=2) print x

NEURON: the HOC programming language – p.8/2;

## proc and func

- proc hello () { print "hello" }
- oc>hello()  
hello
- functions can only return a number
- func hello () { print "hello" return 1 }
- oc>hello()  
hello  
1

NEURON: the HOC programming language – p.9/2;

## Number arguments to procedures:

- proc add () { print \$1 + \$2 }
- oc>add(5,3)  
8
- func add () { return \$1 + \$2 }
- print 7\*add(5,3)  
56

NEURON: the HOC programming language – p.10/2

## Strings

- Unlike numbers, string variables must be explicitly declared
- oc>strdef str  
oc>str=5  
nrniv: parse error  
str=5  
oc>str= "hello"  
oc>print str  
hello

NEURON: the HOC programming language – p.11/2

# Objects

- objref or objectvar declares an object pointer:  
`objref g,vec[5],list`
- the command *new* creates a new instance of an object
- Graphs, vectors, lists, files are all handled as objects  
`g = new Graph()`  
`for ii=0,4 vec[ii] = new Vector()`  
`list= new List()`
- “dot” notation accesses object components or procedures  
`g.erase() // only makes sense if g is a graph`  
`vec.x[3] // will access a location in vector vec`

NEURON: the HOC programming language – p.12/2

# Simulation commands

- GUI buttons are connected to hoc level commands
- Can create and run simulations from the command line
- `oc> create soma`
- `oc> access soma`
- `oc> insert hh`
- `oc> ismembrane("hh")`  
1

NEURON: the HOC programming language – p.13/2

## Sim - stim

- oc> objref stim
- oc> stim = new IClamp(0.5) // current clamp obj
- oc> stim.amp=20 // need big stim (big L, diam)
- oc> stim.dur=1e10 // duration

NEURON: the HOC programming language – p.14/21

## Sim - running

- oc> tstop = 2 // stop at the peak of the spike
- oc> run()
- oc>print v, v(0.5), soma.v(0.5) // all equivalent
- 38.764279

NEURON: the HOC programming language – p.15/21

# Vectors

- Can record to vectors and then analyze the contents

- objref vec

```
oc> vec=new Vector()
oc> vec.record(&soma.v(0.5))
oc> tstop = 100
oc> run()
resize_chunk 2046
resize_chunk 4094
resize_chunk 8190
resize_chunk 16382
```

NEURON: the HOC programming language – p.16/2

# What have we recorded?

- print vec.size(),dt,vec.size\*dt,tstop

- print vec.min,vec.max  
-74.774437 40.444033

- print  
vec.min\_ind,vec.max\_ind,vec.min\_ind\*dt,vec.max\_ind\*dt  
470 190 4.7 1.9

- print vec.x[470],vec.x[190]  
-74.774437 40.444033

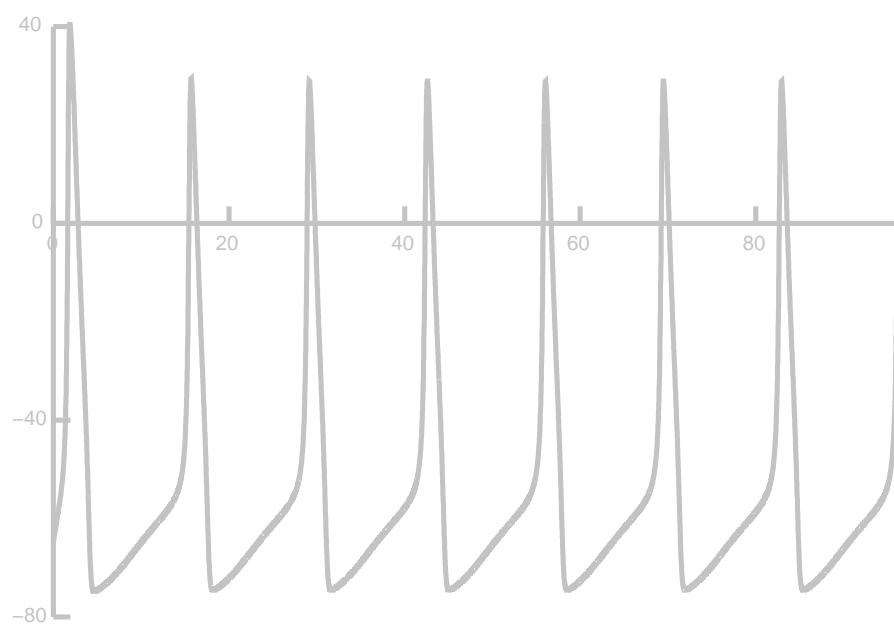
NEURON: the HOC programming language – p.17/2

## Can analyze signals using vectors

- Find the steepest action potential
- `vec[1].deriv(vec,dt)`
- `print vec[1].max_ind,vec[1].max_ind*dt`  
168 1.68

NEURON: the HOC programming language – p.18/2

## Quick & dirty graphics



NEURON: the HOC programming language – p.19/2

## Graphing a vector

- Can put up a graph from the main menu or by hand  
`g = new Graph()`
- Draw the vector on the graph  
`vec.line(g,dt)`
- Need a time vector if using var dt
- Erase and redraw  
`g.erase`

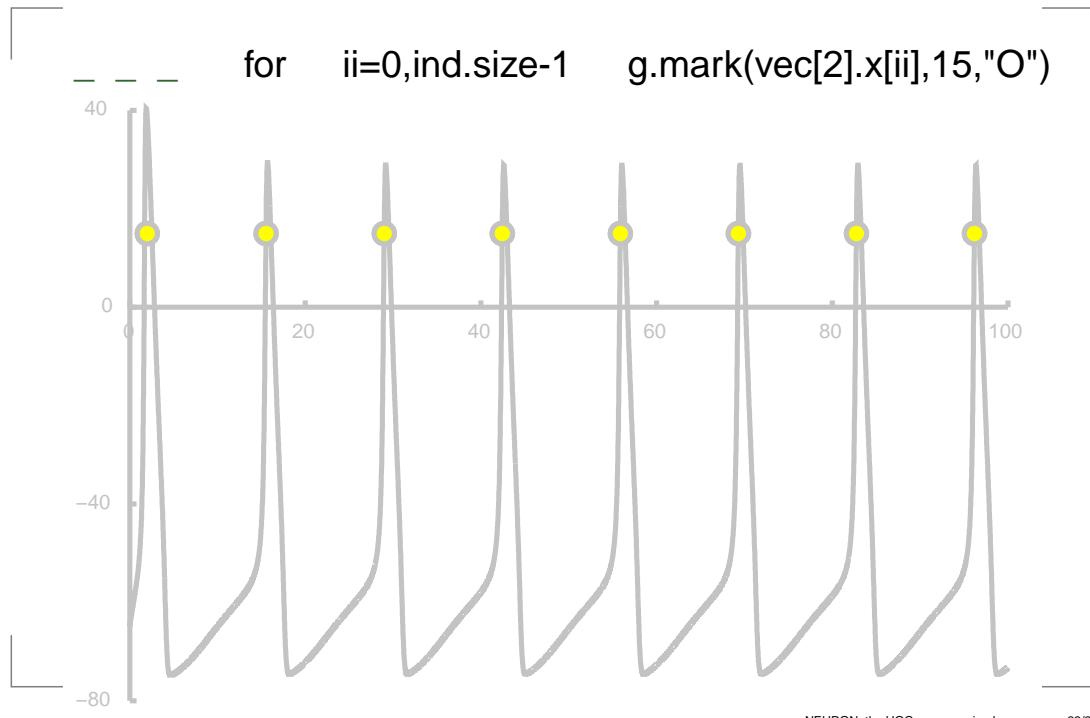
NEURON: the HOC programming language – p.20/21

## Find spikes

- `vec[1].indvwhere(vec,>,15) // indices above a threshold`
- `vec[1].mul(dt) // times`
- `spktime=0`
- `for ii=0,vec[1].size-1 if (vec[1].x[ii]<spktime+2)  
vec[1].x[ii]=-1 else spktime=vec[1].x[ii]`
- `vec[2].where(vec[1],>,0)`

NEURON: the HOC programming language – p.21/21

## Check results graphically



## Now can calculate means etc.

- calculate differences: `vec[3].sub(othervec)`
- take inverses: `vec[3].resize()`, `vec[3].fill(1)`,  
`vec[3].div(othervec)`
- print `vec[3].mean()`, `vec[3].stdev()`

## Other useful vector functions

- `vec.setrand(rdm)` // where rdm=new Random()
- `vec.fft()` // fast fourier transform
- `vec.sort()`
- `vec.histogram()`
- `vec.apply("user_func")`

NEURON: the HOC programming language – p.24/2

## Putting up buttons



NEURON: the HOC programming language – p.25/2

## Reading and writing files

- file=new File()
- file.wopen("tmp")
- vec.printf(file) // or vec.vwrite(file) for binary
- file.close()

NEURON: the HOC programming language – p.26/2

# The NEURON Simulation Environment

The NEURON Simulation Environment

Figure 1

## The Vector class

Efficient methods for collecting  
and manipulating arrays of numbers

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The NEURON Simulation Environment

Figure 3

## Vector functions page 2 of 2

### Algebra

add	div	sub	mul	dot
scale	abs			
log	log10	tanh	pow	sqrt
max	min			
sum	sumsq	mag		
integral	deriv			
eq				

### Signal processing

fft	spectrm	convlv	correl	filter
medfltr	addrand	apply		
psth	spikebin	trigavg		
reduce				

### Statistics

mean	median			
stderr	stdev	var	meansqerr	
fit				
hist	histogram	smhist	sumgauss	

### Simulation

record	play	play_remove		
interpolate				

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# Didactic Presentations

The NEURON Simulation Environment

Figure 2

## Vector functions page 1 of 2

### Initialization & storage

buffer_size	size	resize	
fill	indgen	setstrand	sin
append	c	cl	copy
rebin	resample	reverse	rotate
instrt	remove		

### Database

sort	sortindex		
contains	label		
index	max_ind	min_ind	ind
where	indwhere	indvwhere	

### I/O

fread	fwrite		
vread	vwrite		
scanf	printf	scantil	

### Graph

plot	line	ploterr	mark
------	------	---------	------

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The NEURON Simulation Environment

Figure 4

## Vector record

### SYNTAX

```
vdest.record(&var)
vdest.record(&var, Dt)
vdest.record(&var, tvec)
```

### DESCRIPTION

Save the stream of values of "var"  
during a simulation into the vdest vector.

## Vector play

### SYNTAX

```
vsrcc.play(&var)
vsrcc.play(&var, Dt)
vsrcc.play(&var, tvec)
vsrcc.play("stmt involving $1",
           optional Dt or tvec arg)
vsrcc.play(index)
```

### DESCRIPTION

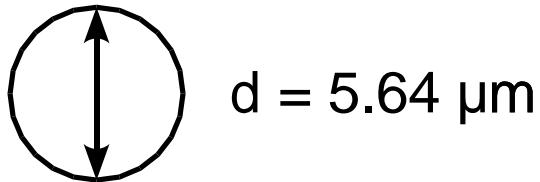
The vsrcc vector values are assigned to  
the "var" variable during a simulation.

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## Example: Model control Arbitrary forcing functions

Physical system: patch of squid axon

Model: isopotential compartment with HH currents



$$\text{surface area} = 100 \mu\text{m}^2$$

Project goals:

- Set up and test a voltage clamp (SEClamp)
- Grapher tool: generate an arbitrary waveform (voltage ramp)
- Clipboard: capture and transfer Vector data
- Vector Play tool: use the recorded waveform as the voltage clamp's "command"

## Example: Simulation Families

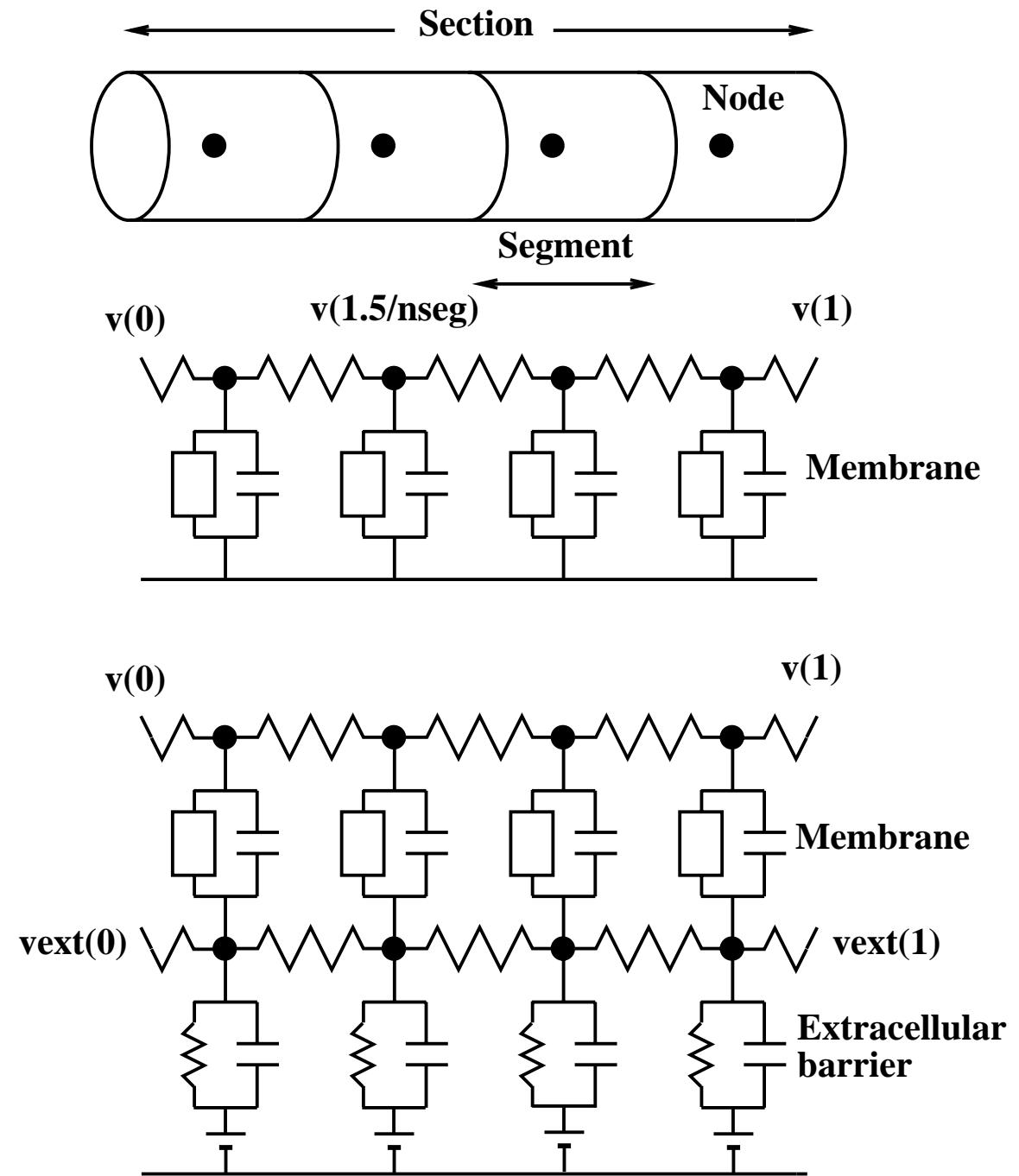
Physical System: pyramidal neuron

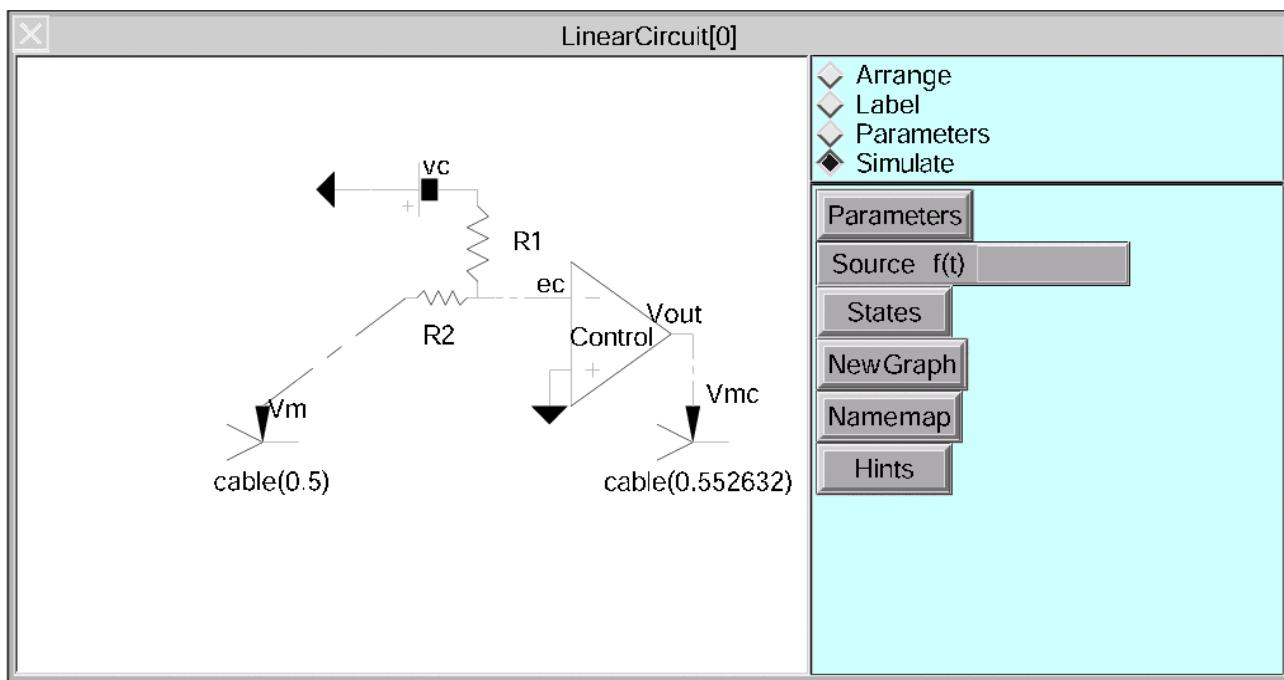
Model: isopotential soma with dendritic cylinder  
conductance–change synapse

Project goals:

- How does peak synaptic depolarization vary with synaptic location?
- Program control of PointProcess location
- Exploratory data collection and analysis
- Using the Vector class to automate data collection and analysis across multiple simulation runs.





**Cable**

d	a	
b	d	a
b	d	a
b	d	a
b	d	

v1
vm
v3
vmc
v5

 **$C y' + G y = b$** 

x		
x	x	x
x	x	x
x	x	x
x		x

vm
vmc
ec
vc
IC
Ivc

d	a		
b	d	a	
b	d	a	
b	d	a	
b	d		
x		x	x
x	x	x	x
x			x
x			x

v1
vm
v3
vmc
v5
ec
vc
IC
Ivc

# NMODL

NEURON Model Description Language

## Add new membrane mechanisms to NEURON

### Density mechanisms

- Distributed Channels
- Ion accumulation

### Point Processes

- Electrodes
- Synapses

### Described by

- Differential equations
- Kinetic schemes
- Algebraic equations

### Benefits

- Specification only -- independent of solution method.
- Efficient -- translated into C.
- Compact
  - One NMODL statement -> many C statements.
  - Interface code automatically generated.
- Consistent ion current/concentration interactions.
- Consistent Units

# NMODL general block structure

## What the model looks like from outside

```
NEURON {
    SUFFIX kchan
    USEION k READ ek WRITE ik
    RANGE gbar, ...
}
```

## What names are manipulated by this model

```
UNITS { (mV) = (millivolt) ... }

PARAMETER { gbar = .036 (mho/cm2) <0, 1e9>... }

STATE { n ... }

ASSIGNED { ik (mA/cm2) ... }
```

## Initial default values for states

```
INITIAL {
    rates(v)
    n = ninf
}
```

## Calculate currents (if any) as function of v, t, states

(and specify how states are to be integrated)

```
BREAKPOINT {
    SOLVE deriv METHOD cnexp
    ik = gbar * n^4 * (v - ek)
}
```

## State equations

```
DERIVATIVE deriv {
    rates(v)
    n' = (ninf - n)/ntau
}
```

## Functions and procedures

```
PROCEDURE rates(v(mV)) {
    ...
}
```

# Density mechanism

```

NEURON {
    SUFFIX leak
    NONSPECIFIC_CURRENT i
    RANGE i, e, g
}

PARAMETER {
    g = .001 (mho/cm2) <0, 1e9>
    e = -65 (millivolt)
}

ASSIGNED {
    i (milliamp/cm2)
    v (millivolt)
}

BREAKPOINT {
    i = g*(v - e)
}

```

# Point Process

## NMODL

```

NEURON {
    POINT_PROCESS Shunt
    NONSPECIFIC_CURRENT i
    RANGE i, e, r
}

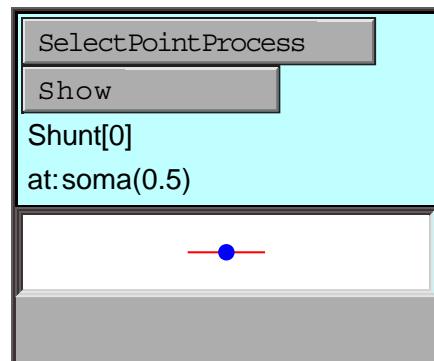
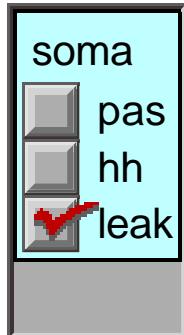
PARAMETER {
    r = 1 (gigaohm) <1e-9,1e9>
    e = 0 (millivolt)
}

ASSIGNED {
    i (nanoamp)
    v (millivolt)
}

BREAKPOINT {
    i = (.001)*(v - e)/r
}

```

## GUI



## Interpreter

```

soma {
    insert leak
    g_leak = .0001
}
print soma.i_leak(.5)

```

```

objref s
soma s = new Shunt(.5)
s.r = 2

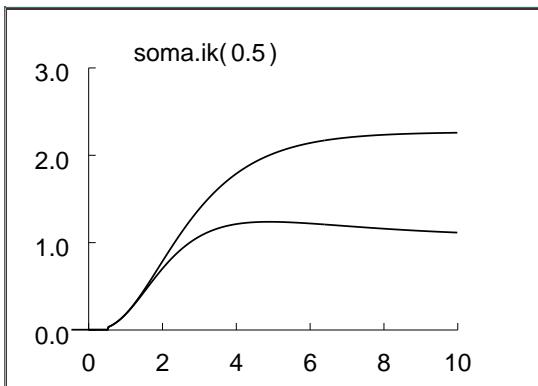
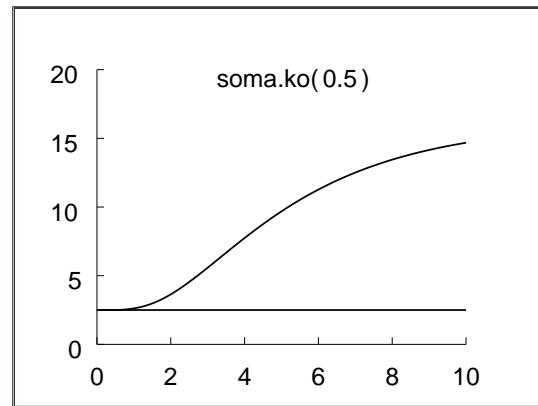
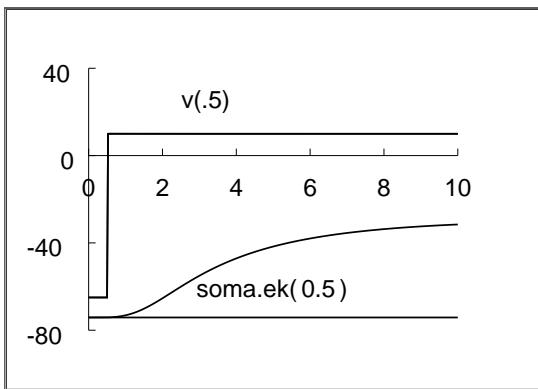
```

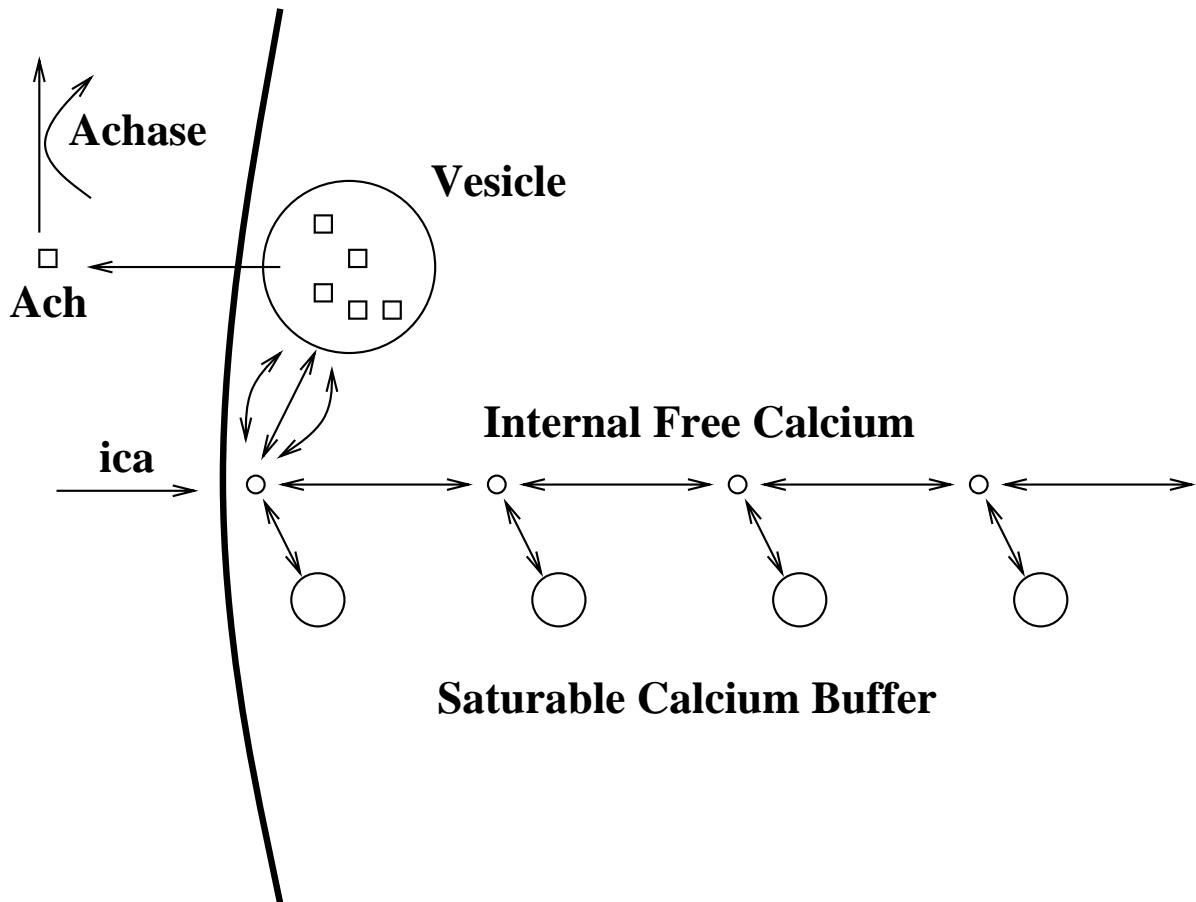
## Ion Channel

```
NEURON {
  USEION k READ ek WRITE ik
}
BREAKPOINT {
  SOLVE states METHOD cnexp
  ik = gbar*n*n*n*n*(v - ek)
}
DERIVATIVE states {
  rate(v*1(/mV))
  n' = (inf - n)/tau
}
```

## Ion Accumulation

```
NEURON {
  USEION k READ ik WRITE ko
}
BREAKPOINT {
  SOLVE state METHOD cnexp
}
DERIVATIVE state {
  ko' = ik/fhspace/F*(1e8)
    + k*(kbath - ko)
}
```





```

STATE {
Vesicle Ach Achase Ach2ase X Buffer[N] CaBuffer[N] Ca[N]
}

KINETIC calcium_evoked_release {
    : release
~ Vesicle + 3Ca[0] <-> Ach      (Agen, Arev)
~ Ach + Achase <-> Ach2ase      (Aase2, 0)   :idiom for enzyme reaction
~ Ach2ase <-> X + Achase       (Aase2, 0)   : requires two reactions

    : Buffering
FROM i = 0 TO N-1 {
    ~ Ca[i] + Buffer[i] <-> CaBuffer[i]     (kCaBuffer, kmCaBuffer)
}

    : Diffusion
FROM i = 1 TO N-1 {
    ~ Ca[i-1] <-> Ca[i]           (Dca*a[i-1], Dca*b[i])
}

    : inward flux
~ Ca[0] <<      (ica)
}

```

# UNITS Checking

```

NEURON { POINT_PROCESS Shunt ... }

PARAMETER {
    e = 0 (millivolt)
    r = 1 (gigaohm) <1e-9,1e9>
}

ASSIGNED {
    i (nanoamp)
    v (millivolt)
}

BREAKPOINT {
    i = (v - e)/r
}

```

**Units are incorrect in the "i = ..." current assignment.**  
 The output from

modlunit shunt  
 is:

Checking units of shunt.mod  
 The previous primary expression with units: 1-12 coul/sec  
 is missing a conversion factor and should read:  
 $(0.001)*()$   
 at line 14 in file shunt.mod  
 $i = (v - e)/r <>$

To fix the problem replace the line with:

$i = (.001)*(v - e)/r$

## What conversion factor will make the following consistent?

$nai' = ina / FARADAY * (c/radius)$   
 $(\mu M/ms) (\mu A/cm^2) / (coulomb/mole) / (\mu m)$

## UNIX

In the directory containing the desired mod files:

```
nrnivmodl  
nrngui
```

Select NEURONMainMenu/Build/singlecompartment.

## MSWIN

Launch mknrndll from the icon in the NEURON program group.

    Navigate to the directory containing the desired mod files.  
    Select "Make nrnmech.dll".

Launch nrngui from the icon in the NEURON program group.

    Select NEURONMainMenu/File/RecentDir to change the working dir and load  
    nrnmech.dll.  
    Select NEURONMainMenu/Build/singlecompartment.

---

### single.hoc

```
load_file("stdgui.hoc")  
create soma  
access soma  
// area 100 um2 means mA/cm2 identical to nA  
{diam=10 L=10/PI}
```

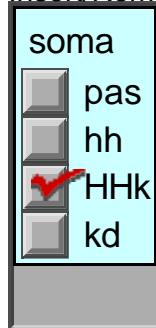
```

: Hodgkin - Huxley k channel

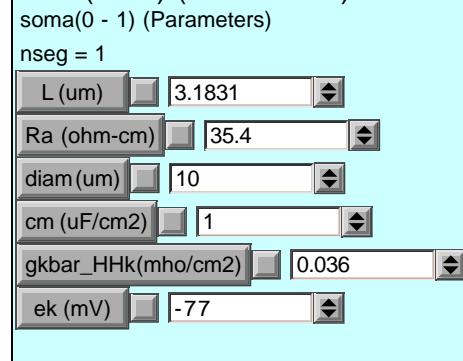
NEURON {
    SUFFIX HHk
    USEION k READ ek WRITE ik
    RANGE gbar, ik, g
    GLOBAL inf, tau
}
UNITS {
    (mA) = (milliamp)
    (mV) = (millivolt)
}
PARAMETER {
    gbar= 0.036 (mho/cm2) <0,1e9>
}
STATE {
    n
}
ASSIGNED {
    v (mV)
    ek (mV)
    celsius (degC)
    ik (mA/cm2)
    inf
    tau (ms)
    g (mho/cm2)
}
INITIAL {
    rate(v)
    n = inf
}
BREAKPOINT {
    SOLVE states METHOD cnexp
    g = gbar*n*n*n*n
    ik = g*(v - ek)
}
DERIVATIVE states {
    rate(v)
    n' =(inf - n)/tau
}
FUNCTION alp(v(mV)) (/ms) { LOCAL q10
    v = -v - 65
    q10 = 3^((celsius - 6.3)/10 (degC))
    alp = q10 * 0.01(/ms-mV)*expM1(v + 10, 10 (mV))
}
FUNCTION bet(v(mV)) (/ms) { LOCAL q10
    v = -v - 65
    q10 = 3^((celsius - 6.3)/10 (degC))
    bet = q10 * 0.125(/ms)*exp(v/80 (mV))
}
FUNCTION expM1(x (mV),y (mV)) (mV) {
    if (fabs(x/y) < 1e-6) {
        expM1 = y*(1 - x/y/2)
    }else{
        expM1 = x/(exp(x/y) - 1)
    }
}
PROCEDURE rate(v (mV)) {LOCAL a, b
    TABLE inf, tau DEPEND celsius FROM -100 TO 100 WITH 200
    a = alp(v)  b=bet(v)
    tau = 1/(a + b)
    inf = a/(a + b)
}

```

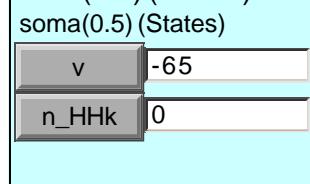
## Insert/Remove Mechanisms



## soma(0 - 1) (Parameters)



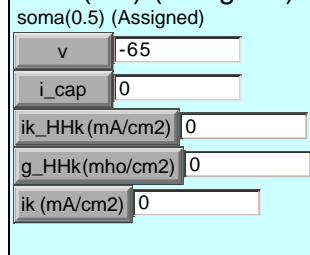
## soma(0.5) (States)



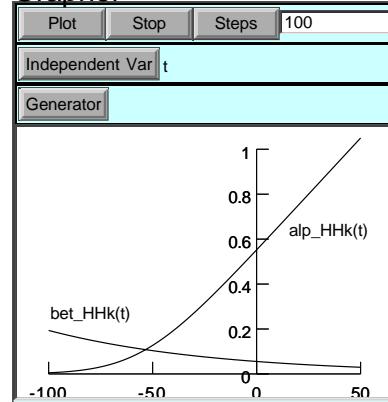
## HHk (Globals)



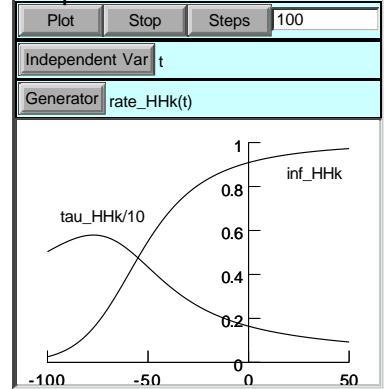
## soma(0.5) (Assigned)



## Grapher



## Grapher



## HH potassium channel conductance data

508

A. L. HODGKIN AND A. F. HUXLEY

From eqn. (6) this may be transformed into a form suitable for comparison with the experimental results, i.e.

$$g_K = \{(g_{K\infty})^t - [(g_{K\infty})^t - (g_{K0})^t] \exp(-t/\tau_n)\}^4, \quad (11)$$

where  $g_{K\infty}$  is the value which the conductance finally attains and  $g_{K0}$  is the conductance at  $t=0$ . The smooth curves in Fig. 3 were calculated from

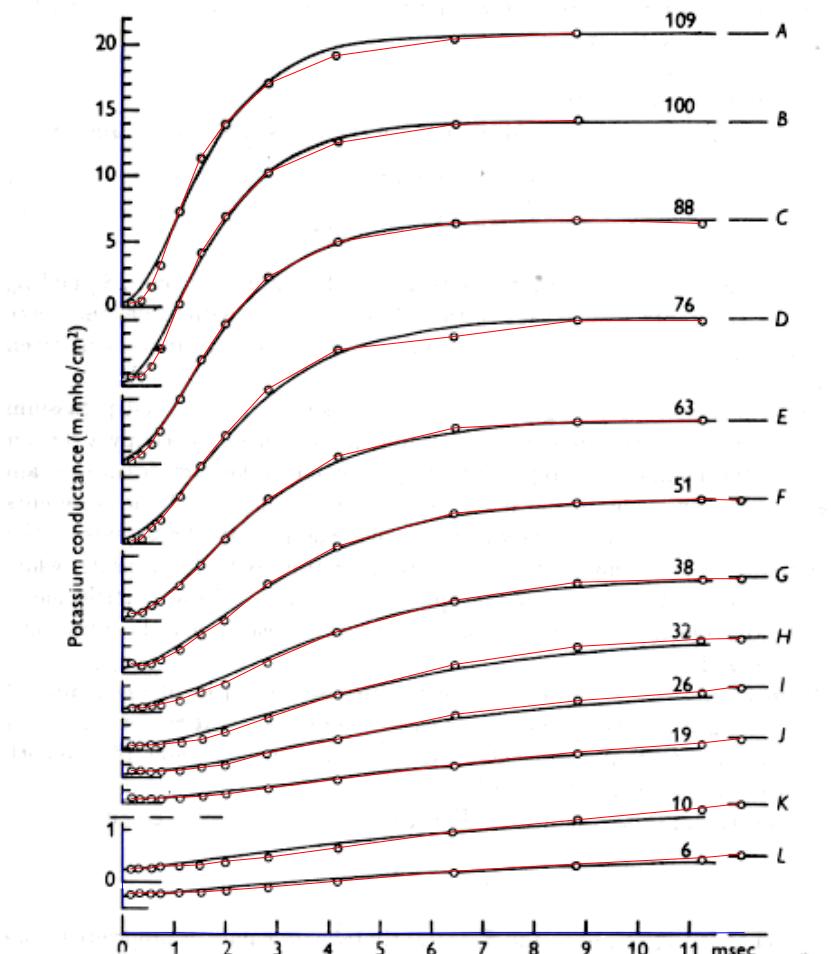


Fig. 3. Rise of potassium conductance associated with different depolarizations. The circles are experimental points obtained on axon 17, temperature 6–7°C, using observations in sea water and choline sea water (see Hodgkin & Huxley, 1952a). The smooth curves were drawn from eqn. (11) with  $g_{K0}=0.24$  m.mho/cm<sup>2</sup> and other parameters as shown in Table 1. The time scale applies to all records. The ordinate scale is the same in the upper ten curves (A to J) and is increased fourfold in the lower two curves (K and L). The number on each curve gives the depolarization in mV.

# Reading the data -- hh508.hoc

```

objref tobj
tobj = new StringFunctions()
if (tobj.is_name("nrrnmainmenu") == 0) {
    xopen("$NEURONHOME/lib/hoc/noload.hoc")
}
objref tobj

// read hh508.dat file and display fig 3 of HH paper (page 508)
// also display steady state conductance as function of clamp voltage

objref vc, gss, g[12], time[12]
strdef tstr

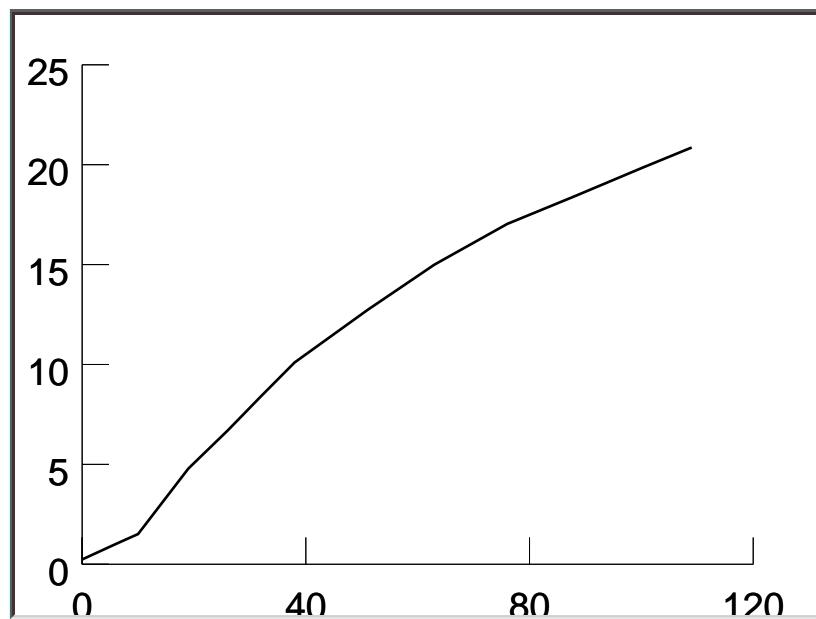
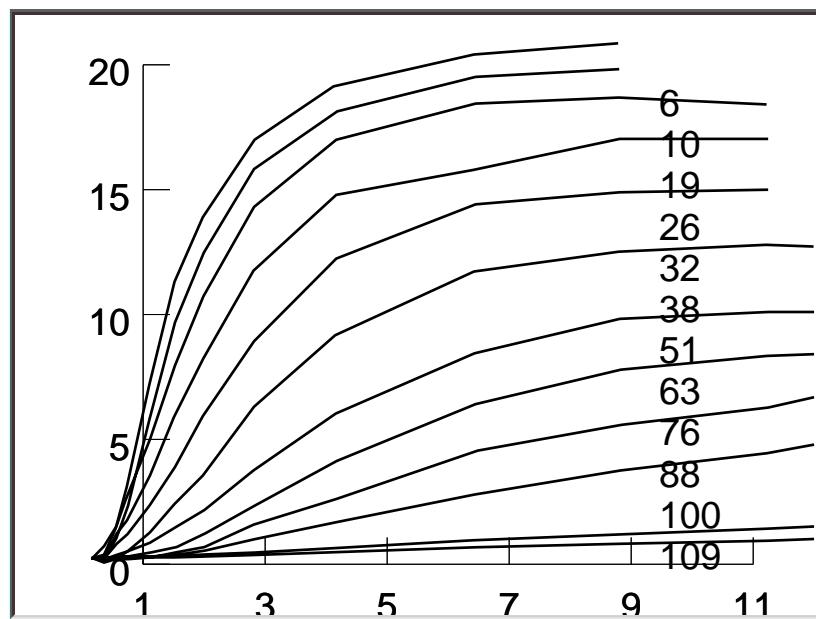
proc readdata() {local i, n, j
//      ropen("hh508.dat")
vc = new Vector(13)
gss = new Vector(13)
for i=0, 11 {
    vc.x[i+1] = fscan()
    n = fscan()
    g[i] = new Vector(n)
    time[i] = new Vector(n)
    sprint(tstr, "%g", vc.x[i+1])
    g[i].label(tstr)
    for j=0, n-1 {
        time[i].x[j] = fscan()
        g[i].x[j] = fscan()
    }
    g[i].add(.24 - g[i].x[0])
    gss.x[i+1] = g[i].x[n-1]
}
vc.x[0] = 0  gss.x[0] = .24
ropen()
}

objref g1, g2
g1 = new Graph()
g1.size(0,11,0,20)
g2 = new Graph()
g2.size(0,120,0,25)
{
readdata()
for i=0, 11 g[i].plot(g1, time[i])
gss.line(g2, vc)
}

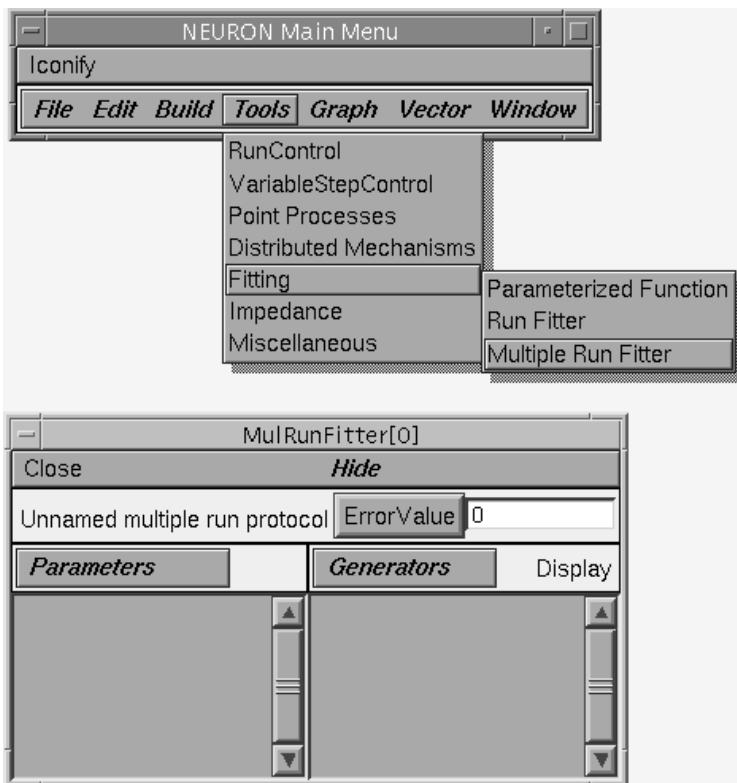
// following is the hh.dat file
6
13
0.148767 0.280702
0.323787 0.298246
...
109
11
0.148767 0.310345
...
8.786 20.931

```

## Conductance data in NEURON



## NEURON MainMenu/Tools/ Fitting/MultipleRunFitter



## Define a FunctionFitness generator for a 2-state steady state Boltzmann distribution

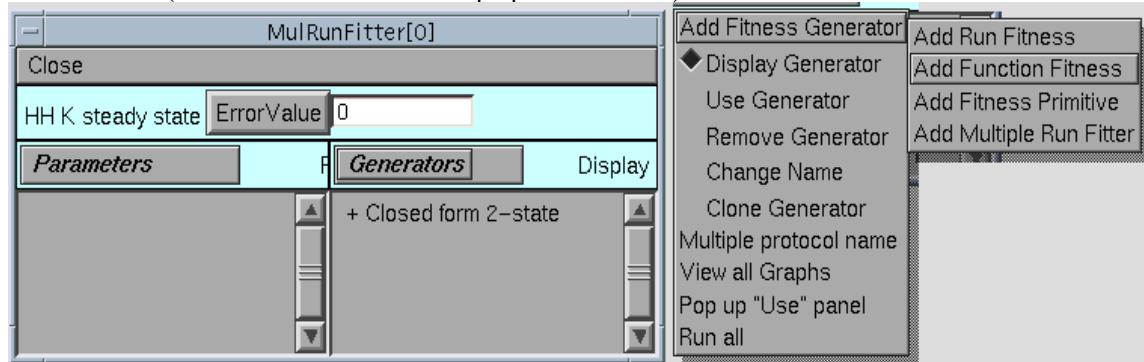
Multiple protocol name --- HH K steady state

Declare the Generator type

AddFitnessGenerator/AddFunctionFitness

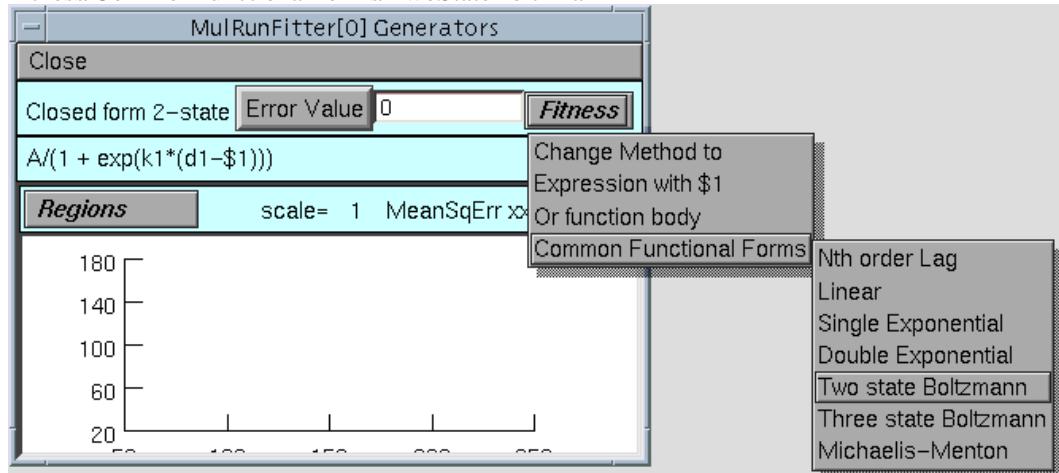
Change Name (double click on item)-- Closed form 2-state

UseGenerator (double click on item so '+' prepended to item)

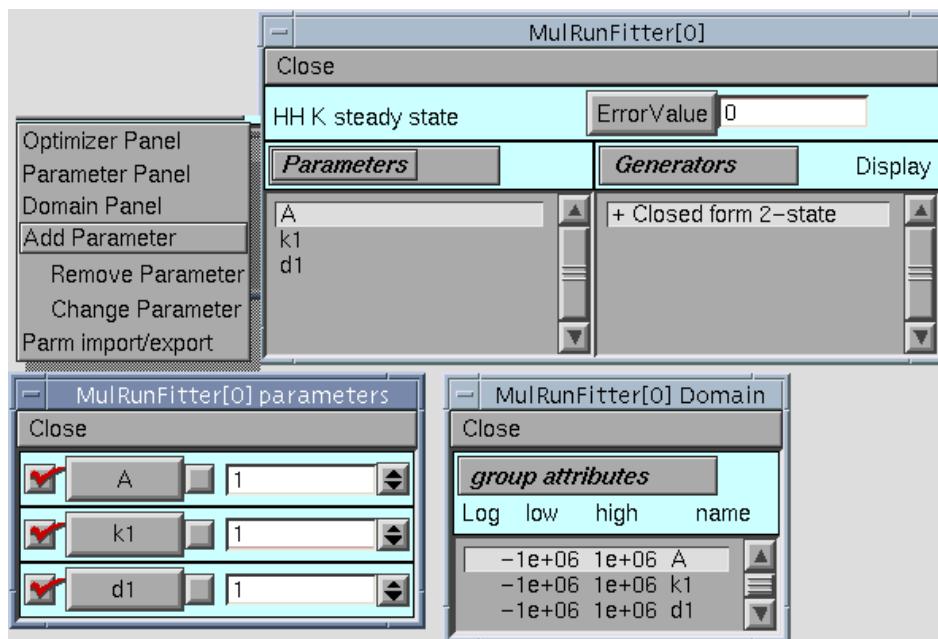


Display Generator (double click on item)

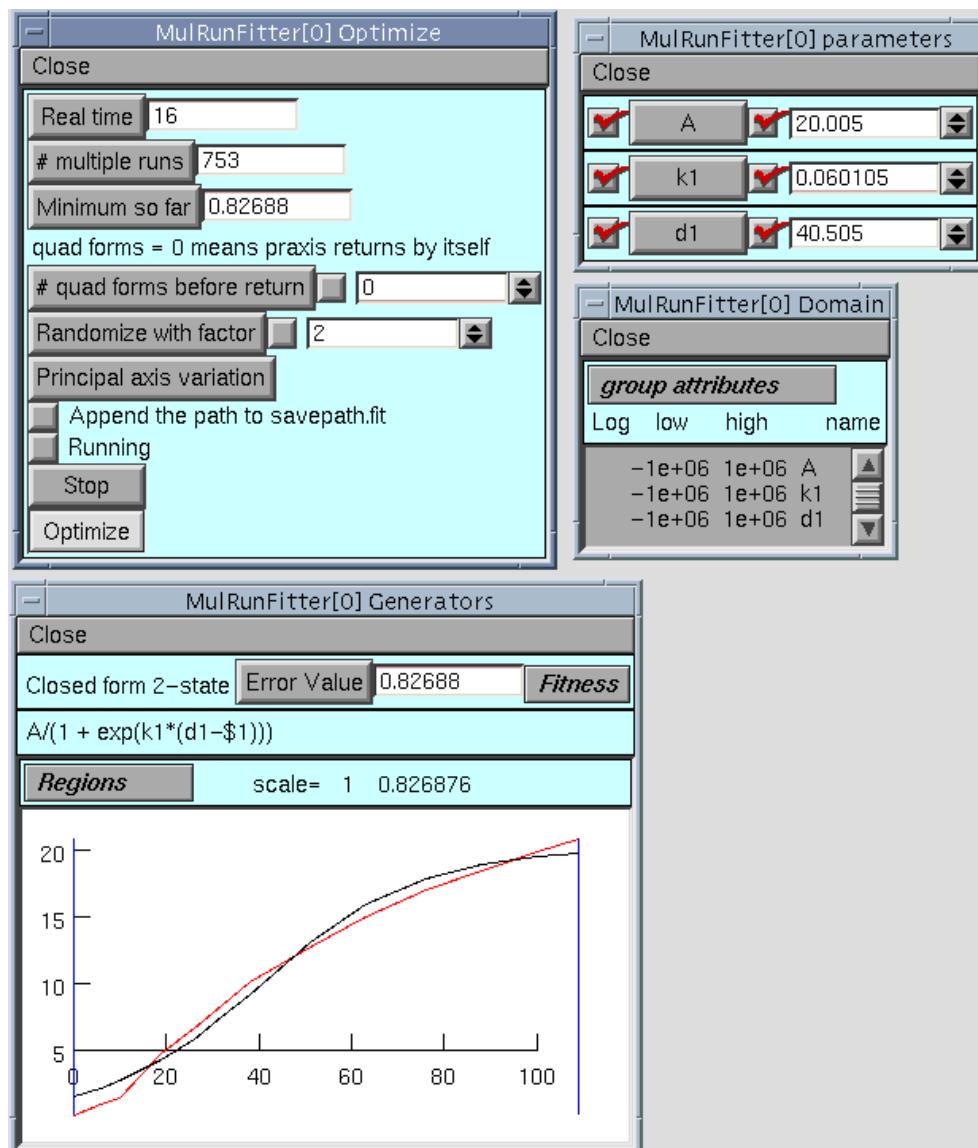
Specify the expression for the FunctionFitness generator  
Fitness/CommonFunctionalForms/TwoStateBoltzmann



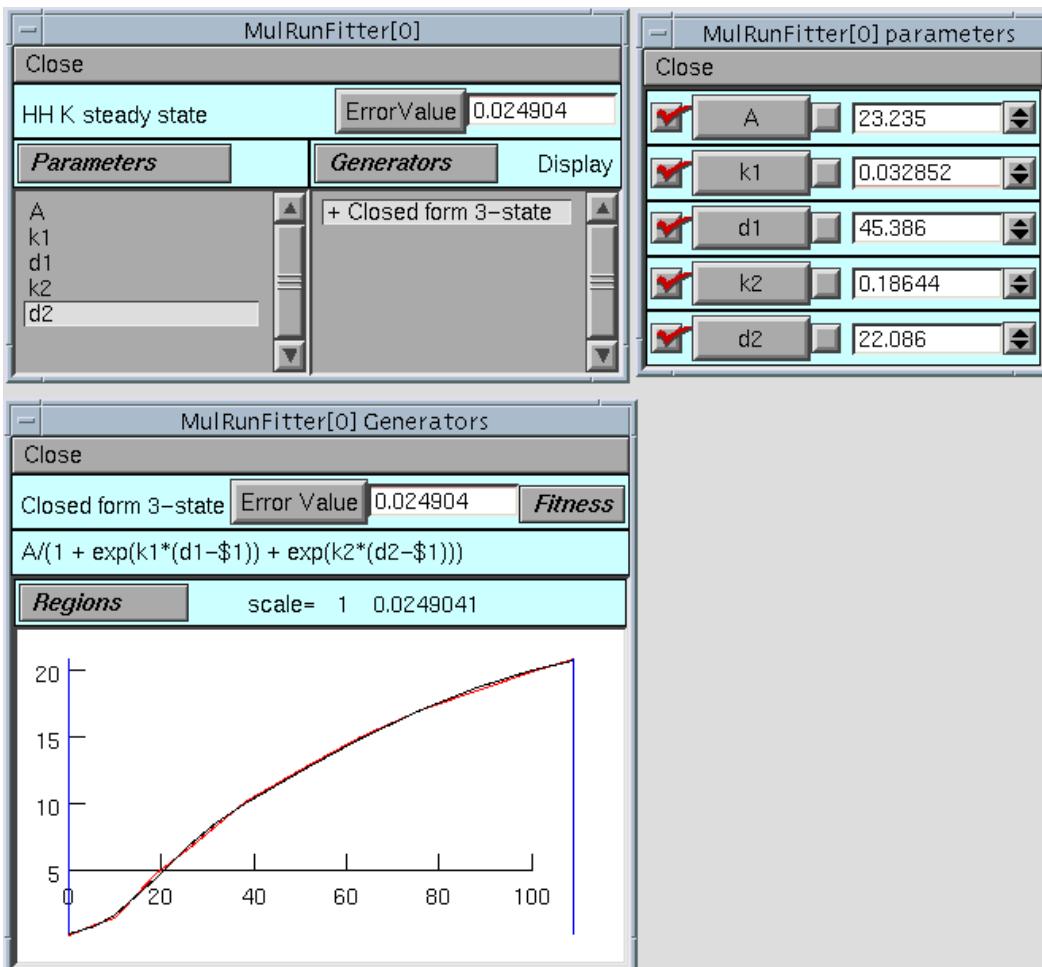
## Choose parameters to optimize



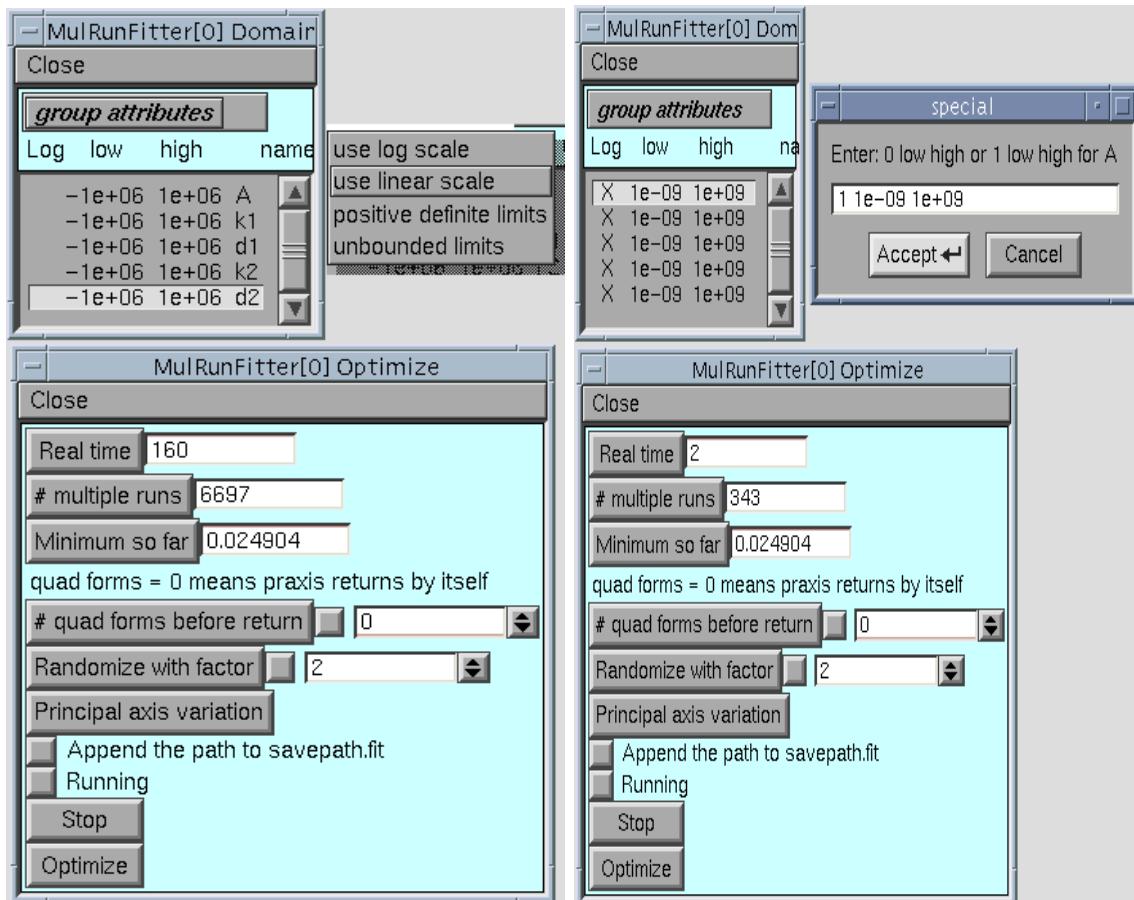
## Steady state (two state Boltzmann model)



## Steady state (three state Boltzmann model)



## Log scaling sometimes has higher performance





## k3.mod -- Three state kinetic scheme



```

NEURON {
  SUFFIX khh
  USEION k READ ek WRITE ik
  RANGE g, gbar
  GLOBAL a1, b1, a2, b2, K1, K2, tau1, tau2
}

PARAMETER { ... } ASSIGNED { ... }

STATE {c1 c2 o}

INITIAL { SOLVE kin STEADYSTATE sparse }

BREAKPOINT {
  SOLVE kin METHOD sparse
  g = gbar*o
  ik = g*(v - ek)*(1e-3)
}

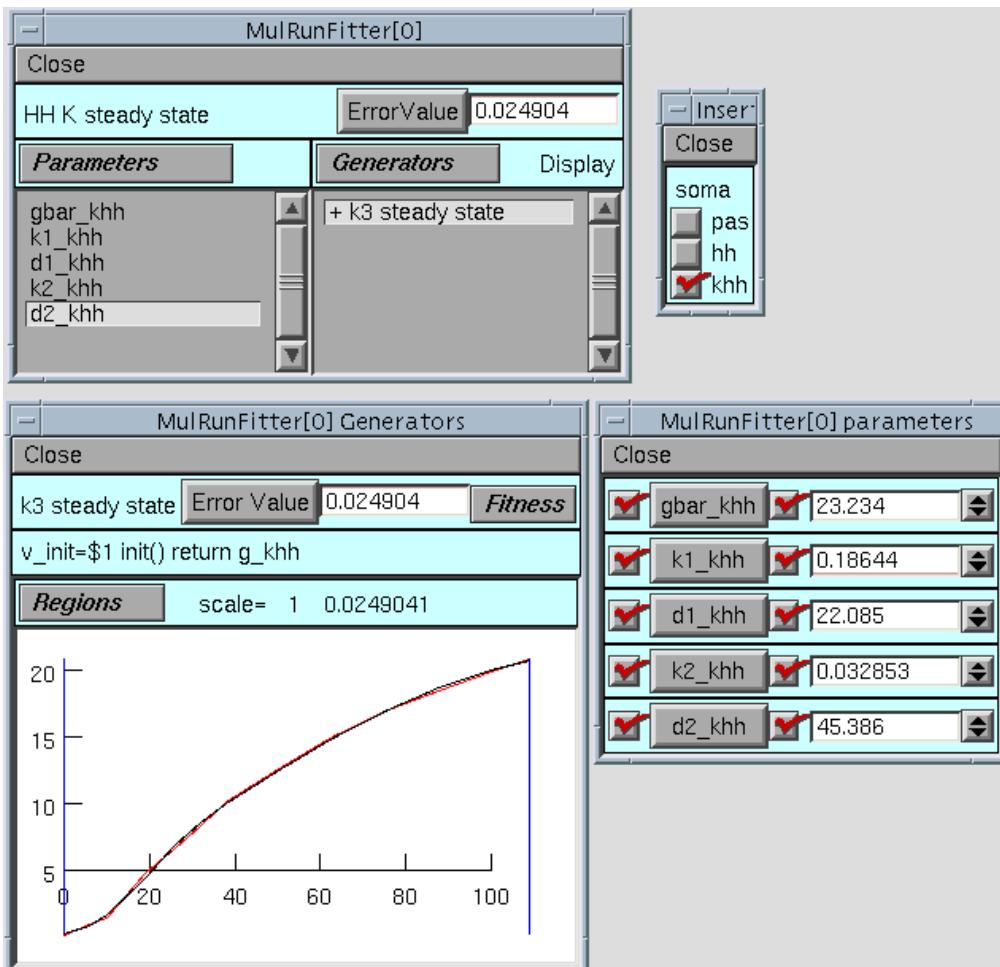
KINETIC kin {
  rates(v) :
  ~ c1 <-> c2 (a1, b1)
  ~ c2 <-> o (a2, b2)
  CONSERVE c1 + c2 + o = 1
}

PROCEDURE rates(v(millivolt)) {
  LOCAL vr
  vr = v - vrest : v = vrest means rates at 0

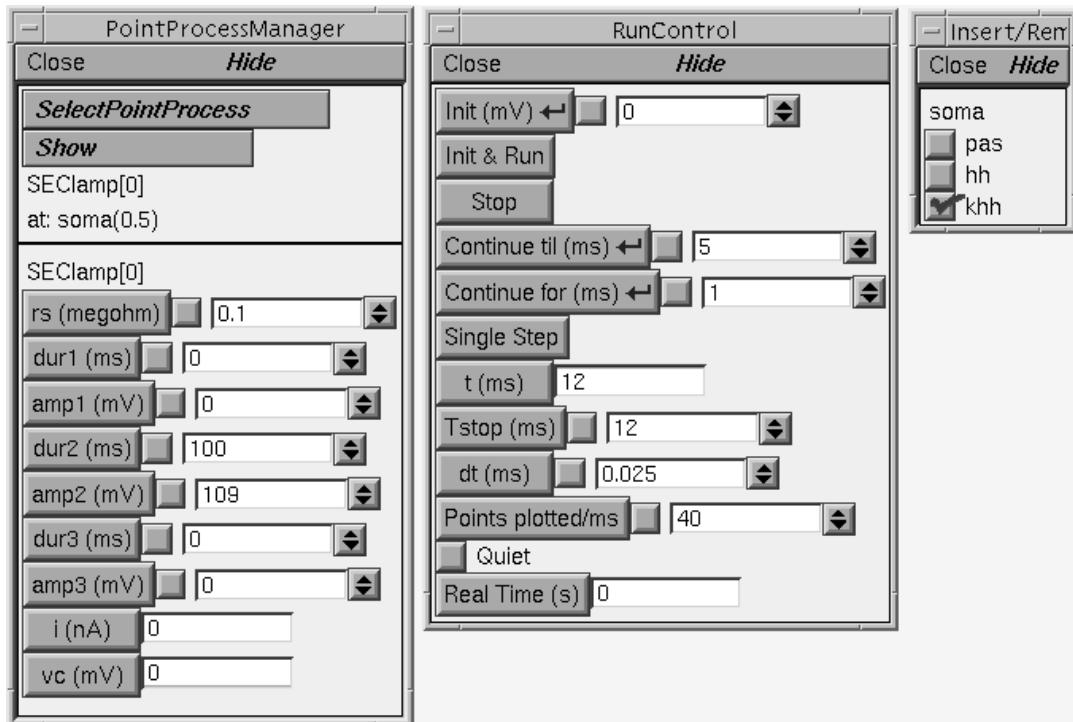
  K2 = exp(-(k2*(d2 - vr)))
  K1 = exp((k2*(d2 - vr)) - (k1*(d1 - vr)))
  tau1 = ta1*exp(tk1*vr)  tau2 = ta2*exp(tk2*vr)

  a1 = K1/(tau1*(K1+1))  b1 = 1/(tau1*(K1+1))
  a2 = K2/(tau2*(K2+1))  b2 = 1/(tau2*(K2+1))
}
  
```

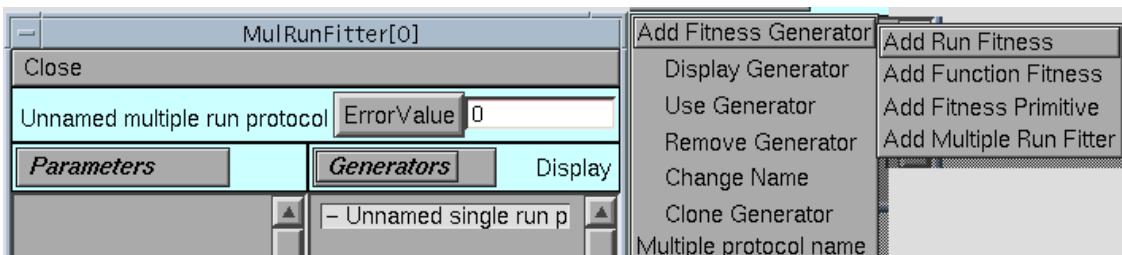
## Steady state fit of k3.mod



## Voltage clamp setup



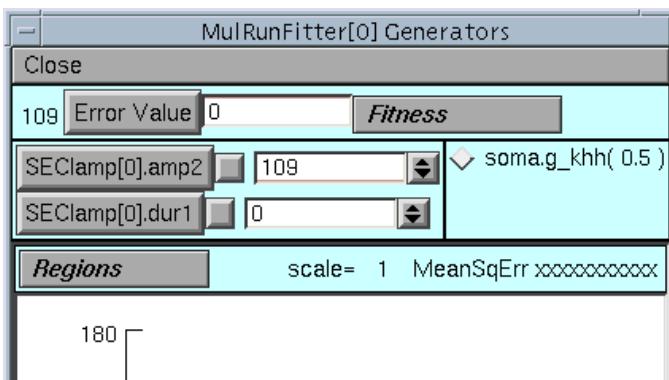
## Setting up a RunFitness generator



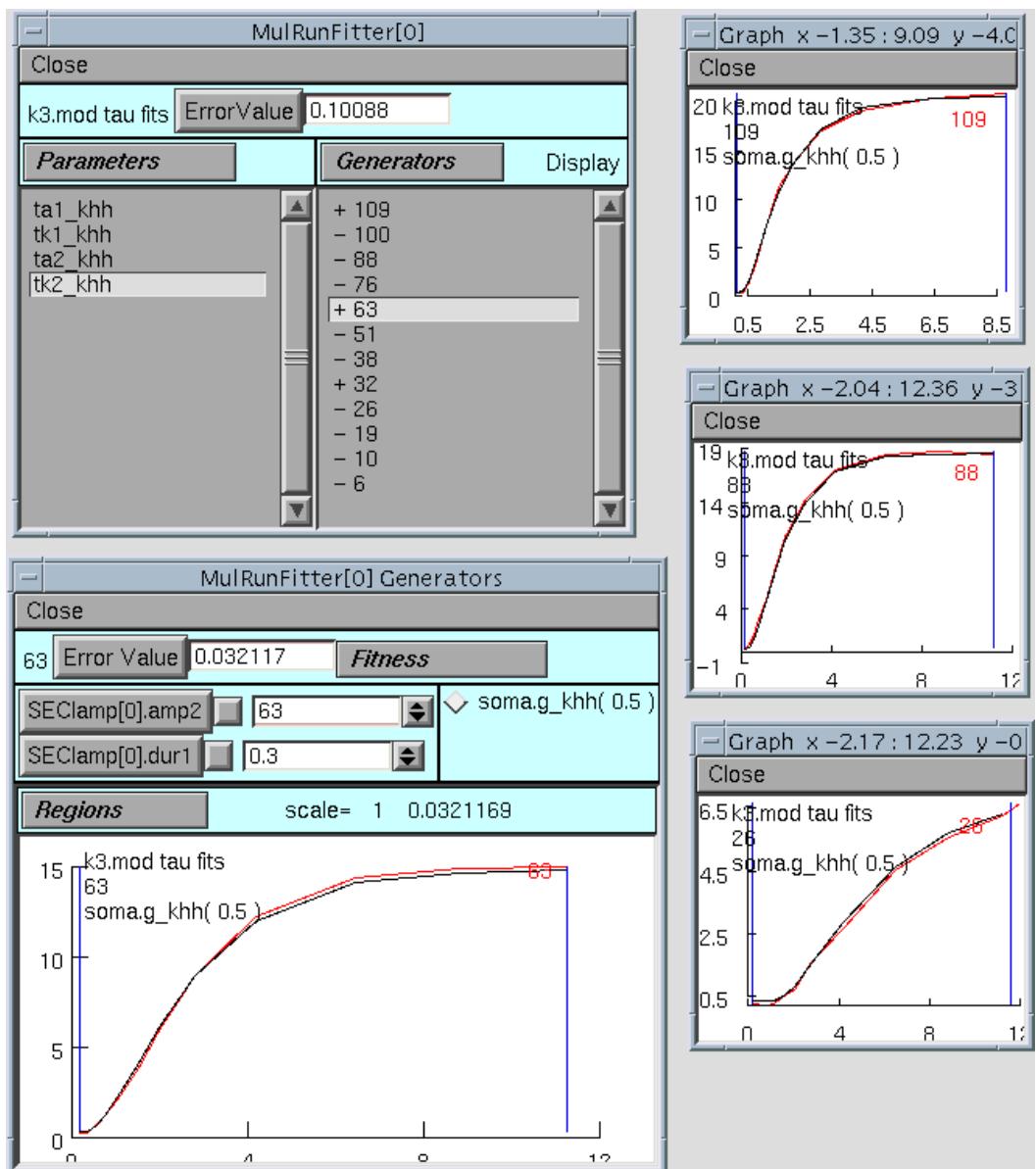
A RunFitness generator does an "Init&Run" to compute the difference between model and data.



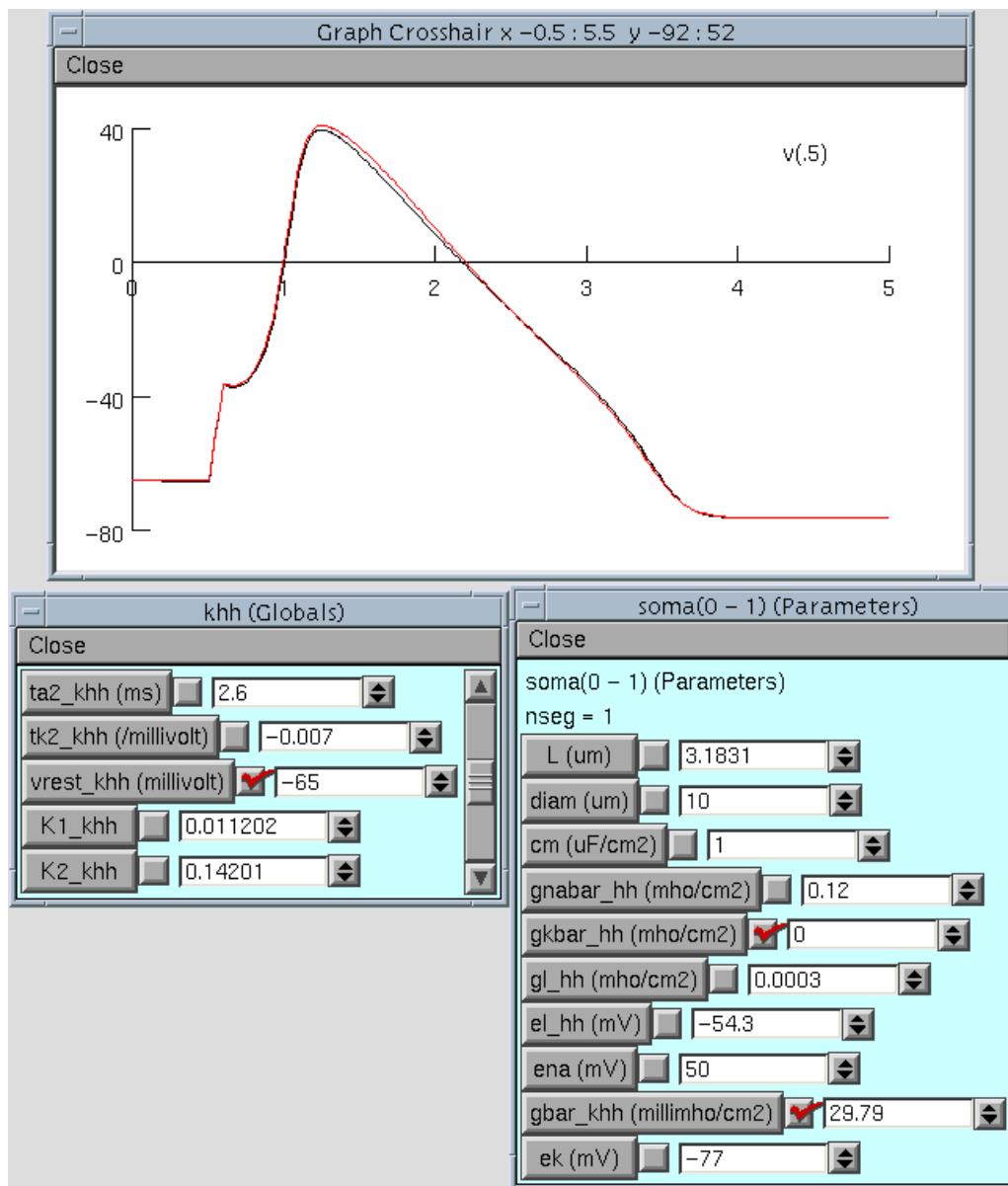
Protocol constants distinguish one run from another.  
Variable to fit is some variable computed during a run.



## Temporal fit of voltage clamp family



## Comparing the action potential







# Computational Modeling and Neuroscience

Does computational modeling have a role  
in neuroscience research?

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## Best Practices

Know the literature

Collaborate with experimentalists

Use Occam's razor

Adhere to scientific method

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## Scientific Method

Observation

Hypothesis

Prediction

Verification

Evaluation

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**The ideal:**

**Reproducibility**

"Reproducibility is the cornerstone  
of scientific method."

"Experiments should be fully described  
so that anyone can reproduce them."

**Harsh reality:**

**Velilind's Laws of Experimentation**

If reproducibility may be a problem,  
conduct the test only once.

If a straight line is required,  
obtain only two data points.

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**<http://senselab.med.yale.edu/senselab/modeldb/>**



ModelDB provides an accessible location for storing and efficiently retrieving compartmental neuron models. ModelDB is tightly coupled with [NeuronDB](#). Models can be coded in any language for any environment, though ModelDB has been initially constructed for use with [NEURON](#) and [GENESIS](#). Model code can be viewed before downloading and browsers can be set to auto-launch the models. [Help](#)

- Search for models by author name
- List models sorted by [first author](#), by [each author](#) or by [model name](#)
- Find models of a particular [Neuron](#) type
- Find models containing a particular Property: [Currents](#), [Receptors](#), or [Transmitters](#)
- Find models that relate to a [Concept](#), e.g. synaptic plasticity, pattern recognition, etc.
- Find models that run in a particular [Simulation environment](#)
- List models of: [Networks](#), [Neurons](#), [Synapses](#) (and ligand-gated ion channels), [Neuromuscular Junctions](#), [Axons](#), voltage-gated [Ion Channels](#)
- Find models containing the following words    Case Sensitive
- [Search for publications](#)

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ModelDB can accommodate models from a wide range of simulation environments



#### Find Models by Simulation Environment

Click on a link to show a list of models implemented in that simulation environment or programming language.

Simulation Environment	Homepage	Number of models
BLISS/SYNOD	<a href="#">BLISS/SYNOD</a>	0
C or C++ program	<a href="#">C or C++ program</a>	0
CellML	<a href="#">CellML</a>	0
<a href="#">Genesis</a>	<a href="#">Genesis</a>	1
<a href="#">Genesis (web link to model)</a>	<a href="#">Genesis (web link to model)</a>	2
L-Neuron	<a href="#">L-Neuron</a>	0
MCell	<a href="#">MCell</a>	0
Neosim	<a href="#">Neosim</a>	0
<a href="#">Neuron</a>	<a href="#">Neuron</a>	93
<a href="#">Neuron (web link to model)</a>	<a href="#">Neuron (web link to model)</a>	3
Surf-Hippo	<a href="#">Surf-Hippo</a>	0

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## Search results

### Models by moore

1. [Nerve terminal currents at lizard neuromuscular junction; Lindgren and Moore 1989](#)  
Lindgren CA, Moore JW (1989) Identification of ionic currents at presynaptic nerve endings of the lizard. *J Physiol* 414:201–22 [PubMed]
2. [Presynaptic calcium dynamics at neuromuscular junction; Stockbridge and Moore 1984](#)  
Stockbridge N, Moore JW (1984) Dynamics of intracellular calcium and its possible relationship to phasic transmitter release and facilitation at the frog neuromuscular junction. *J Neurosci* 4:803–11 [PubMed]
3. [Site of impulse initiation in a neuron by Moore et al 1983](#)  
Moore JW, Stockbridge N, Westerfield M (1983) On the site of impulse initiation in a neurone. *J Physiol* 336:301–11 [PubMed]
4. [Current flow during PAP in squid axon at diameter change; Joyner et al 1980](#)  
Joyner RW, Westerfield M, Moore JW (1980) Effects of cellular geometry on current flow during a propagated action potential. *Biophys J* 31:183–94 [PubMed]
5. [Conduction in uniform myelinated axons; Moore et al 1978](#)  
Moore JW, Joyner RW, Brill MH, Waxman SD, Najar-Joa M (1978) Simulations of conduction in uniform myelinated fibers. Relative sensitivity to changes in nodal and internodal parameters. *Biophys J* 21:147–60 [PubMed]
6. [Temperature-Sensitive conduction at axon branch points by Westerfield et al 1978](#)  
Westerfield M, Joyner RW, Moore JW (1978) Temperature-sensitive conduction failure at axon branch points. *J Neurophysiol* 41:1–8 [PubMed]
7. [Myelinated axon conduction velocity by Brill et al 1977](#)  
Brill MH, Waxman SG, Moore JW, Joyner RW (1977) Conduction velocity and spike configuration in myelinated fibres: computed dependence on internode distance. *J Neurol Neurosurg Psychiatry* 40:769–74 [PubMed]

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## Site of impulse initiation in a neuron by Moore et al 1983

### Site of impulse initiation in a neuron by Moore et al 1983

Examines the effect of temperature, the taper of the axon hillock, and HH channel density on antidromic spike invasion into the soma and spike initiation under dendritic stimulation.  
Reference: Moore JW, Stockbridge N, Westerfield M (1983) On the site of impulse initiation in a neurone. *J Physiol* 336:301–11 [PubMed]

### Citations [Citation Browser](#)

Model Information (Click on a link to find other models with that property)

Model Type: [Neuron](#)  
Cell Type(s): [Spinal motor neuron](#)  
Channel(s): [INa](#); [IK](#)  
Receptor(s):  
Transmitter(s):

Simulation Environment: [Neuron](#)  
Model Concept(s): [Action Potential Initiation](#); [Simplified Models](#);

Search NeuronDB for information about: [Spinal motor neuron](#); [INa](#); [IK](#);

Model files | [Download zip file](#) | Auto-launch | [Help downloading and running models](#)

<ul style="list-style-type: none"> <li><input checked="" type="checkbox"/> <a href="#">moore83</a></li> <li><input type="checkbox"/> <a href="#">README</a></li> <li><input type="checkbox"/> <a href="#">mosinit.hoc</a></li> <li><input type="checkbox"/> <a href="#">init.hoc</a></li> <li><input type="checkbox"/> <a href="#">startses</a></li> </ul>	<p>Moore, Stockbridge, and Westerfield. (1983) On the site of impulse initiation in a neurone. <i>J. Physiol.</i> 336: 301–311.</p> <p>This model qualitatively reproduces figures 1–5. Note that orthodromic stimulus amplitude is considerably different from that noted in the paper. IClamp[0].amp was chosen to give qualitative similarity. We attribute minor quantitative differences to the following:</p> <ol style="list-style-type: none"> <li>1) The precise site of axon v vs t curve is not specified. We plot axon.v(0.25).</li> <li>2) The antidromic stimulus was unspecified.</li> </ol> <p>The NEURON implementation of this model was prepared by Michael Hines. Questions about details of this implementation should be addressed to him at michael.hines@yale.edu.</p>
--	--

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## How to proceed

Read model notes, abstract, paper

Download and extract the zip file

Compile the mod files

Run mosinit.hoc and see what it does

Figure out what's there and how it works

topology(), Shape plot

forall psection()

analyze hoc code

Look for reusable components

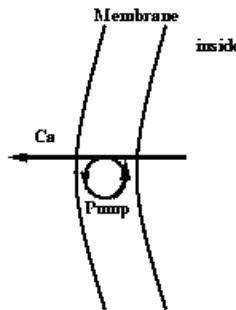
model specification	topology and geometry mechanisms
---------------------	-------------------------------------

interface specification	parameter control instrumentation run control
-------------------------	---

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## Rate limited active transport of calcium.



```
KINETIC pmp {
    ~ cabulk <-> cam                      (1/tau, 1/tau)
    ~ cam + pump <-> capump                (k1, k2)
    ~ capump <-> cao + pump                (k3, k4)
    ica_pmp = 2*FARADAY*(f_flux - b_flux)

    ~ cam << -(ica) : there is a problem here

    COMPARTMENT width {cam} : volume in (um)
    COMPARTMENT 1 {pump capump} : area is dimensionless
    COMPARTMENT 1(m) {cao cabulk}
}
```

## Declarations for capump.mod

```
NEURON {
    SUFFIX capmp
    USEION ca READ cao, ica, cai WRITE cai, ica
    RANGE tau, width, cabulk, ica, pump0
}

UNITS {
    (um)      =          (micron)
    (molar)   =          (1/liter)
    (mM)      =          (millimolar)
    (uM)      =          (micromolar)
    (mA)      =          (milliamp)
    (mol)     =          (1)
    FARADAY =          (faraday)      (coulomb)
}

PARAMETER {
    width = 0.1 (um)
    tau = 1 (ms)
    k1 = 5e8          (/mM-s)
    k2 = 0.25e6        (/s)
    k3 = 0.5e3          (/s)
    k4 = 5e0          (/mM-s)
    cabulk = 0.1 (uM)
    pump0 = 3e-14 (mol/cm2)
}

ASSIGNED {
    cao (mM) : 10
    cai (mM) : 1e-3
    ica (mA/cm2)
    ica_pmp (mA/cm2)
    ica_pmp_last (mA/cm2)
}

STATE {
    cam (uM)           <1e-6>
    pump (mol/cm2)    <1e-16>
    capump (mol/cm2) <1e-16>
}
```

## Equations for capump.mod

```
INITIAL {
    ica = 0
    ica_pmp = 0
    ica_pmp_last = 0
    SOLVE pmp STEADYSTATE sparse
}

BREAKPOINT {
    SOLVE pmp METHOD sparse
    ica_pmp_last = ica_pmp
    ica = ica_pmp
}

KINETIC pmp {
    ~ cabulk <-> cam (width/tau, width/tau)
    ~ cam + pump <-> capump ((1e7)*k1, (1e10)*k2)
    ~ capump <-> cao + pump ((1e10)*k3, (1e10)*k4)
    ica_pmp = (1e-7)*2*FARADAY*(f_flux - b_flux)

    : ica_pmp_last vs ica_pmp needed because
    : of STEADYSTATE calculation
    ~ cam << (-(ica - ica_pmp_last) / (2*FARADAY) * (1e7))

    CONSERVE pump + capump = (1e13)*pump0
    COMPARTMENT width {cam}      : volume has dimensions of um
    COMPARTMENT (1e13) {pump capump} : area is dimensionless
    COMPARTMENT 1(um) {cabulk}
    COMPARTMENT (1e3)*1(um) {cao}

    cai = (0.001)*cam
}
```

## Testing capump.mod

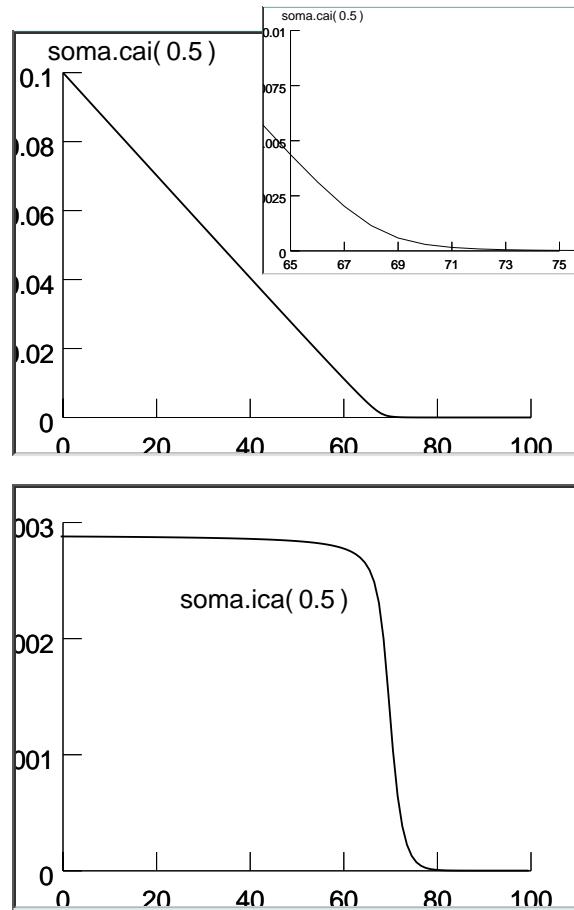
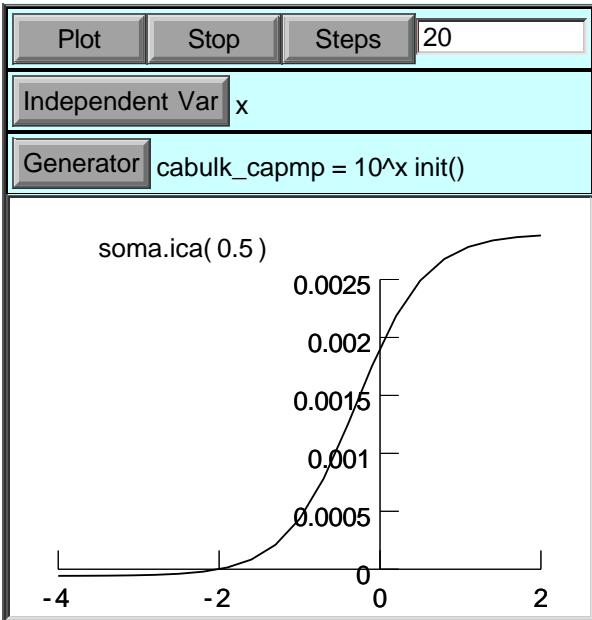
```

load_file("single.hoc")

// define a replacement for the stdrun.hoc version of
// proc init() {
//     finitialize(v_init)
//     fcurren()
// }
// that lets you escape from the tyranny of the
// steady state initialization of cai.

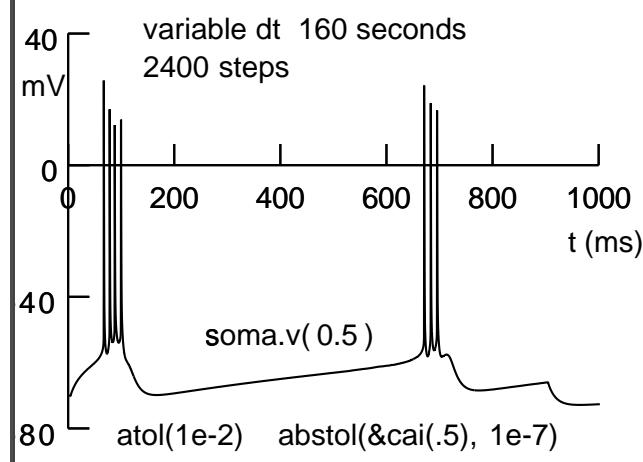
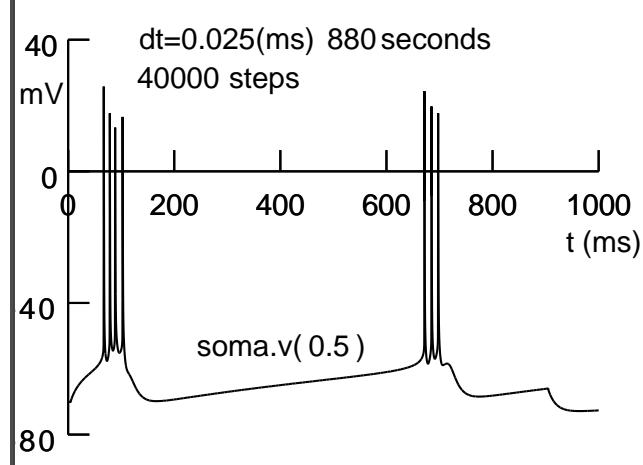
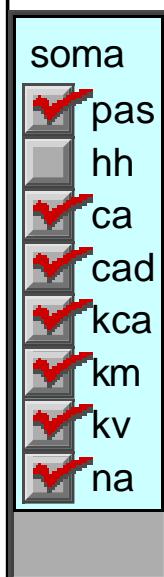
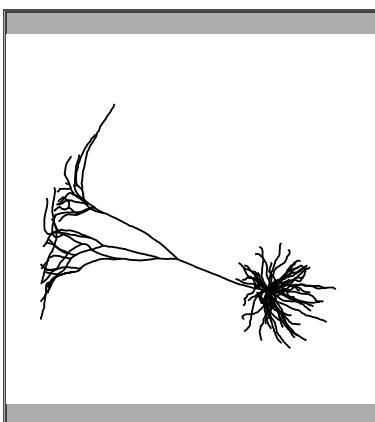
proc init() { local savtau
    // will initialize cai to cabulk
    savtau = tau_capmp
    tau_capmp = 1e-6
    finitialize(v_init)
    tau_capmp = savtau
    fcurren()
}

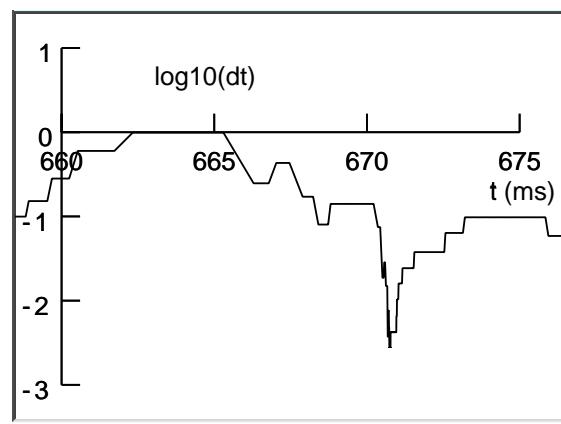
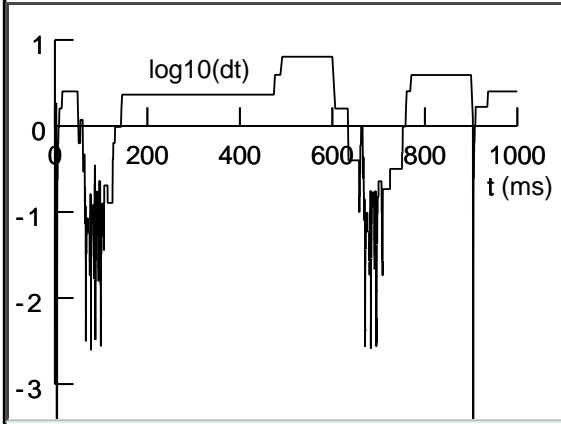
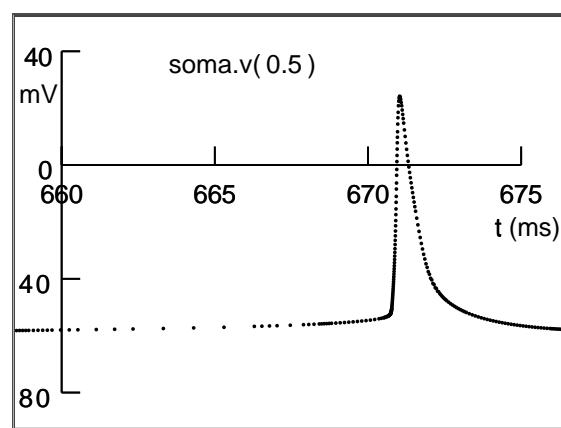
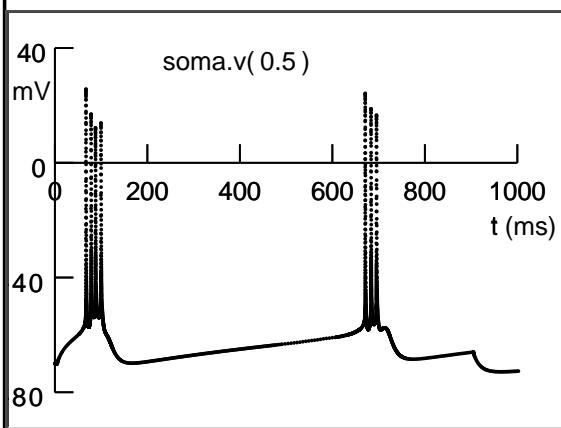
```

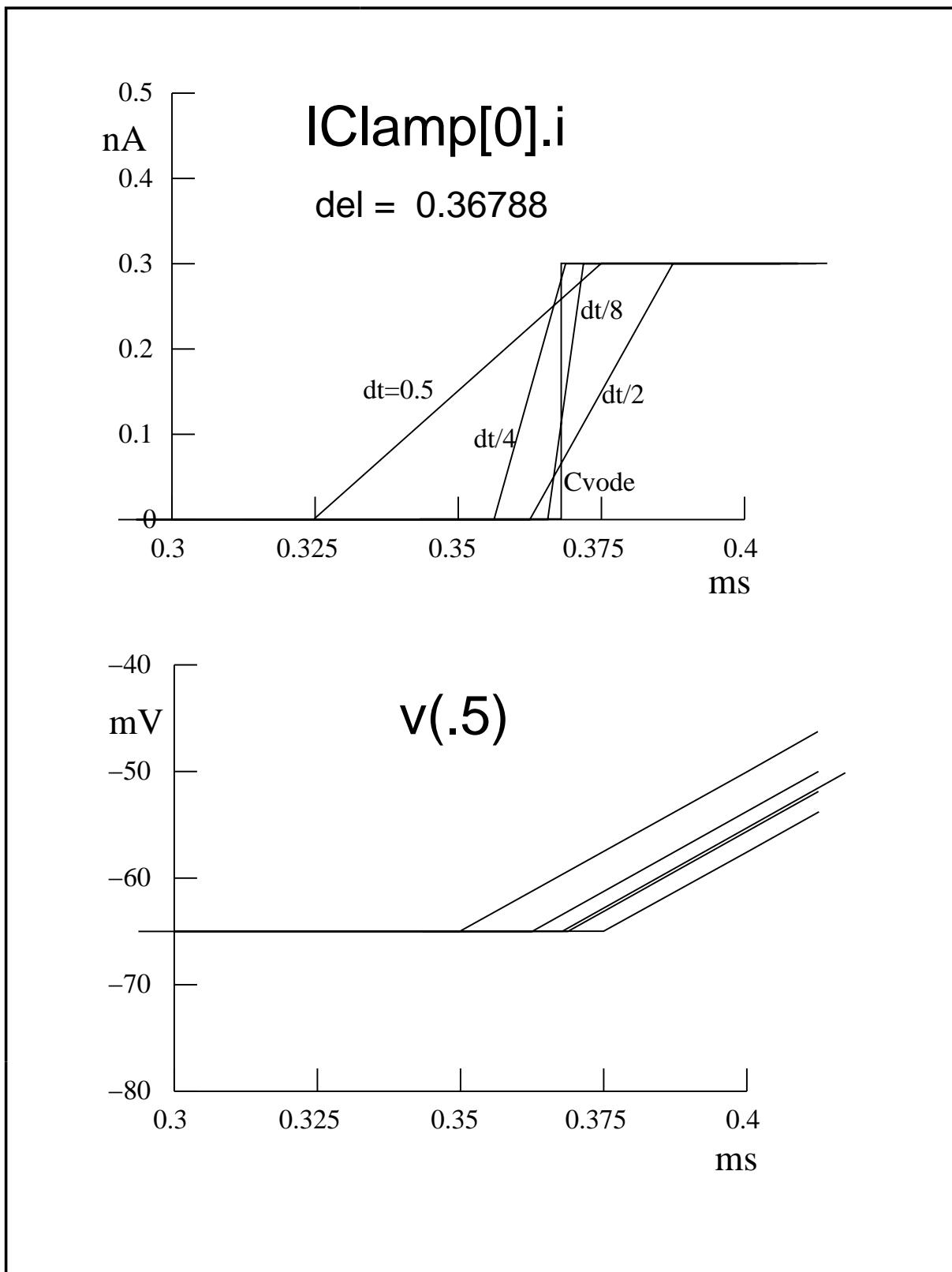


## L5 Pyramid demo

From:  
Z. F. Mainen and T. J. Sejnowski (1996)  
Influence of dendritic structure on  
firing pattern in model neocortical  
neurons. Nature 382: 363-366.

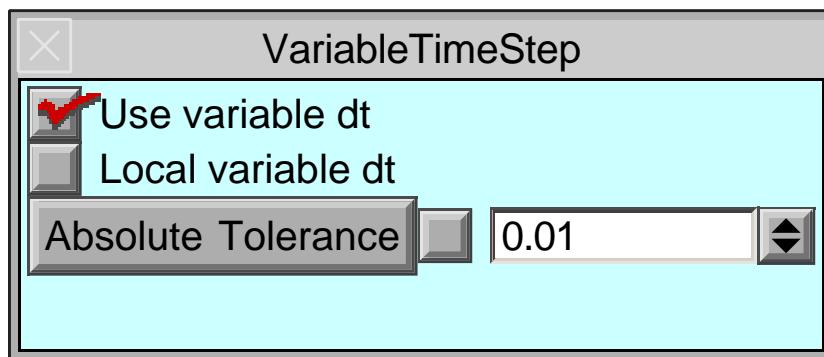






## Control for Variable time step method

### GUI control



### HOC control

```
cvode = new CVode() instance managed by stdrun.hoc  
  
cvode_active(0 or 1)  
cvode_local(0 or 1)
```

## Error Control

$$e_i < RTOL \cdot |y_i| + ATOL_i$$

```
cvode.rtol(0)
```

```
cvode.atol(1e-2)
```

```
cvode.atolscale(&cai(.5), 1e-8)
```

```
STATE {
    cai      (mM)      <1e-8>
    pump    (mol/cm2)  <1e-17>
    pumpca  (mol/cm2)  <1e-17>
}
```

## Use DERIVATIVE block for hh-like channels

```
BREAKPOINT {
    SOLVE states METHOD cnexp
    ina = gnabar*m^3*h * (v - ena)
}

DERIVATIVE states {
    rates(v)
    m' = (minf-m)/mtau
    h' = (hinf-h)/htau
}



---


}

PROCEDURE states() {
    rates(v)
    m = m + m_exp * (m_inf - m)
    h = h + h_exp * (h_inf - h)
}

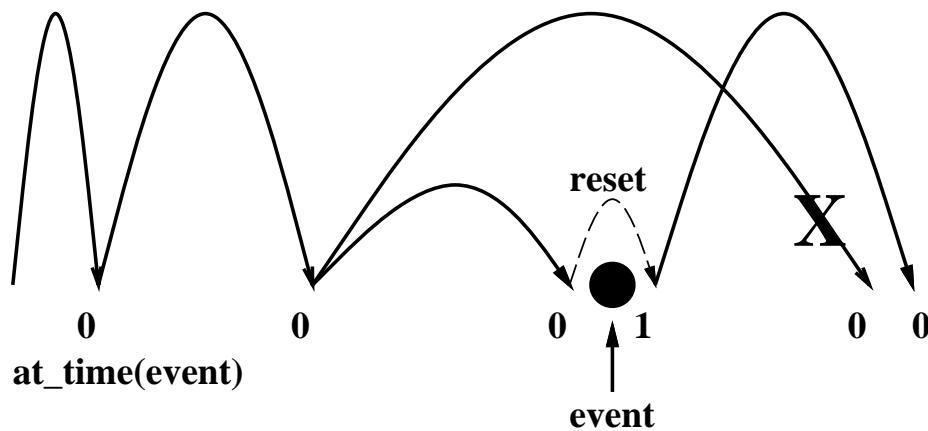
m_exp = 1 - Exp(-dt/tau_m)
```

## Events with CVODE

Generated internally by the model

```
INITIAL {
    i = 0
}
```

```
BREAKPOINT {
    if (at_time(del)) {
        i = amp
    }
    if (at_time(del+dur)) {
        i = 0
    }
}
```



```
INITIAL {
    i = 0
}
```

```
BREAKPOINT {
    at_time(del) at_time(del+dur)
    if (t >= del && t < del + dur) {
        i = amp
    }else{
        i = 0
    }
}
```

Externally generated event

```
NET_RECEIVE(value) {
    i = value
}
```

```
NET_RECEIVE(value) {
    if (flag == 0) {
        i = i + value
        net_send(dur, 1)
    }else{
        i = i - value
    }
}
```

## Abrupt change in state

```
STATE { A (uS) G (uS) }

BREAKPOINT {
    if (gmax && at_time(onset)) {
        state_discontinuity(A, A + E*gmax)
    }
    SOLVE state METHOD sparse
    i = G*(v - e)
}

KINETIC state {
    ~ A <-> G          (k, 0)
    ~ G ->                (k)
}

NET_RECEIVE(weight) {
    state_discontinuity(A, A + E*weight)
}
```

# Communication between cells

Gap junctions

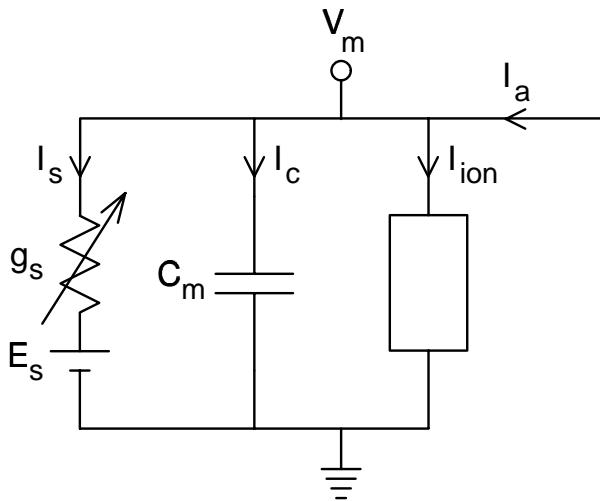
Synapses

# Graded synaptic transmission

## Physical system:

A presynaptic variable governs the continuous release of transmitter, which in turn modulates some property of the postsynaptic cell.

## Conceptual model:



where  $g_s$  is a function of  $V_{pre}$

$$C_m \frac{dV_m}{dt} + I_{ion} = I_a - (V_m - E_s) \cdot g_s(V_{pre})$$

# Graded synaptic transmission

continued

## Computational implementation of model:

### 1. Inefficient hack (don't ever do this!)

At each time step, use a hoc statement  
to update the synaptic mechanism's  $V_{pre}$

```
post_cell.syn.v_pre = pre_cell.axon.v(1)
```

### 2. More efficient: POINTER variable has same effect as

```
section1.mechanism1.variable1(x1) =
    section2.mechanism2.variable2(x2)
```

but is much faster

## NMODL specification of synaptic mechanism

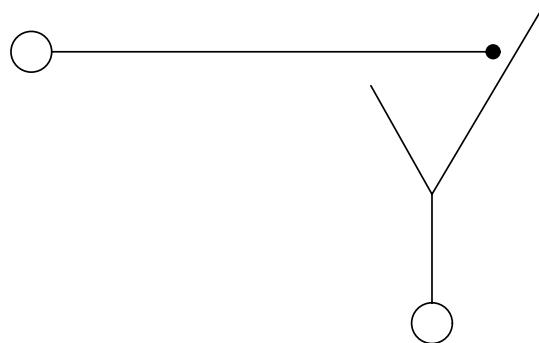
```
NEURON {
    POINT PROCESS Syn
    POINTER v_pre
}
```

## hoc usage

```
objref syn
somedendrite syn = new Syn(0.8)
setpointer syn.v_pre, pre_cell.axon.v(1)
```

# Spike-triggered synaptic transmission

## Physical system:



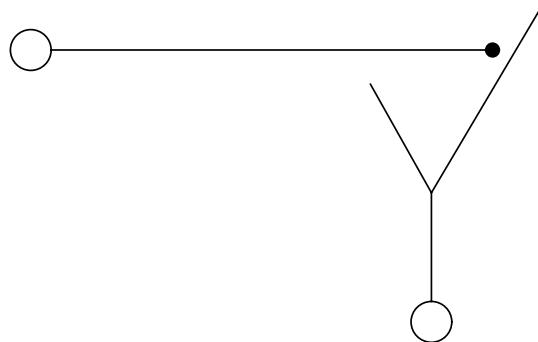
Presynaptic neuron with spike trigger zone and an axon leading to a terminal that makes a synaptic connection onto a postsynaptic cell.

## Conceptual model:

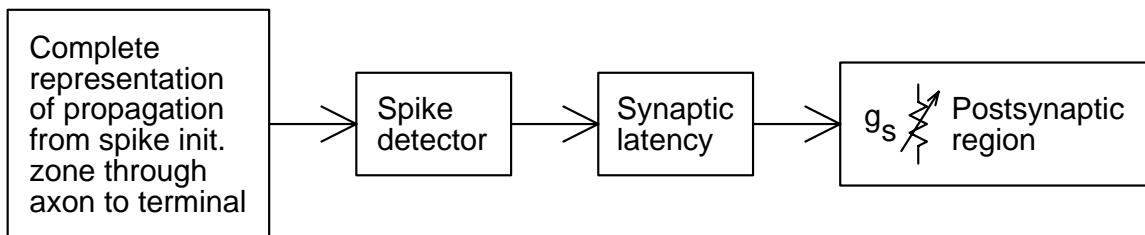
Spike in presynaptic terminal triggers transmitter release; presynaptic details are unimportant

Postsynaptic effect is described by a DE or kinetic scheme that is perturbed by presynaptic spikes

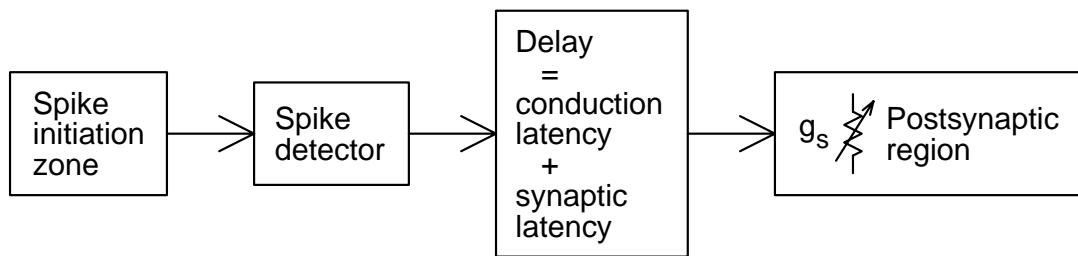
## Computational implementation of model of spike-triggered synaptic transmission:



### The basic idea



### More efficient: "virtual spike propagation"



## The NetCon class

### hoc usage

```
section netcon = new Netcon(&v(x), target,  
                           threshold, delay, weight)  
  
netcon = new Netcon(source, target,  
                     threshold, delay, weight)  
  
section netcon = new Netcon(&v(x), target)  
netcon = new Netcon(source, target)
```

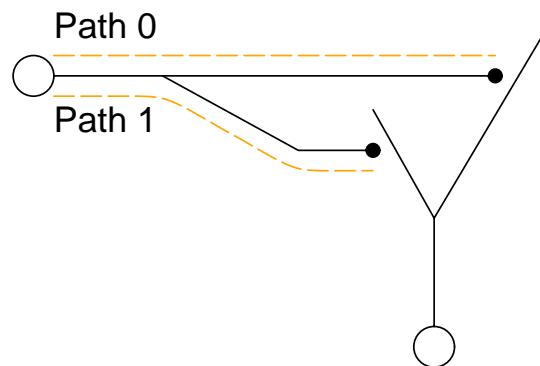
### Defaults

```
threshold = 10  
delay = 1 // must be >= 0  
weight = 0
```

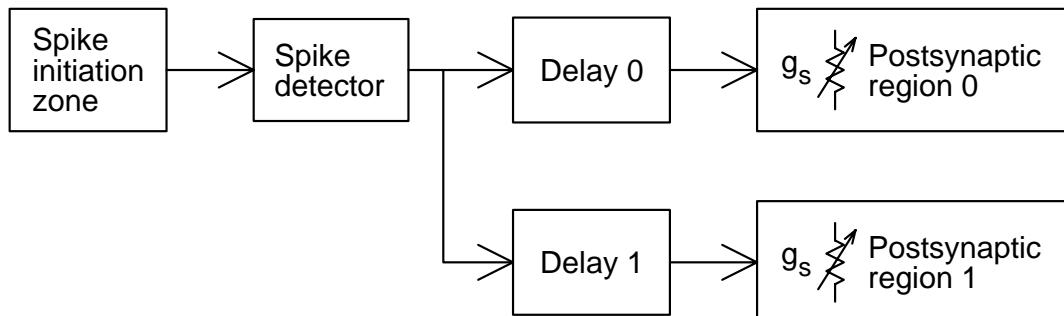
### NMODL specification of synaptic mechanism

```
NET_RECEIVE(weight (microsiemens)) {  
    . . .  
}
```

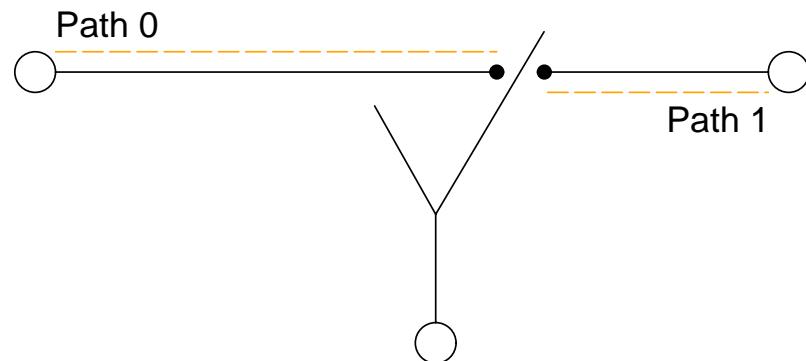
## Efficient divergence



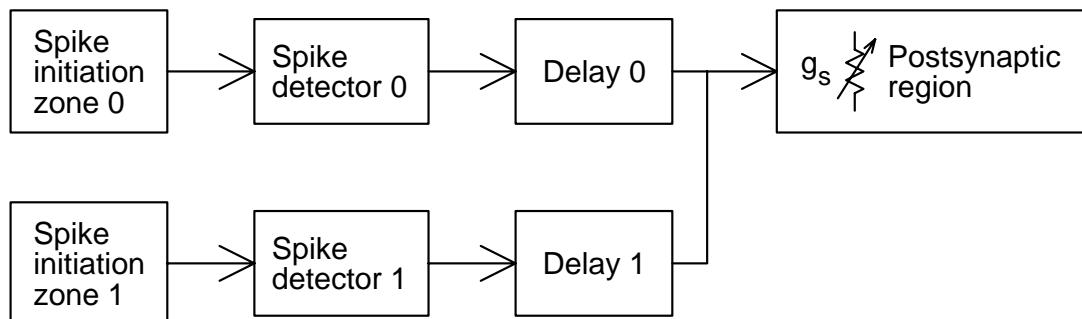
Multiple NetCons with a common source  
share a single threshold detector



## Efficient convergence



NetCons can share a postsynaptic mechanism  
(single equation handles multiple inputs)



## Example: $g_s$ with fast rise and exponential decay

Each synaptic activation produces an abrupt increase of  $g_s$ , which then decays with a single time constant

```

NEURON {
    POINT_PROCESS ExpSyn
    RANGE tau, e, i
    NONSPECIFIC_CURRENT i
}

PARAMETER {
    tau = 0.1 (ms)
    e = 0 (millivolt)
}

ASSIGNED {
    v (millivolt)
    i (nanoamp)
}

STATE { g (micromho) }

INITIAL { g=0 }

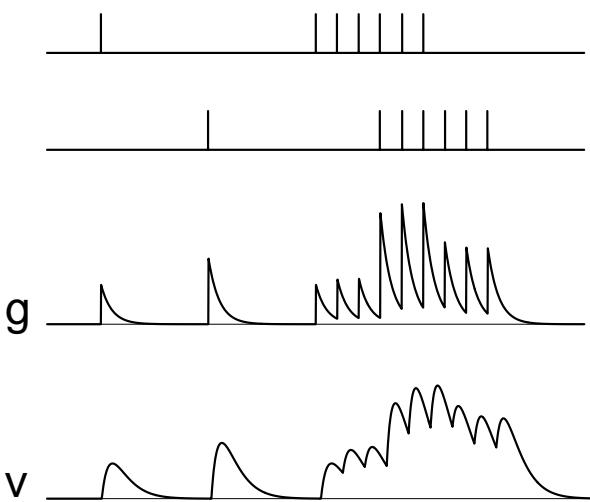
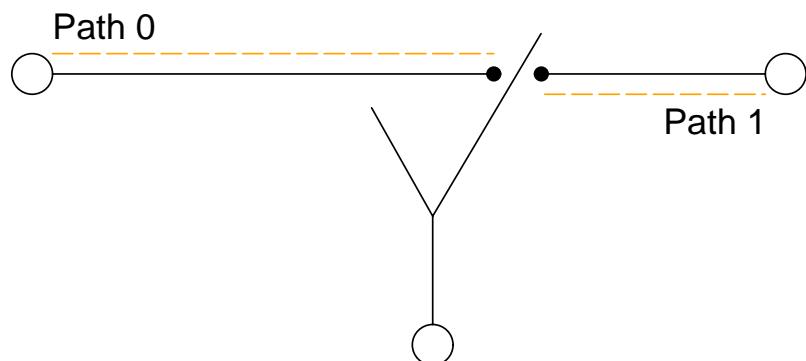
BREAKPOINT {
    SOLVE state METHOD cnexp
    i = g*(v - e)
}

DERIVATIVE state { g' = -g/tau }

NET_RECEIVE(weight (micromho)) {
    state_discontinuity(g, g + weight)
}

```

## Test of ExpSyn



$g$  summarizes linearly

$v$  shows nonlinear summation

## **Spike-triggered synaptic transmission**

Separate specification of what is connected

from

specification of the postsynaptic mechanism



# Network Construction

- 1) Define the types of cells
- 2) Create each cell in the network
- 3) Connect the cells

## Define the types of cells

### "Real" cell types

Sections + density mechanisms + synapses.

The latter are PointProcesses that have a NET\_RECEIVE block that affects membrane current.

ExpSyn  
Exp2Syn

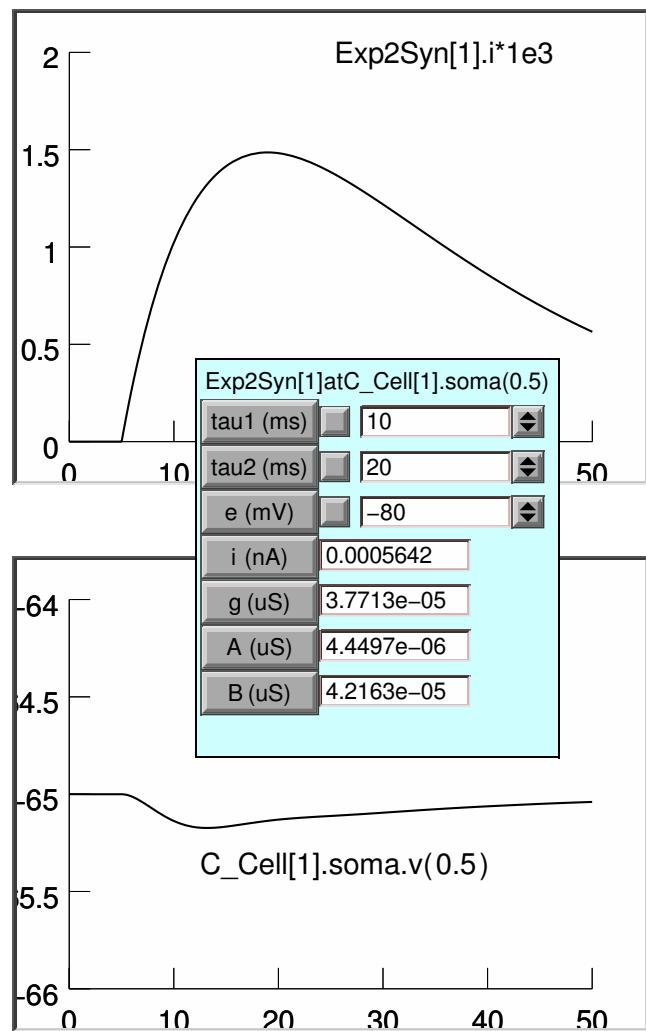
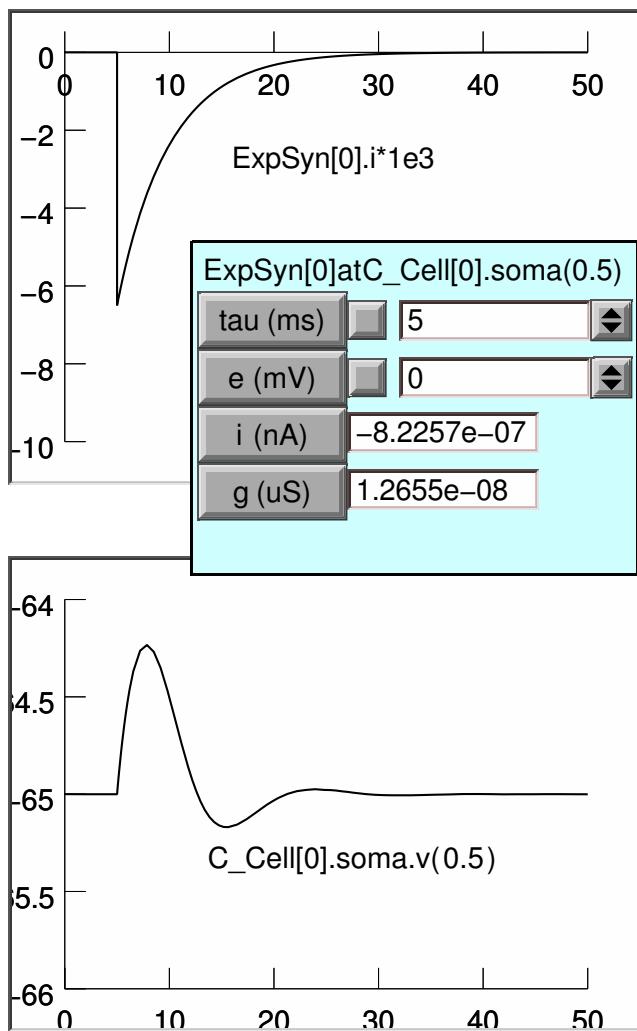
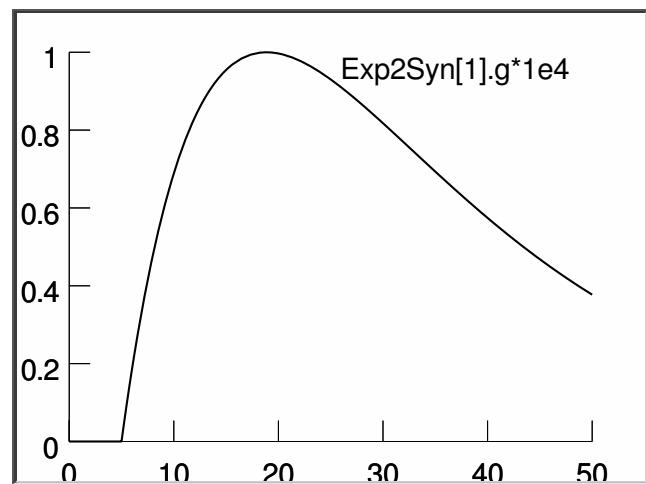
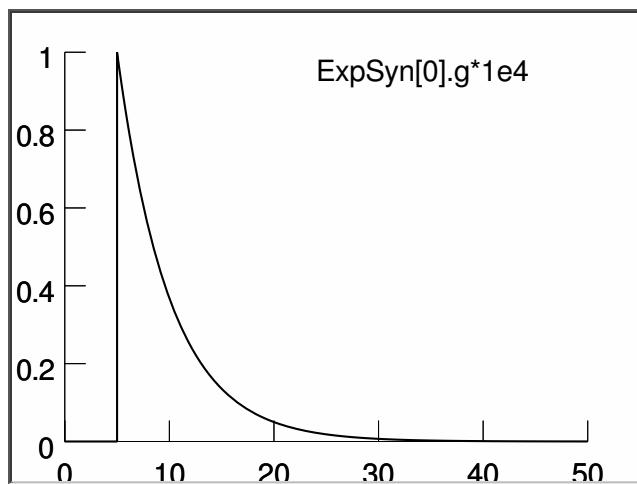
### Encapsulate in a class

```
begintemplate Cell
    public soma, E, I
    create soma
    objref E, I
    proc init() {
        soma insert hh
        soma { E = new ExpSyn(.5)   I = new ExpSyn(.5) }
        I.e = -80
    }
endtemplate Cell
```

## Artificial cell types

PointProcesses that have a NET\_RECEIVE block that calls net\_event

NetStim  
IntFire1  
IntFire2  
IntFire4



## G-Protein synapse -- gsyn.mod

```

NEURON {
    POINT_PROCESS GSyn
    RANGE tau1, tau2, e, i
    RANGE Gtau1, Gtau2, Ginc
    NONSPECIFIC_CURRENT i
    RANGE g
}

PARAMETER {
    tau1=0.1 (ms)
    tau2 = 1 (ms)
    Gtau1 = 20 (ms)
    Gtau2 = 21 (ms)
    Ginc = 1
    e=0      (mV)
}

STATE {
    A (umho)
    B (umho)
}

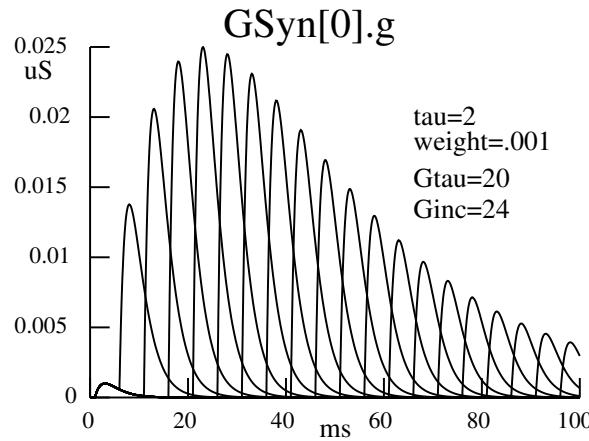
INITIAL {
    LOCAL tp
    A = 0
    B = 0
    tp = (tau1*tau2)/(tau2 - tau1) * log(tau2/tau1)
    factor = -exp(-tp/tau1) + exp(-tp/tau2)
    factor = 1/factor
    tp = (Gtau1*Gtau2)/(Gtau2 - Gtau1) * log(Gtau2/Gtau1)
    Gfactor = -exp(-tp/Gtau1) + exp(-tp/Gtau2)
    Gfactor = 1/Gfactor
}

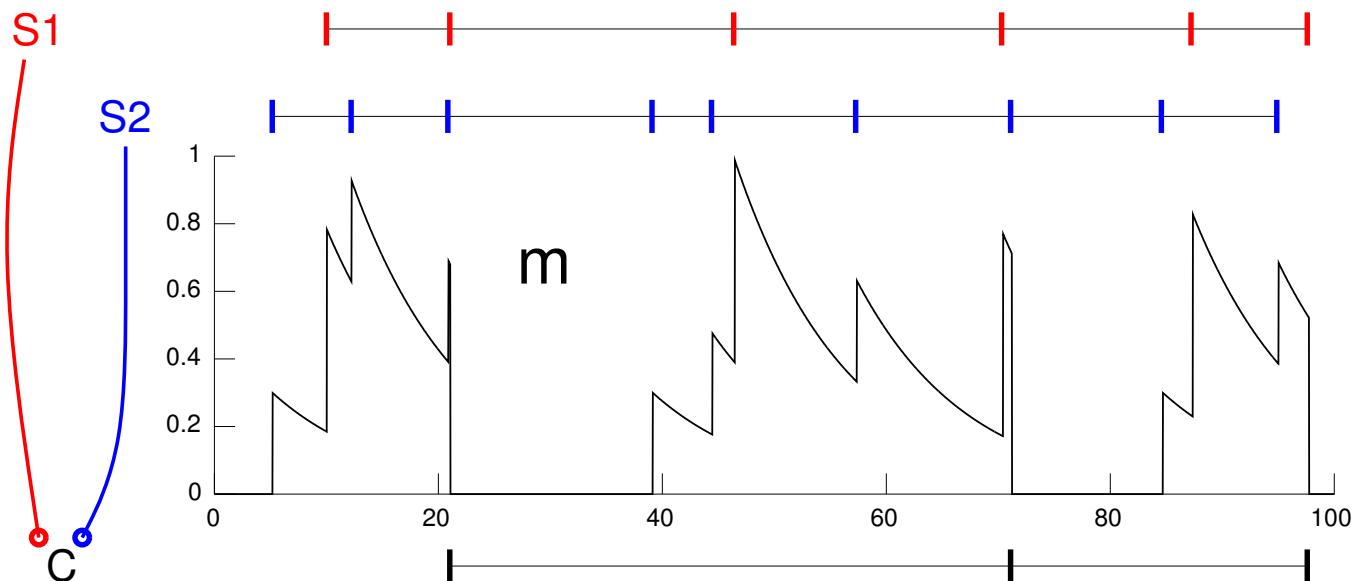
BREAKPOINT {
    SOLVE state METHOD cnexp
    g = B - A
    i = g*(v - e)
}

DERIVATIVE state {
    A' = -A/tau1
    B' = -B/tau2
}

NET_RECEIVE(weight (umho), w, G1, G2, t0 (ms)) {
    INITIAL { G1 = 0 G2 = 0 t0 = 0 }
    G1 = G1*exp(-(t-t0)/Gtau1)
    G2 = G2*exp(-(t-t0)/Gtau2)
    G1 = G1 + Ginc*Gfactor
    G2 = G2 + Ginc*Gfactor
    t0 = t
    w = weight*(1 + G2 - G1)
    state_discontinuity(A, A + w*factor)
    state_discontinuity(B, B + w*factor)
}

```



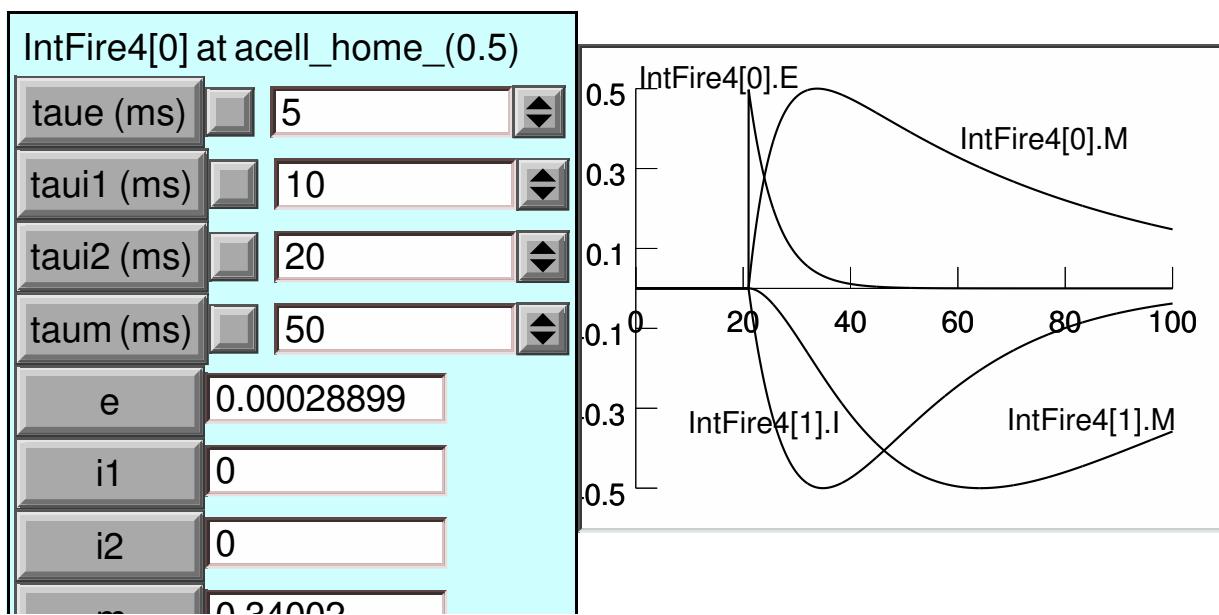
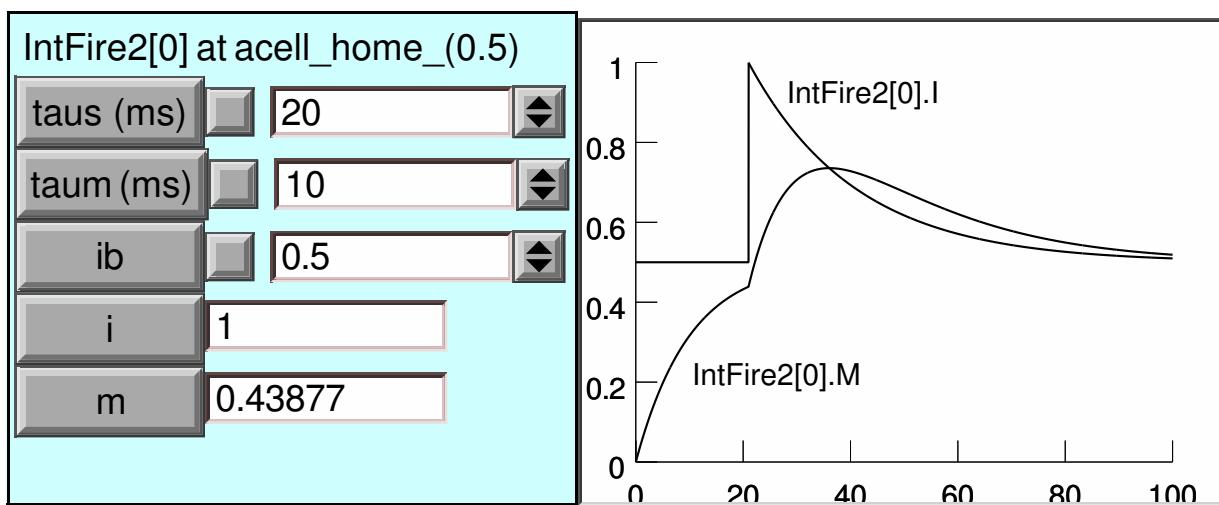
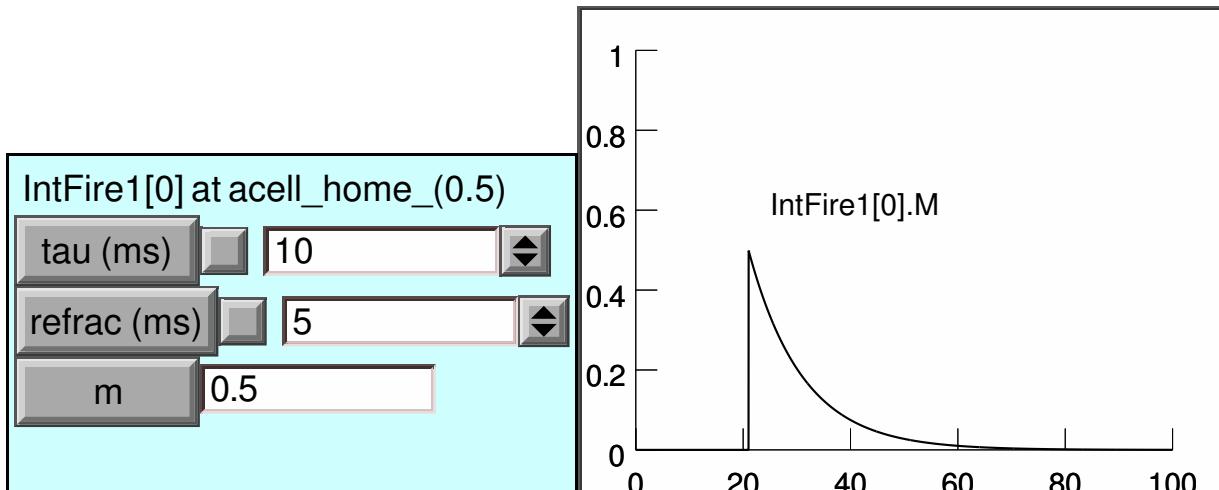


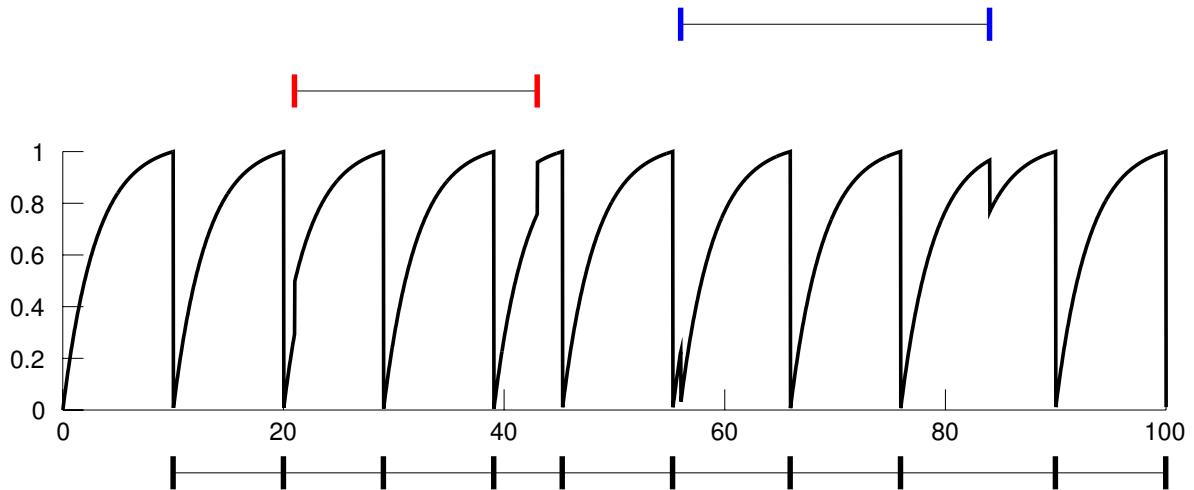
```
NEURON {
    ARTIFICIAL_CELL IntFire
    RANGE tau, m
}
```

...declarations...

```
INITIAL { m = 0 t0 = t }
```

```
NET_RECEIVE (w) {
    m = m*exp(-(t - t0)/tau)
    t0 = t
    m = m + w
    if (m > 1) {
        net_event(t)
        m = 0
    }
}
```





```

: dm/dt = (minf - m)/tau
: input event adds w to m
: when m = 1, or event makes m >= 1, cell fires
: minf is calculated so that the natural
:      interval between spikes is invl

INITIAL {
    minf = 1/(1 - exp(-invl/tau))
    m = 0
    t0 = t
    net_send(firetime(), 1)
}

NET_RECEIVE (w) {
    m = minf + (m - minf)*exp(-(t - t0)/tau)
    t0 = t
    if (flag == 0) {
        m = m + w
        if (m > 1) {
            m = 0
            net_event(t)
        }
        net_move(t+firetime())
    }else{
        net_event(t)
        m = 0
        net_send(firetime(), 1)
    }
}

FUNCTION firetime() { : m < 1 < minf
    firetime = tau*log((minf-m)/(minf - 1))
}

```

## NetCon and NET\_RECEIVE

```
NetCon(source, target, threshold, delay, weight)

Event delivery with axonal delay

Watch the source for threshold crossing in positive
direction.
&soma.v(.5)
PresynapticObject.x
Or PresynapticObject has a NET_RECEIVE block and calls
net_event(t1) (discrete event simulation)

All NetCon objects with same source use same threshold
detector.

If threshold occurs at time, t1, insert
NetCon objects with that source into delivery queue
for delivery at time t2 = t1 + NetCon.delay

Balanced binary tree queue implementation.
No loss of events. Works for delay=0.

Event delivered to target NET_RECEIVE block at time t2.
Same synaptic target equations used by many NetCon s.

All declared NET_RECEIVE arguments are call by
reference with separate storage in each NetCon.
Calculations for different streams can be done once
per event instead of once per dt.

A target can send itself an event with
net_send(delay, flag) and move it to a new time with
net_move(t)

With variable step methods, and 1 or more events at time
t, fadvance() returns at time t before the events are
delivered and at time t after the events are delivered.
```

## ***Wiring networks in Neuron***

Bill Lytton

SUNY - Downstate  
Brooklyn, NY

Wiring networks in Neuron – p.1/4

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- |                                       |   |                                       |
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| 5. Define connectivity                | 6. Hopfield-Brody synchronization model   | 7. Unconnected cells                  |
| 8. Negative (inhibitory) connectivity |   | 9. Q&D synchronization measure        |
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| 13. Scale up to 100 cells             | 14. Need to normalize weights             | 15. NEURON's <i>list</i> object       |
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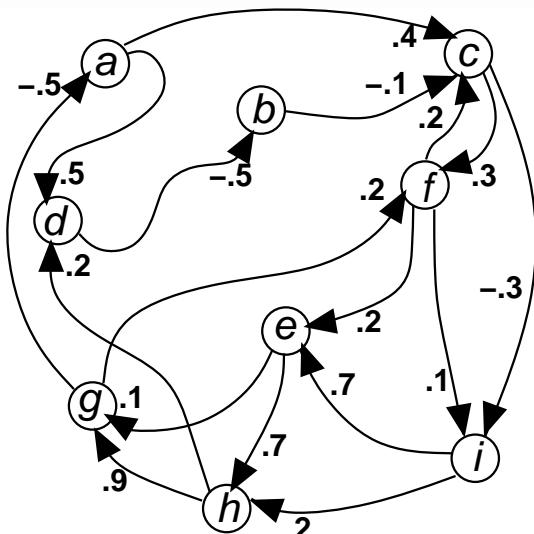
Wiring networks in Neuron – p.2/4

TOC2

- 28. Look at 10% connectivity
  - 29. Show all connections
  - 30. Show selected connections
  - 31. Balancing convergence and divergence
  - 32. Geographic connectivity
  - 33. Random wiring with distance fall-off
  - 34.  $p_{ij} = .5$ : convergence for 10 cells
  - 35.  $p_{ij} = .1$ : lower density to be tested
  - 36. Doesn't sync very well
  - 37. Is there localized sync'ing?
  - 38. How to animate
  - 39. Other explorations
  - 40. Advantages of NEURON for networks

Wiring networks in Neuron – p.3/4

## *Simple network*



Wiring networks in Neuron – p. 4/4

T

## Connections table

<b>FROM</b> ⇒	<i>a</i>	<i>b</i>	<i>c</i>	<i>d</i>	<i>e</i>	<i>f</i>	<i>g</i>	<i>h</i>	<i>i</i>
<b>TO</b> ↓ <i>a</i>	■						- .5		
<i>b</i>		■			- .5				
<i>c</i>	.4	- .1	■				.2		
<i>d</i>	.5			■				.2	
<i>e</i>					■	.2			.7
<i>f</i>			.3			■	.2		
<i>g</i>					.1		■	.9	
<i>h</i>					.7			■	.2
<i>i</i>						.1			■

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Wiring networks in Neuron – p.5/4;

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## Connectivity matrix

$$\begin{pmatrix} 0 & 0 & 0 & 0 & 0 & 0 & - .5 & 0 & 0 \\ 0 & 0 & 0 & - .5 & 0 & 0 & 0 & 0 & 0 \\ .4 & - .1 & 0 & 0 & 0 & .2 & 0 & 0 & 0 \\ .5 & 0 & 0 & 0 & 0 & 0 & 0 & .2 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & .2 & 0 & .7 \\ 0 & 0 & .3 & 0 & 0 & 0 & .2 & 0 & 0 \\ 0 & 0 & 0 & 0 & .1 & 0 & 0 & .9 & 0 \\ 0 & 0 & 0 & 0 & .7 & 0 & 0 & 0 & .2 \\ 0 & 0 & - .3 & 0 & 0 & .1 & 0 & 0 & 0 \end{pmatrix} \begin{pmatrix} a \\ b \\ c \\ d \\ e \\ f \\ g \\ h \\ i \end{pmatrix}$$

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Wiring networks in Neuron – p.6/4;

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## Define connectivity



- ⑥ S=number of syns; D=divergence; C=convergence
- ⑥  $S = C \cdot Post; S = D \cdot Pre$
- ⑥ connectivion density  
 $p_{ij} = C/Pre = D/Post = S/(Pre \cdot Post)$
- ⑥ Below: 1 kind of cell  $\Rightarrow$  Pre and Post are the same

---

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Wiring networks in Neuron – p.7/4;

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## Hopfield-Brody synchronization model



- ⑥ All to all connectivity
- ⑥ Firing cells synchronize due to mutual inhibition
- ⑥ Each cell has a natural period
- ⑥ Inhibition from other cells provides a reset, locking them together

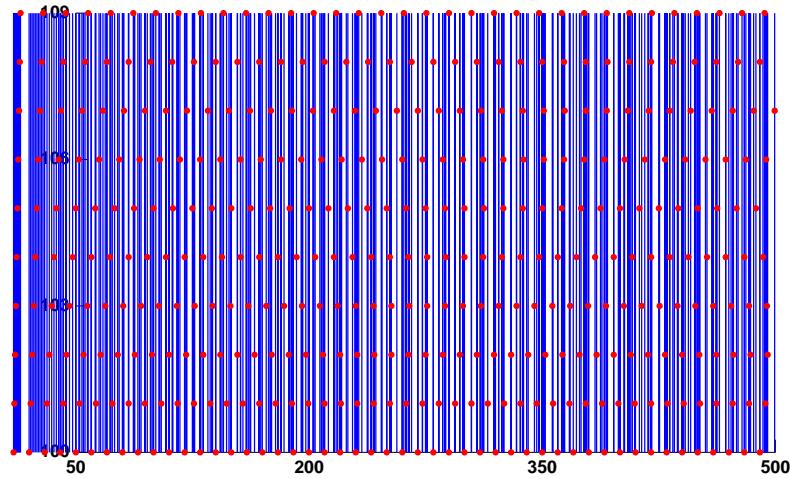
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Wiring networks in Neuron – p.8/4;

### ***Unconnected cells***

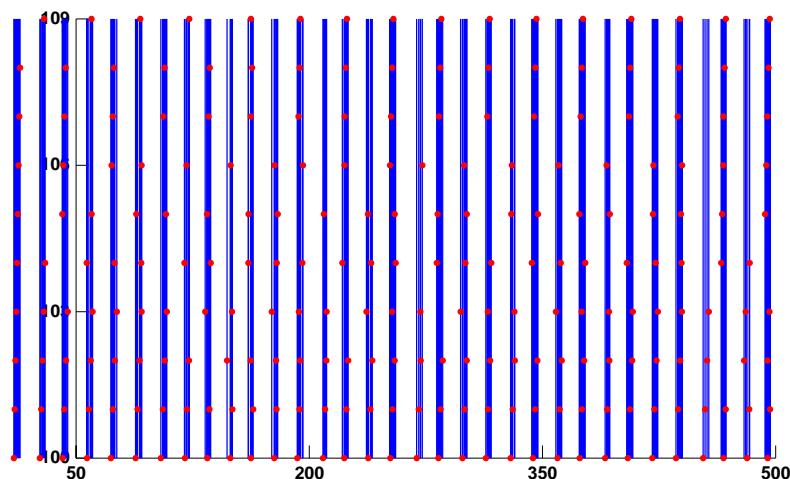
$wt=-1e-5$   
cell fire at own rates and go out of phase



Wiring networks in Neuron – p.9/4;

### ***Negative (inhibitory) connectivity***

$wt=-3e-1$



Wiring networks in Neuron – p.10/4;

T

## ***Q&D synchronization measure***

```
// syncer() :: returns sync measure 0 to <1
// measures how well spikes "fill up" the time bin
// assumes spike times in tvec, tstop
// param: width
func syncer () { local t0,tt,cnt,width
    t0=-1 width=1 cnt=0
    for ii=0,tvec.size-1 {
        tt=tvec.x[ii]
        if (tt>=t0+width) {t0=tt cnt+=1}
    }
    return 1-cnt/(tstop/width)
}
```

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Wiring networks in Neuron – p.11/4;

T

## ***Check sync with increasing inhib***

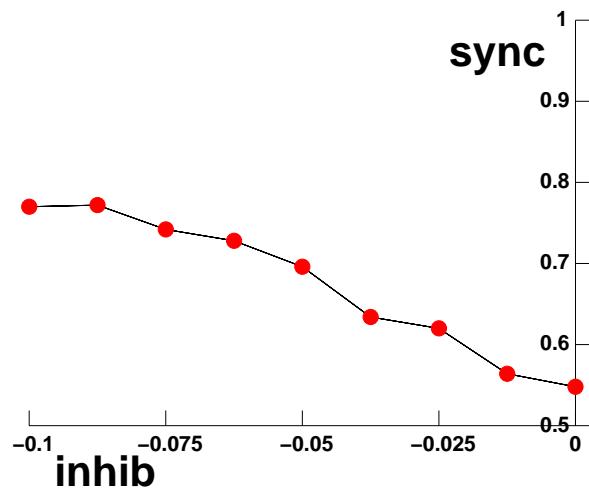
```
// loop increasing neg. synaptic weight
// save measures in vec[1],vec[0]
max= -0.1
for (w=0;w>=max;w+=(max/8)) {
    w+=1e-6 // avoid using zero weight
    setparams() run()
    // g=new Graph() showspks()
    vec[1].append(w) vec.append(syncer())
}
```

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Wiring networks in Neuron – p.12/4;

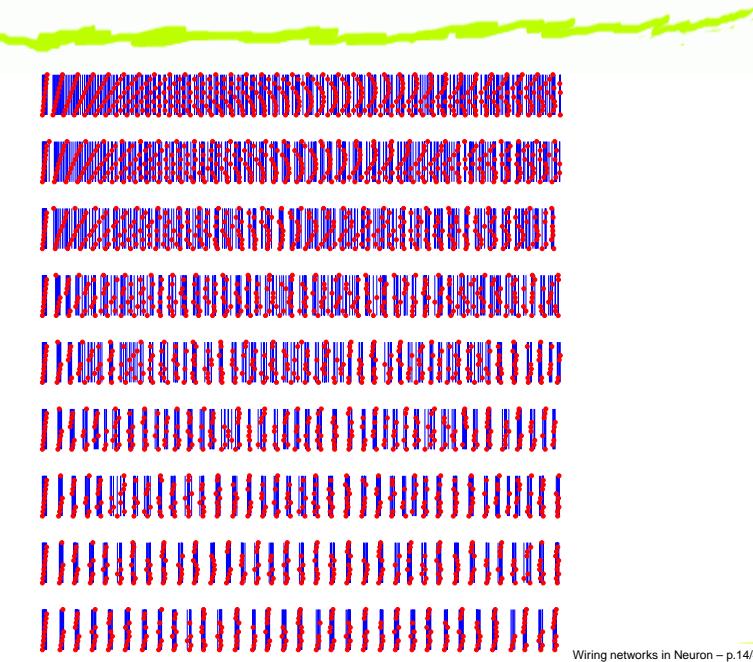
## Graph results

```
{vec.line(g,vec[1]) vec.mark(g,vec[1])}
```



Wiring networks in Neuron – p.13/4;

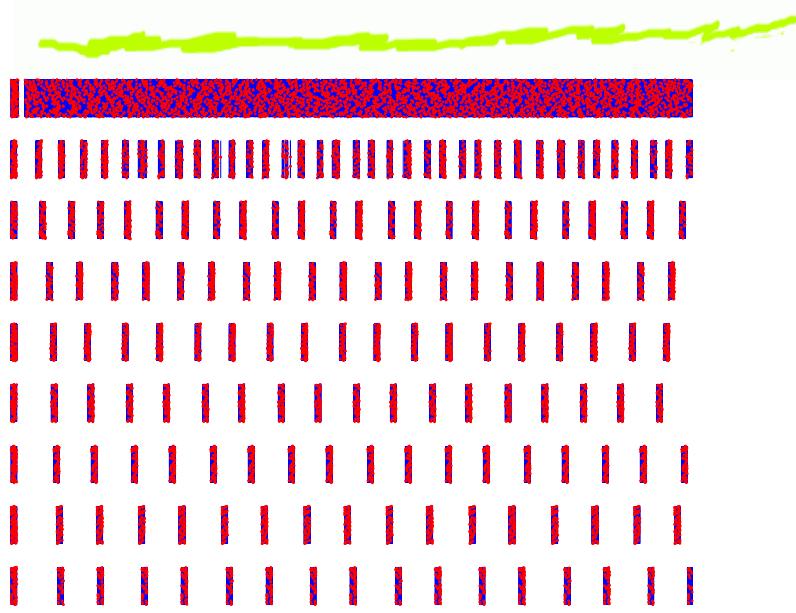
## Confirm with raw data



Wiring networks in Neuron – p.14/4;

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## Scale up to 100 cells

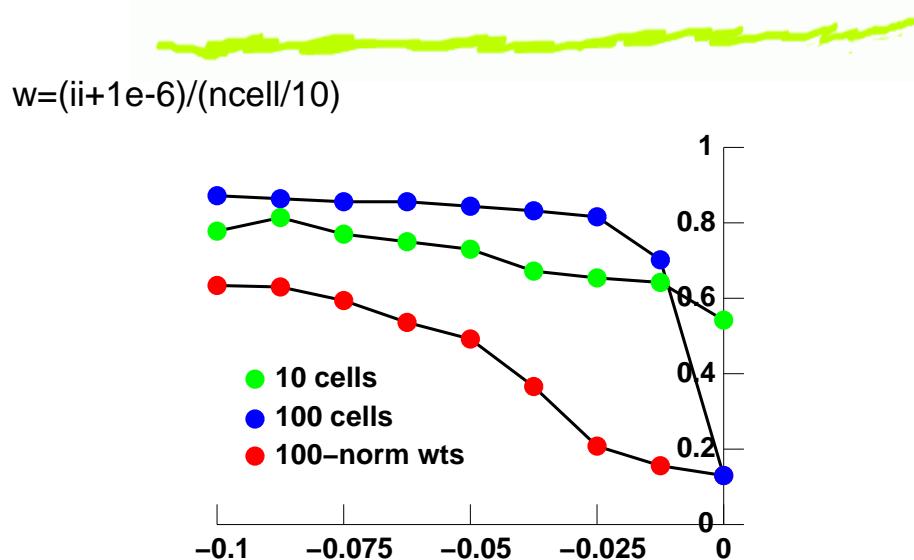


Wiring networks in Neuron – p.15/4;

L

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## Need to normalize weights



Wiring networks in Neuron – p.16/4;

## NEURON's list object

- ⑥ An alternative to object array e.g., objref nc [9900]
- ⑥ Advantage: can change number of objects stored
- ⑥ nclist = new List()
- ⑥ add syn: nclist.append(netcon)
- ⑥ how many?: nclist.count()
- ⑥ retrieve syn #5: netcon=nclist.object(5)
- ⑥ clear: nclist.remove\_all

Wiring networks in Neuron – p.17/4

## Wiring the network

```
// wire():: full non-self connectivity
// artificial cell template have obj.pp
// params: ncell
// creates nclist: list of NetCons
proc wire () {
    nclist.remove_all()
    for i=0,ncell-1 for j=0,ncell-1 if (i!=j)
        netcon = new NetCon(cells.object(i).pp,\n
                            cells.object(j).pp)
        nclist.append(netcon)
    }
}
```

Wiring networks in Neuron – p.18/4

T

***100 x 100 matrix***

- ⑥ Index synapse from 0 →  $S = \text{ncells}^2 - \text{ncells}$
- ⑥ Either set  $p_{ij} \cdot S$  or delete (zero out)  $(1 - p_{ij}) \cdot S$  syns
- ⑥ e.g.,
 

```
rdm.discunif(0,S-1) // random indices
vec.resize((1-pij)*S)
vec.setrand(rdm)
```

—

L

Wiring networks in Neuron – p.19/4;

T

***Rewiring for different densities***

- ⑥ Can either rewire (if sparse) or just set weights to 0 (if not)
- ⑥ rewrite wire():
 

```
// don't create if syn_num is not on list
// note that num of nclist.object(num)
// no longer meaningful
// here array better: 'objref nc[9900]'
for i=0,ncell-1 for j=0,ncell-1 {
    if (i!=j && !vec.contains(i*100+j)) {
        ... new NetCon ...
    }
}
```

—

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Wiring networks in Neuron – p.20/4;

T

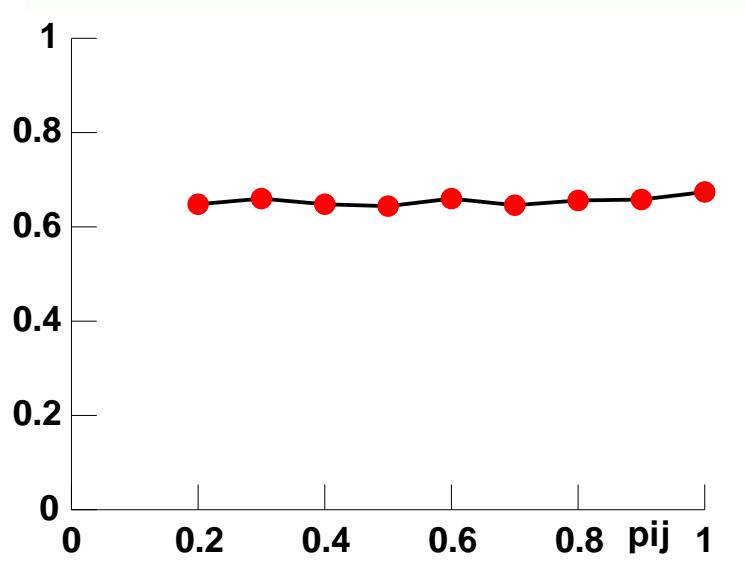
***Or rewrite weight()***

```
// weight2(WT,EXCLUDE_VEC) :: set weight to w
//      unless in EXCLUDE_VEC then set wt. to
proc weight2 () { local i,ww
    w = $1
    for i=0,nclist.count-1 {
        if ($o2.contains(i)) ww=0 else ww=w
        nclist.object(i).weight = ww
    }
}
```

L

Wiring networks in Neuron – p.21/4;

T

***Density doesn't make much difference!***

Wiring networks in Neuron – p.22/4;

## ***Checking connectivity***



- ⑥ Surprising findings are often artifacts
- ⑥ Pseudo-random may be more pseudo than random
- ⑥ Best-written programs of mice & men
- ⑥ Check if network looks reasonable

Wiring networks in Neuron – p.23/4:

## ***cvode.netconlist()***



access NEURON's internal NetCon list

- ⑥ Unwieldy, but important to make sure that WYWIWYG
- ⑥ To check divergence:  

```
for ii=0,ncell-1 print\  
  cvode.netconlist(cells.object(ii).pp,"",")  
  .count
```
- ⑥ To check convergence:  

```
for ii=0,ncell-1 print\  
  cvode.netconlist("", "",cells.object(ii).pi  
  .count
```
- ⑥ Could count non-zero synapses by iterating through  
`cvode.netconlist("", "", "")`

Wiring networks in Neuron – p.24/4:

T

***In addition to cvode.netconlist()***

Develop a parallel database

- ⑥ I often use a sparse matrix for molding connectivity
- ⑥ In present case, we can work with nclist
- ⑥ Beware stray NetCons



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Wiring networks in Neuron – p.25/4

T

***fconn() – find connections***

```
// fconn(PREVEC, POSTVEC) places values of
// pre- and post-syn cells in parallel vectors
// only lists pairs with non-zero connection
// getcnum() returns index of cell obj
proc fconn () {
    $o1.resize(0) $o2.resize(0)
    for ii=0,nclist.count-1 {
        XO=nclist.object(ii)
        if (XO.weight!=0) {
            $o1.append(getcnum(XO.pre))
            $o2.append(getcnum(XO.syn))
        }
    }
}
```

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Wiring networks in Neuron – p.26/4

T

## Now can check non-zero connectivity

- ➊  $p_{ij} = 0.2 \dots$
- ➋ `fconn(vec[4],vec[5])`
- ➌ `print vec[4].size`  
4479
- ➍ Wrong answer!:  $p_{ij} \cdot S \sim 2000$
- ➎ Zero-weighting vector had repeats

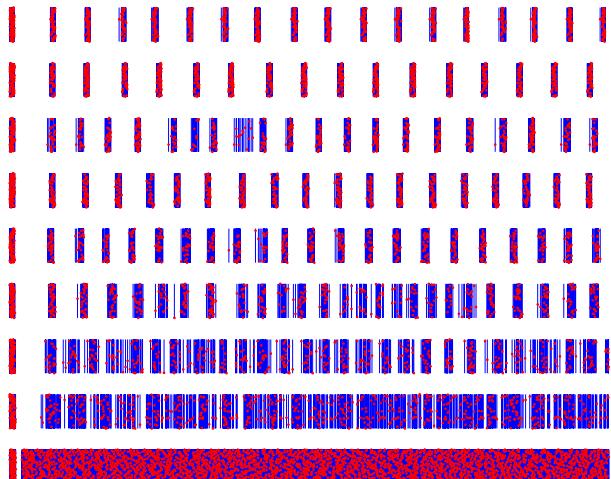
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Wiring networks in Neuron – p.27/4

T

## Rewrite randomizer

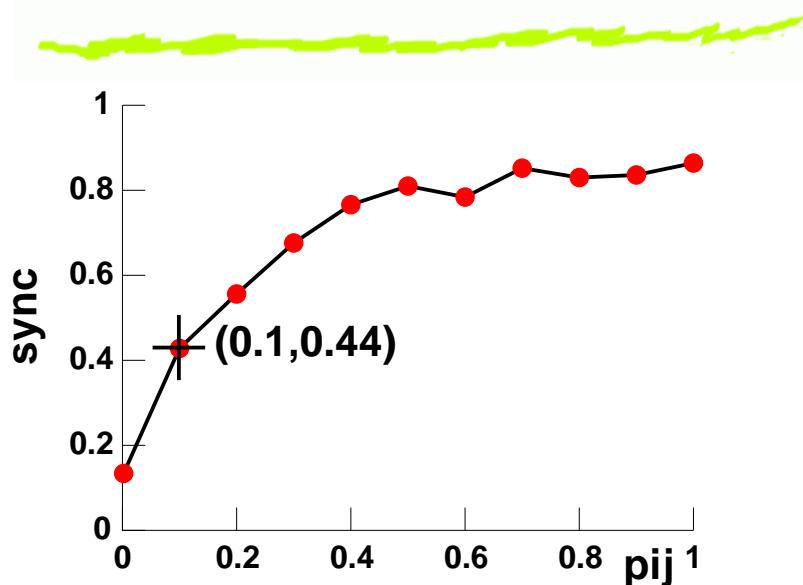
`rdmunq()` – augments vec by n unique vals from rdm  
 scale weights to compensate for reduced convergence



Wiring networks in Neuron – p.28/4

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## Synchronization measure



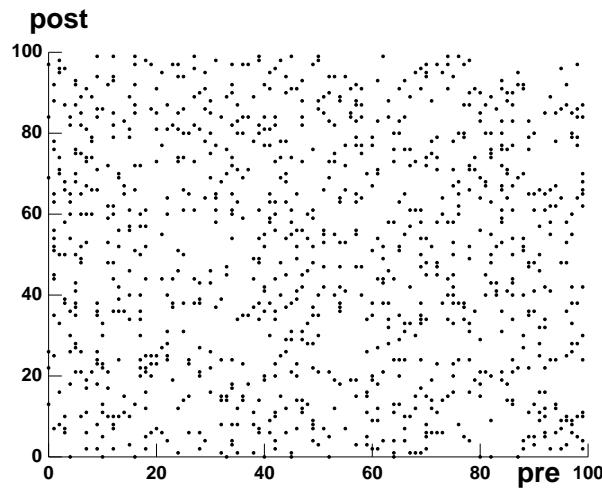
Wiring networks in Neuron – p.29/4;

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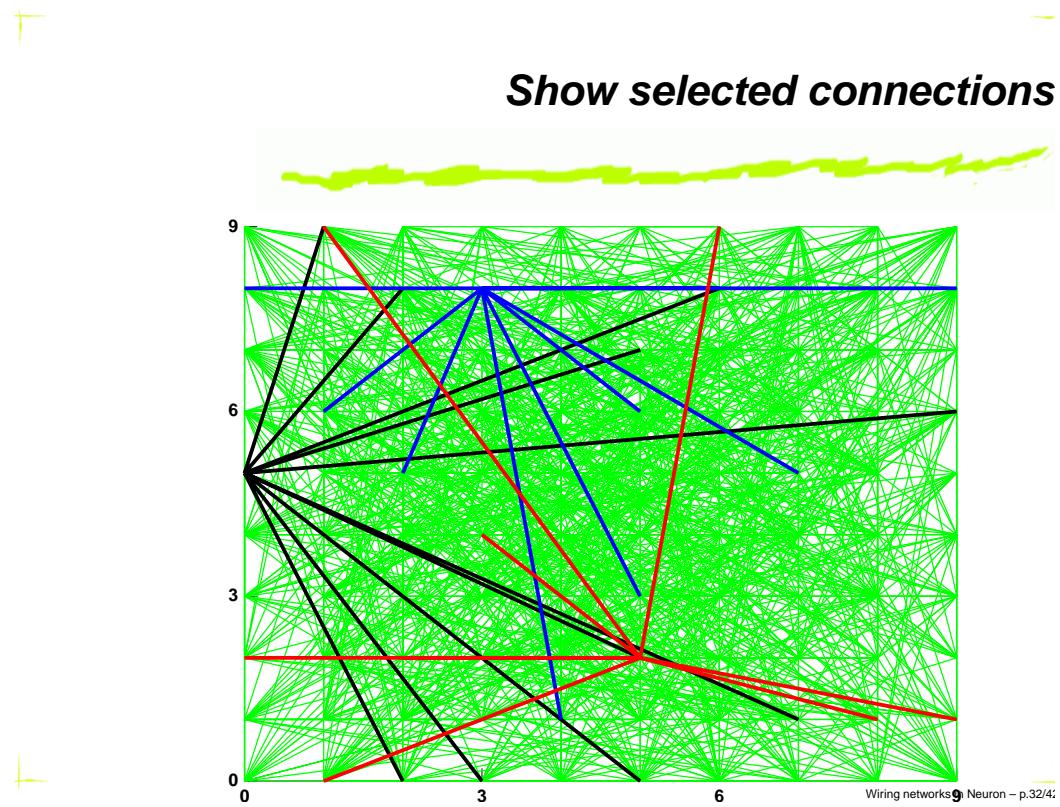
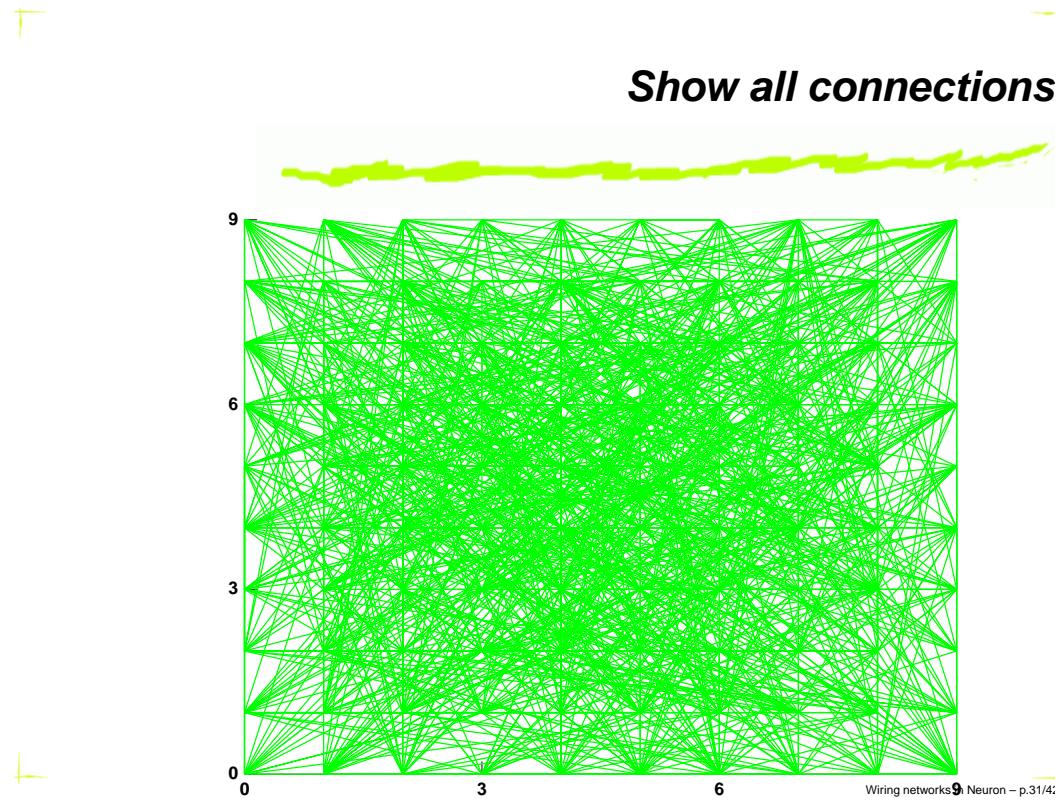
## Look at 10% connectivity

```
{PRE=4 POST=5 fconn(vec[PRE],vec[POST])
vec[POST].mark(g,vec[PRE],"O",2,1,1)}
```



Wiring networks in Neuron – p.30/4;

L



## ***Balancing convergence and divergence***



- ⑥ Wide variation in connectivity:  $\langle C \rangle = 9.91 \pm 2.99$ ;  
 $\langle D \rangle = 9.91 \pm 3.09$
- ⑥  $C_{min} = 3$ ;  $C_{max} = 21$ ;  $D_{min} = 4$ ;  $D_{max} = 17$ ;
- ⑥ With realistic cells, must be careful to balance convergence or will blast some cells

---

Wiring networks in Neuron – p.33/4;

## ***Geographic connectivity***



- ⑥ Neuroanatomy furnishes non-random connectivity
- ⑥ Map onto model connectivity
- ⑥ e.g., fall-off with distance

---

Wiring networks in Neuron – p.34/4;

T

## **Random wiring with distance fall-off**



- ⑥ 1. Go through syns in random order
- ⑥ 2. Flip biased coin proportional to distance
 

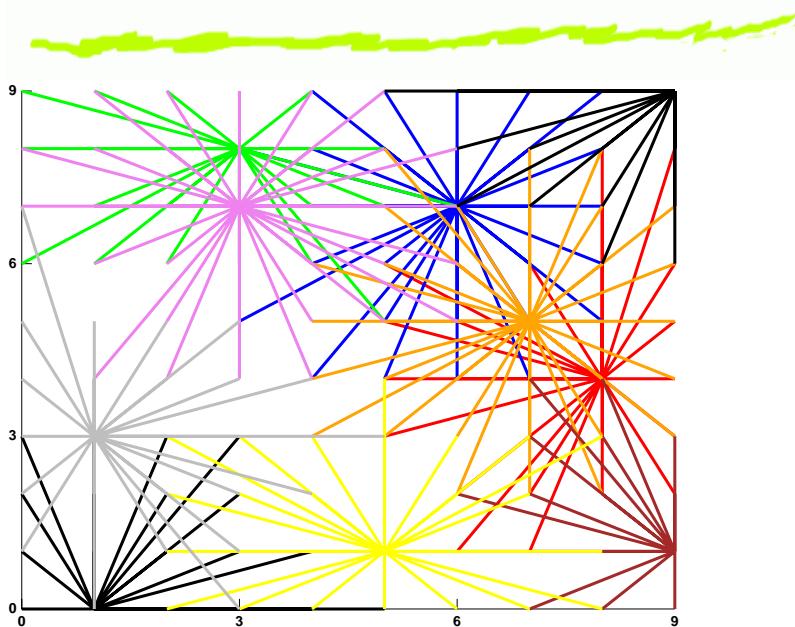
```
rdm[1].uniform(0,1) // for flipping coin
prob = 1-distn()/maxdist
if (rdm[1].repick<prob) { ... }
```
- ⑥ 3. Count syns till reach desired density
- ⑥ Better if used a hexagonal array

L

Wiring networks in Neuron – p.35/4;

T

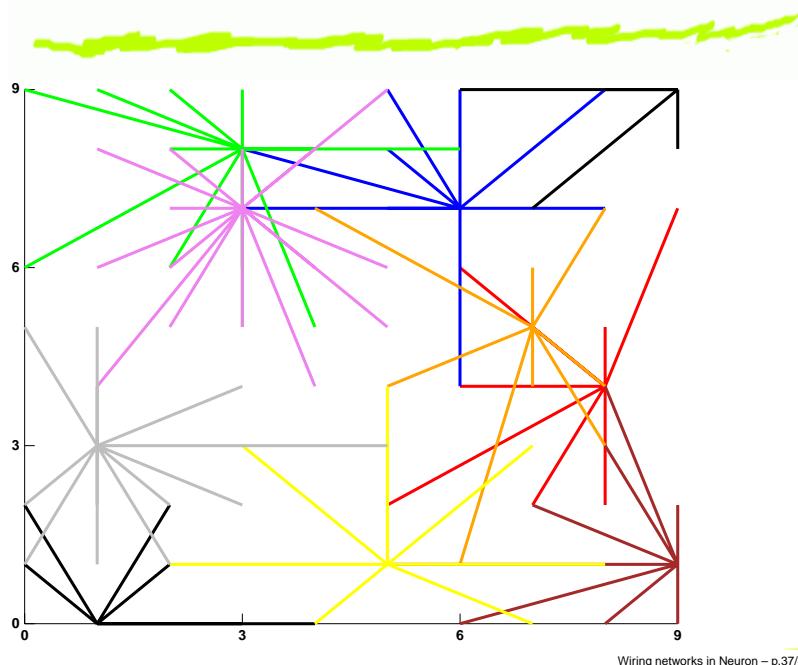
$p_{ij} = .5$ : **convergence for 10 cells**



Wiring networks in Neuron – p.36/4;

T

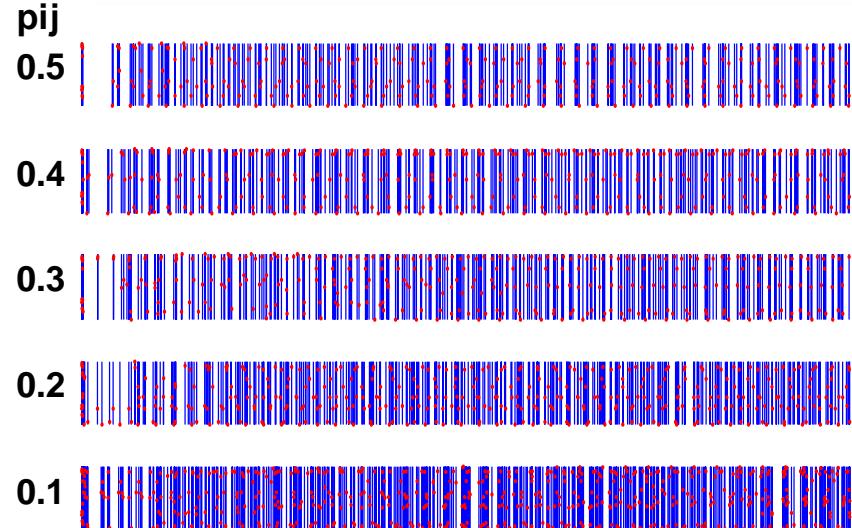
$p_{ij} = .1$ : **lower density to be tested**



L

T

**Doesn't sync very well**



L

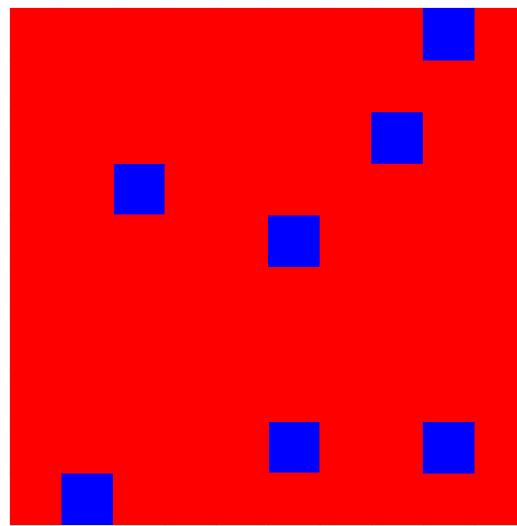
Wiring networks in Neuron – p.38/4;

T

## ***Is there localized sync'ing?***



Look at animation.



Wiring networks in Neuron – p.39/4;

L

T

## ***How to animate***



```
for (tt=0;tt<=tstop;tt+=tstep) {  
    for (;tt>tvec.x[ii];ii+=1){  
        drv.x[animv.indwhere("==",ind.x[ii])]:=  
    for (;tt >scr.x[jj];jj+=1){  
        drv.x[animv.indwhere("==",ind.x[jj])]:=  
    . . .
```

—

—

L

Wiring networks in Neuron – p.40/4;



## ***Other explorations***



- ⑥ Try weight fall-off rather than restricted wiring
- ⑥ Mix excitatory and inhibitory connects ( $\pm$  Dale)
- ⑥ Connect two populations at various densities



Wiring networks in Neuron – p.41/4;



## ***Advantages of NEURON for networks***



- ⑥ Local variable dt
- ⑥ Mix IF and realistic neurons
- ⑥ Flexibility (/learning curve)
- ⑥ Mike & Ted



Wiring networks in Neuron – p.42/4;



## NEURON's standard run system

nrn/share/nrn/lib/hoc/stdrun.hoc  
(MSWin: c:\nrn\lib\hoc\stdrun.hoc)

```
proc init() {
    finitialize(v_init)
}

proc advance() {
    fadvance()
}
```

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## Initialization, broadly speaking:

We want to get the same result every time we click on  
Init & Run, no matter what we did before

Note: this presentation explicitly omits details of initialization  
of ionic concentrations and equilibrium potentials

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## Initialization should assign values at $t = 0$ for

- membrane potential
- gating states
- ionic concentrations
- chemical kinetic states
- voltage across capacitors in linear circuits
- internal states of op amps
- random number generators

## and properly configure

- event queues
- vector record and play
- counters

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**NEURON's `finitiaze()`**

- sets `t = 0`
- clears event queue
- sets up internal data structures that depend on topology and geometry
- initializes `Vector.play` controller
- delivers events whose delivery time is 0
- if `finitiaze` was called with `v_init` argument, sets `v` in all compartments to `v_init`
- calls `INITIAL` block of every inserted mechanism in every segment
- if `extracellular` is used, sets `vext` to 0
- initializes ions; calculates equilibrium potentials if necessary
- initializes mechanisms that `WRITE` ion concentrations; recalcs equilib potentials as needed
- calls all other `INITIAL` blocks
- initializes `LinearMechanism` states
- calls `INITIAL` blocks inside `NET_RECEIVE` blocks; if this spawns network events, delivers any whose delay is 0 to their target `NET_RECEIVE` blocks
- if fixed time step integrator is used, calls all `BREAKPOINT` blocks
- initializes adaptive integrator (if being used)
- initializes any `cvoid.record` and `vector.record` recordings

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**Default initialization: the standard run library**

`nrn/share/nrn/lib/hoc/stdrun.hoc`  
 (MSWin: `c:\nrn\lib\hoc\stdrun.hoc`)

**`stdinit()`**

Called when you

click on Init or Init & Run in the RunControl  
 or  
 enter a new value for `v_init` in the Init button's field editor

```
proc stdinit() {
    realtime=0 // "run time" in seconds
    startsw() // initialize run time stopwatch
    setdt()
    init()
    initPlot()
}
```

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**init()**

Most customizations are made here

```
proc init() {
    finitialize(v_init)
    // User-specified customizations go here.
    // If this invalidates the initialization of
    // variable dt integration and vector recording,
    // uncomment the following code.
    /*
    if (cvode.active()) {
        cvode.re_init()
    } else {
        fcurrent()
    }
    frecord_init()
    */
}
```

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**INITIAL blocks in NMODL****HH-like mechanisms**

```
PROCEDURE rates(v(mv)) {
    minf = alpha(v)/(alpha(v) + beta(v))
    . . .
}
. . .

INITIAL {
    rates(v)
    m = minf
}
. . .
```

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### Kinetic schemes

```

INITIAL {
    SOLVE scheme METHOD steadystate
}
e.g.
NEURON {
    USEION k READ ek WRITE ik
}
STATE { c1 c2 o }
INITIAL {
    SOLVE scheme METHOD steadystate
}
BREAKPOINT {
    SOLVE scheme METHOD sparse
    ik = gbar*o*(v - ek)
}
KINETIC scheme {
    rates(v) : calculate the 4 k rates.
    ~ c1 <-> c2 (k12, k21)
    ~ c2 <-> o ( k2o, ko2)
}

```

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### Default initialization of STATES

Use state0, e.g.

```

PARAMETER {
    state0 = 1
}

```

or alternative syntax

```

STATE {
    state START 1
}

```

It's best to be explicit

```

INITIAL {
    m = m0
    h = h0
}

```

To make them visible from hoc

```

NEURON {
    GLOBAL m0
    RANGE h0
}

```

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## Typical custom initializations

Steady state

- unperturbed system

- system under constant voltage or current clamp

Defined starting point on a trajectory  
of an oscillating or chaotic system

Adjust parameters to meet some condition

### How?

- Use a custom `init()` procedure.

- Load after the standard library, so it won't be overwritten.

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### Initializing to steady state

"Travel into the past," take large steps with implicit Euler, then return to the present.

```
proc init() { local dtsav, temp
    finitialize(v_init)
    t = -1e10
    dtsav = dt
    dt = 1e9
    // if cvode is on, turn it off to do large fixed step
    temp = cvode.active()
    if (temp!=0) { cvode.active(0) }
    while (t<-1e9) {
        fadvance()
    }
    // restore cvode if necessary
    if (temp!=0) { cvode.active(1) }
    dt = dtsav
    t = 0
    if (cvode.active()) {
        cvode.re_init()
    } else {
        fcurrent()
    }
    frecord_init()
}
```

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## Initializing to a desired state

Especially useful for oscillating or chaotic models.

Run a "warmup simulation," then save all states

```
objref svstate, f
svstate = new SaveState()
svstate.save()
```

If desired, write state info to a file for future use

```
f = new File("states.dat")
svstate	fwrite(f)
```

To read from a file

```
objref svstate, f
svstate = new SaveState()
f = new File("states.dat")
svstate.fread(f)
```

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## Initializing to a desired state continued

A custom init() that restores saved states

```
proc init() {
    finitialize(v_init)
    svstate.restore()
    t = 0 // t is one of the "states"
    if (cvode.active()) {
        cvode.re_init()
    } else {
        fcurrent()
    }
    frecord_init()
}
```

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## Initializing to a particular resting potential

One approach: adjust the leakage equilibrium potential  
so that leakage current balances the other ionic currents  
when the cell is at the desired resting potential

Example: for a single compartment model with hh,

```
proc init() {
    finitialize(v_init)
    el_hh = (ina + ik + gl_hh*v)/gl_hh
    if (cvode.active()) {
        cvode.re_init()
    } else {
        fcurrent()
    }
    frecord_init()
}
```

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Alternative strategy: add a mechanism that injects a constant current  
to balance the other currents.

Example:

```
NEURON {
    SUFFIX constant
    NONSPECIFIC_CURRENT i
    RANGE i, ic
}

UNITS {
    (mA) = (milliamp)
}

PARAMETER {
    ic = 0 (mA/cm2)
}

ASSIGNED {
    i (mA/cm2)
}

BREAKPOINT {
    i = ic
}
```

This needs a different custom `init()`

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Custom `init()` to use with constant current mechanism:

```
proc init() {
    finitialize(-65)
    ic_constant = -(ina + ik + il_hh)
    if !(cvode.active()) {
        cvode.re_init()
    } else {
        fcurrent()
    }
    frecord_init()
}
```

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Figure 1

## Anatomy and Empirically-based Models

Quality of data

histology

staining, amputation, shrinkage

human error

diameter

spines

Data formats

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Figure 2

## Tests for Quality of Data

Quick and dirty "litmus test"

insert pas

set Ra and g\_pas low

inject large depolarizing current at soma

examine shape plot of v

Quantitative: look for pt3d data

with suspicious diameters,

e.g. too large or too small, = 0, etc.

A "one liner"

```
forall for i=0, n3d()-1
    if (diam3d(i) == 0)
        print secname(), i, diam3d(i)
```

More quantitative: look for systematic errors, e.g. with a histogram of diameters

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Figure 1

## NEURON's tools for Electrotom Analysis

Input and transfer impedances

Voltage transfer ratio

$$V_{downstream} / V_{upstream}$$

Electrotom transformation

$$\log(V_{downstream} / V_{upstream})$$

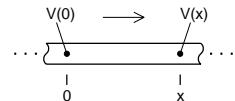
. . . all as functions of  
frequency and space

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Figure 2

## CLASSICAL CABLE THEORY



Infinite cylinder in the steady state

$$V(x) = V(0) e^{-x/\lambda}$$

$x \equiv$  physical distance

$\lambda \equiv$  length constant

Classical Definition of Electrotom Distance:

$$X = \ln V(0) / V(x) = x / \lambda$$

$$\therefore \text{attenuation } A^V(x) = V(0) / V(x) = e^{x/\lambda}$$

Intuitively simple

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Figure 3

BUT neurons  $\neq$  infinite cylinders

Attempted fix: reduce dendritic tree to  
an equivalent cylinder of finite length

Finite cylinder in the steady state

$$A^V(x) = \cosh L_{classical} / \cosh(L_{classical} - X)$$

$$L_{classical} \equiv \text{physical length of cylinder} / \lambda$$

$$X \equiv x / \lambda$$

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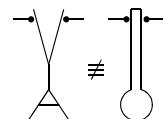
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Figure 4

## The good and the bad news about the equivalent cylinder approximation

### The bad news:

- ◆ Neither intuitive nor simple
- ◆ Destroys the spatial relationships among synaptic inputs



- ◆ Classical electrotom distance  $X \equiv x / \lambda$  fosters conceptual error because it obscures the direction-dependence of attenuation in finite structures

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Figure 5

**The good news:** it's not valid either

Property	Assumption	Truth
Dendritic terminations	electrically equidistant from soma	varies widely
Diameters	cylindrical	irregular
Branch points	3/2 power criterion	no

$$d_p^{3/2} = \sum d_d^{3/2}$$

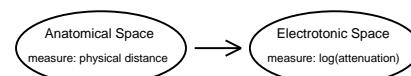
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Figure 6

Alternative: a transformation from anatomical to electrotonic space that

- ✓ is intuitive
- ✓ is empirically-based
- ✓ makes no restrictive assumptions about anatomy



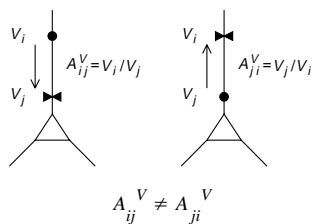
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Figure 7

Foundation of this approach:  
two-port analysis of electrotonus

How well do signals propagate?

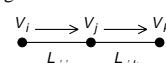


Signal transfer is direction-dependent

Attenuation identities

$$A_{ij}^V = A_{ji}^I \quad A_{ij}^I = A_{ji}^Q$$

$$A_{ik}^V = \frac{V_i}{V_k} = \frac{V_i}{V_j} \frac{V_j}{V_k} = A_{ij}^V A_{jk}^V$$



$$\therefore L_{ik} = L_{ij} + L_{jk}$$

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Figure 8

### The Electrotonic Transformation

Functional definition of electrotonic distance

$$L = \log(\text{attenuation})$$

- ✓ simple, direct relationship to attenuation
- ✓ direction-dependent:  $L_{ij}^V = \ln(A_{ij}^V)$ ,  $L_{ji}^V = \ln(A_{ji}^V)$ , and in general  $L_{ij}^V \neq L_{ji}^V$
- Each physical segment  $ij$  of a cell has **two** representations in electrotonic space—one for each direction of propagation!
- ✓ identical to classical electrotonic distance for an infinite cylinder
- ✓ additive over a path with a consistent direction of propagation

$$A_{ik}^V = \frac{V_i}{V_k} = \frac{V_i}{V_j} \frac{V_j}{V_k} = A_{ij}^V A_{jk}^V$$

$$\therefore L_{ik} = L_{ij} + L_{jk}$$

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Figure 9

### Using the Electrotonic Transformation

At each frequency of interest:

Step 1: Transform from anatomical to electrotonic space

- Compute attenuations between points of interest
- Map into electrotonic space (log)

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Figure 11

**Q:** How does somatic peak PSP amplitude depend on synaptic location?

**A?:**  $A_{in}^V$  (voltage attenuation) or  $k_{syn \rightarrow soma}$  (synapse to soma voltage transfer ratio)?

Time-honored and **wrong!**

- ◆ assumes synapses act like voltage sources.
- ◆ real synapses act more like current sources (Jaffe & Carnevale 1999).

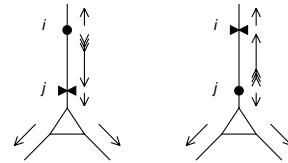
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Figure 10

Step 2: Render graphically with respect to a reference point (because attenuation is direction-dependent)

- A convenient reference: the soma
- Changing the reference point location alters only the direction of signal flow on the direct path between the old and new locations.



Therefore somatocentric renderings of the transform can be rearranged to generate the renderings for any other reference location.

- The attenuation identities give us the transform identities

$$V_{in} = I_{out} = Q_{out} \text{ and } V_{out} = I_{in} = Q_{in}$$

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Figure 11

**Q:** How does somatic peak PSP amplitude depend on synaptic location?

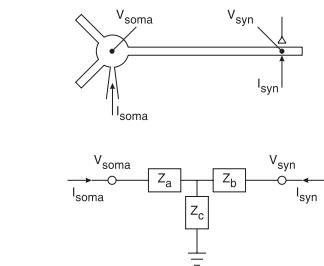
**A?:**  $A_{in}^V$  (voltage attenuation) or  $k_{syn \rightarrow soma}$  (synapse to soma voltage transfer ratio)?

Time-honored and **wrong!**

- ◆ assumes synapses act like voltage sources.
- ◆ real synapses act more like current sources (Jaffe & Carnevale 1999).

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Figure 12



Modified from Fig. 1 in Jaffe & Carnevale 1999.

If synapse  $\approx$  voltage source, then

- $V_{syn}(t) \approx$  independent of synaptic location  
and

- Synapse to soma voltage transfer ratio

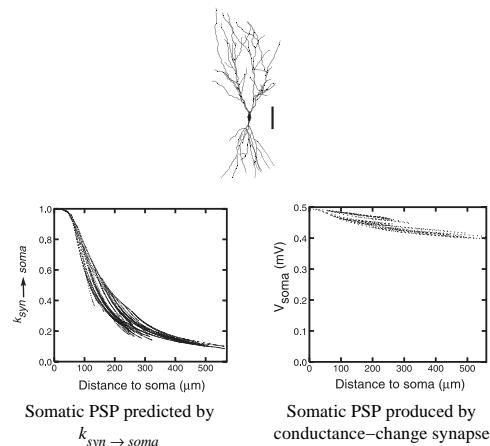
$$k_{syn \rightarrow soma} = 1/A_{in}^V = Z_c / (Z_b + Z_c)$$

predicts the variation of somatic PSP amplitude with synaptic location

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Figure 13



Modified from Fig. 5 in Jaffe &amp; Carnevale 1999.

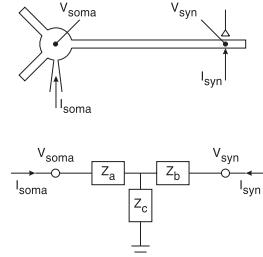
**Q:** Why does  $k_{syn \rightarrow soma}$  fail to predict the relationship between somatic peak PSP amplitude and synaptic location?

**A:** Because synapses act more like current sources than voltage sources.

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Figure 14



Modified from Fig. 1 in Jaffe &amp; Carnevale 1999.

If synapse  $\approx$  current source, then

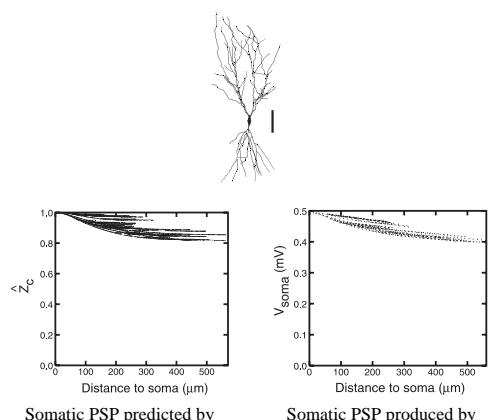
1.  $I_{syn}(t) \approx$  independent of synaptic location  
and

2. Transfer impedance  $Z_c$  predicts the variation of somatic PSP amplitude with synaptic location

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Figure 15



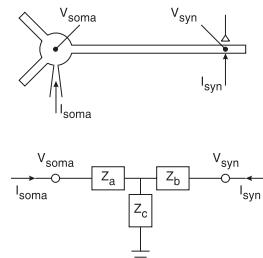
Modified from Fig. 5 in Jaffe &amp; Carnevale 1999.

Normalized transfer impedance  $\hat{Z}_c$  is a good predictor of how somatic PSP amplitude varies with synaptic location.

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Figure 16



Modified from Fig. 1 in Jaffe &amp; Carnevale 1999.

Soma to synapse voltage transfer ratio  $k_{soma \rightarrow syn}$  is identical to normalized transfer impedance  $\hat{Z}_c$ .

Proof:

$k_{soma \rightarrow syn} = Z_c / (Z_a + Z_c)$  but  $Z_a + Z_c$  is  $Z_N^{soma}$ , i.e. the input impedance of the cell at the soma.

Since  $Z_N^{soma}$  is the maximum transfer impedance between any location and the soma,  $k_{soma \rightarrow syn} \equiv \hat{Z}_c$ .

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## **Survey**

We'd appreciate your frank opinions and suggestions to help us refine this course and design future offerings on related subjects.

<b>Please score these items</b>	<b>according to this scale</b>
Overall impression	no opinion 0
Relevance to my research	poor, not helpful 1
Didactic presentations	fair 2
Hands-on exercises	good 3
Written handouts	excellent, very helpful 4
Overhead transparencies	
Computer projection	
Computer classroom	
Food	
Housing	
Best feature	
Weakest feature	

Additional topics that should be covered, topics that should receive more or less coverage, or other suggestions for improvement.

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Circle one

Y    N    I would recommend this course to others who are interested in neural modeling.

My area of primary research interest is \_\_\_\_\_

circle one

Y    N    I have developed my own modeling software using a high-level language (FORTRAN, C/C++ etc.).

Y    N    I have created my own models using modeling software.

Which software? \_\_\_\_\_