Physics of Condensed Matter I

BK FOR 6? = 675

1100-4INZ`PC

Molecules

Faculty of Physics UW Jacek.Szczytko@fuw.edu.pl





Laboratorium magnetometrii SQUID

Adsorption of Doxorubicin onto Citrate-Stabilized Magnetic Nanoparticles Krzysztof Nawara, Jerzy Romiszewski, Krystyna Kijewska, Jacek Szczytko, Andrzej Twardowski, Maciej Mazur, and Paweł Krysinski

J. Phys. Chem. C 2012, 116, 5598–5609.



Figure 5. (A) Magnetization as a function of magnetic field at temperatures ranging from 2 to 300 K. The hysteresis loop is shown in the inset. (B) Magnetization at 300 K (points) and theoretical approach (solid line) proposed by Millan et al.²⁸ for parameters: diameter 12 nm, M_s = 35 emu/g, χ = 1.7e-4 emu/(g·Oe); see text for details.

2015-11-27

Confocal microscopy

Confocal microscopy

Magnetic field up to 9T, temperatures down to 2.0K



Ti-Sa tunable laser 700-1000 nm



Confocal microscopy

Confocal microscopy Magnetic field up to 9T, temperatures dc







-30.87 mV





Tunneling microscope STM









301nm



Topography - Scan forward



X*

0nm

Zawiesina nanomagnesów w polu magnetycznym



Piotr Habdas



Chains of 1 million magnetic nanoparticles have been assembled and disassembled in a solution of suspended particles in a controlled way, scientists at the National Institute of Standards and Technology (NIST) report.

http://www.physics.emory.edu/~weeks/lab/pics.html

Magnetic moment of a single metal nanoparticle determined from



Faraday effect



FIG. 1. Faraday rotation angle due to the inclusion of nanoparticles (θ_F^i) vs external magnetic field (B_{ext}) at different wavelengths of light. Experimental data are marked as points, theoretical curves are solid lines.

Magnetic moment of a single metal nanop

Faraday

determined from

0.2 0.25 0.3 0.35 0.4 Magnetic field B_{ext} (T)

a angle due to the inclusion of nanoparticles (θ_F^i) vs external magnetic aerent wavelengths of light. Experimental data are marked as points, theoretical e solid lines.

Magnetic moment of a single metal nanoparticle determined from

Faraday effect



FIG. 2. Saturated value of Faraday rotation angle $(\theta_F^i)^{sat}$ vs. wavelength of light λ . Solid line represents fit with $\omega_p=198$ nm, $f = 9.2 \times 10^{-5}$, dashed lines is for 188 nm ($f = 1.4 \times 10^{-4}$) and dot-dashed line is for 202 nm ($f = 7.8 \times 10^{-5}$). Experimental data are marked as points.

Magnetic moment of a single metal nanoparticle determined from

Faraday effect



FIG. 3. The normalized Faraday rotation angle $(\theta_F^i)^{norm}$ vs. magnetic field (B_{ext}) for 3 solutions of particles with different diameters of the magnetic core. The diameter was calculated assuming the bulk value of the magnetic moment of an atom $(1.751\mu_B)$. The experiment was performed with the He-Ne laser 633 nm line.

Chemical bonding and molecules

Born Oppenheimer approximation

Full non-relativistic Hamiltonian of the nuclei and electrons:

$$\begin{split} H(\vec{r}, R) \Psi(\vec{r}, R) &= E \Psi(\vec{r}, R) \\ H(\vec{r}, \vec{R}) &= \\ &= -\frac{\hbar^2}{2m} \sum_i \nabla_i^2 - \sum_N \frac{\hbar^2}{2M_N} \nabla_N^2 - \frac{1}{4\pi\varepsilon_0} \sum_{N,i} \frac{Z_N e^2}{|\vec{r}_i - \vec{R}_N|} + \\ &+ \frac{1}{4\pi\varepsilon_0} \sum_{N < K} \frac{Z_N Z_K e^2}{|\vec{R}_N - \vec{R}_K|} + \frac{1}{4\pi\varepsilon_0} \sum_{i < j} \frac{e^2}{|\vec{r}_i - \vec{r}_j|} = \\ &= \hat{T}_e + \hat{T}_N + V(\vec{r}, \vec{R}) + V_e(\vec{r}) + G(\vec{R}) \end{split}$$

 $m, \vec{r_i}, i - ext{electrons}$ $M_N, \vec{R_N}, Z_N - ext{nuclei}$

Coordinates of electrons subsystem and nuclei subsystem (ions) are mixed, separation of electronic and nuclear variables is impossible.

One should use the Born-Oppenheimer adiabatic approximation

Chemical bonding and molecules

Approximations

$$\widehat{T}_N + E_{el}(\vec{r}, \vec{R}) + G(\vec{R})]\chi^n(\vec{R}) = E^n \chi^n(\vec{R})$$

The kinetic energy separates on vibration (oscillation) and rotation energy – we assume "small" oscillations and slow speed of rotataion.

$$\left[\widehat{T}_{osc} + \widehat{T}_{rot} + E_{el}(\vec{r}, \vec{R}) + G(\vec{R})\right] \chi^n(\vec{R}) = E^n \chi^n(\vec{R})$$

Operators act on different coordinates: we can we separate the variables:

$$\chi^{n}(\vec{R}) = \chi^{n}_{osc}(R)\chi^{n}_{rot}(\theta,\varphi)$$
$$E^{n} = E^{n}_{osc} + E^{n}_{rot}$$

Altogether:

$$\Psi(\vec{r},\vec{R}) = \chi^n(\vec{R})\Psi_{el}^n(\vec{r},\vec{R}) = \chi_{osc}^n(R)\chi_{rot}^n(\theta,\varphi)\Psi_{el}^n(\vec{r},\vec{R})$$
$$E^n = E_{osc}^n + E_{rot}^n + E_{el}$$



Chemical bonding and molecules

Approximations

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ine we will discuss: Operators act on different coordinates: we ca tronic structure separate the variables:

$$\chi^{n}(\vec{R}) = \chi^{n}_{osc}(R)\chi^{n}_{rot}(\theta, \varphi) \text{ one we struc}$$

$$E^{n} = E^{n}_{osc} + E^{n}_{rot} \text{ One by one vector onic struc}$$

$$electronic struc$$

Altogether:

$$\Psi(\vec{r},\vec{R}) = \chi^n(\vec{R})\Psi_{el}^n(\vec{r},\vec{R}) = \chi_{osc}^n(R)\chi_{rot}^n(\theta,\varphi)\Psi_{el}^n(\vec{r},\vec{R})$$
$$E^n = E_{osc}^n + E_{rot}^n + E_{el}$$



Electronic structure of molecules

Electronic structure of molecules $E_{el}^{n}(\vec{R})$

Electronic Schrödinger equation takes into account the motion of all the electrons in the molecule, interacting with each other and with fixed potential of nuclei.

The most important is the electrostatic interaction and we take into account only this. Other effects can be considered as perturbation.



Approximation

Each electron moves in the electrostatic field created by fixed nuclei charges and the mean static charge distribution of all other electrons. $\widehat{H}_{el}\Phi = E\Phi$



 $\Phi(\vec{r}_1, \vec{r}_2, \vec{r}_3, \dots \vec{r}_n) = \Psi_1(\vec{r}_1) \Psi_2(\vec{r}_2) \Psi_3(\vec{r}_3) \dots \Psi_n(\vec{r}_n)$

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Approximation

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 $\widehat{H}_{el} = \sum_{i} \widehat{H}_{i}^{0} = \sum_{i} \varepsilon_{i}$ **Molecular Orbital** can be approximately represented as a linear combination of atomic functions which atomic $\widehat{H}_i^0 = \widehat{T}_i + V_i + U_i$ orbitals φ_A , each of which describes a different state of the *i*-th electron, when it is close to the nucleus A. $\widehat{H}_i^0 \Psi_i = \varepsilon_i \Psi_i$ $\Psi_i(\vec{r}) = \sum_A c_A^i \varphi_A(\vec{r})$ $\left|c_{\Lambda}^{i}\right|^{2}$ The probability of finding electron close to th enucleus A

 $\Phi(\vec{r}_1,\vec{r}_2,\vec{r}_3,...\vec{r}_n) = \Psi_1(\vec{r}_1) \,\Psi_2(\vec{r}_2) \,\Psi_3(\vec{r}_3)...\Psi_n(\vec{r}_n)$

The Self-consistent Field Method

Molecular orbital theory

For each of the atomic orbitals φ_A the origin is at another point (orbitals are centered on different atomic nuclei). This method is called **LCAO-MO** (Linear Combination of Atomic Orbitals – Molecular Orbitals).

Theoretically one can take any combination of atomic orbitals, but in reality we take some "adequate" orbitals (resulting from the symmetry - group theory).

The electron wavefunction as a product of molecular orbitals is not a strict eigenfunction of the Hamiltonian, because it does not take into account the correlation of electrons. This function can be improved by adding the expression corresponding to combinations of other atomic orbitals (different atomic configurations). This method is called Configuration Interaction - **CI** (**C**onfiguration Interaction)

In most accurate calculation of the electron wave function for the ground state of the hydrogen molecule H₂ takes into account 100 atomic configuration (W. Kołos).

$$\Psi_i(\vec{r}) = \sum_A c_A^i \varphi_A(\vec{r})$$

The Self-consistent Field Method

LCAO

Numerical solution of electronic Hamiltonian

$$H_{el}(\vec{r},\vec{R})\Psi_{el}^k(\vec{r},\vec{R}) = \left[\hat{T}_e + V(\vec{r},\vec{R}) + V_e(\vec{r})\right]\Psi_{el}^k(\vec{r},\vec{R}) = E_{el}^k(\vec{R})\Psi_{el}^k(\vec{r},\vec{R})$$

Each of the single-electron spinorbital $\varphi_n^{sp}(\vec{r}_n, s_n)$ must be different - two spinorbitals may have for instance the same orbital part φ , but then must have different spin

$$\varphi_n^{sp}(\vec{r}_n, s_n) = \varphi_n^{sp}(\vec{r}_n) \begin{bmatrix} 0\\1 \end{bmatrix} \text{ or } \varphi_n^{sp}(\vec{r}_n) \begin{bmatrix} 1\\0 \end{bmatrix}$$

This $\Psi_{el}^k(\vec{r}_1, \vec{r}_2, \vec{r}_3, \dots, s_1, s_2, s_3, \dots)$ (below) is not a good wavefunction – why?

$$\Psi_{el}^{k}(\vec{r}_{1},\vec{r}_{2},\vec{r}_{3},\ldots s_{1},s_{2},s_{3},\ldots) = \varphi_{1}^{sp}(\vec{r}_{1},s_{1})\varphi_{2}^{sp}(\vec{r}_{2},s_{2})\ldots\varphi_{n}^{sp}(\vec{r}_{n},s_{n})$$

The Self-consistent Field Method

LCAO

Numerical solution of electronic Hamiltonian

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LCAO-MO in Hartree-Fock approximation – self-consistent method, n-electrons wavefunction as a single **Slater determinant**, automatically providing antysymmetry of the wavefunction due to the interchanging the particles occupying any pair of states :

$$\Psi_{el}^{k}(\vec{r}_{1},\vec{r}_{2},\vec{r}_{3},\dots,s_{1},s_{2},s_{3},\dots,s_{1}) = \frac{1}{\sqrt{n!}} \begin{vmatrix} \varphi_{1}^{sp}(\vec{r}_{1},s_{1}) & \varphi_{1}^{sp}(\vec{r}_{2},s_{2}) & \dots & \varphi_{1}^{sp}(\vec{r}_{n},s_{n}) \\ \varphi_{2}^{sp}(\vec{r}_{1},s_{1}) & \varphi_{2}^{sp}(\vec{r}_{2},s_{2}) & \dots & \varphi_{2}^{sp}(\vec{r}_{n},s_{n}) \\ \dots & \dots & \dots & \dots \\ \varphi_{n}^{sp}(\vec{r}_{1},s_{1}) & \varphi_{n}^{sp}(\vec{r}_{2},s_{2}) & \dots & \varphi_{n}^{sp}(\vec{r}_{n},s_{n}) \end{vmatrix}$$

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Homonuclear diatomic molecules, eg. H₂, Li₂, N₂, O₂

Because molecule is diatomic we are looking for a combination of two orbitals φ_A and φ_B .

 $\Psi = c_A \varphi_A + c_B \varphi_B$

If the nuclei are the same:

$$|c_A|^2 = |c_B|^2 \Rightarrow c_A = \pm c_B$$

$$\Psi_+ = N_+(\varphi_A + \varphi_B)$$

$$\Psi_- = N_-(\varphi_A - \varphi_B)$$

$$S = \int \varphi_A \varphi_B \, d\vec{r} \quad \text{overlap integral (całka przekrycia)}$$

$$N_+ = \frac{1}{\sqrt{2(1+S)}} \qquad N_- = \frac{1}{\sqrt{2(1-S)}}$$

Homonuclear diatomic molecules, eg. H₂, Li₂, N₂, O₂

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$$\pi - \text{orbital}$$

3 A

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$$\Psi = c_A \varphi_A + c_B \varphi_B$$

 $S = \int \varphi_A \varphi_B \, d\vec{r}$ overlap integral (*całka przekrycia*)







Homonuclear diatomic molecules, eg. H₂, Li₂, N₂, O₂

$$\begin{split} \Psi &= c_A \varphi_A + c_B \varphi_B \\ S &= \int \varphi_A \varphi_B \, d\vec{r} \quad \text{overlap integral} \\ \varepsilon_{\pm} &= \int \Psi_{\pm}^* \hat{H}^0 \Psi_{\pm} d\vec{r} \\ \varepsilon_{\pm} &= \frac{\int \Psi_{\pm}^* \hat{H}^0 \Psi_{\pm} d\vec{r}}{2(1+S)} \\ \varepsilon_{\pm} &= \frac{H_{AA} + H_{AB} + H_{BA} + H_{BB}}{2(1+S)} \\ \varepsilon_{\pm} &= \frac{H_{AA} - H_{AB} - H_{BA} + H_{BB}}{2(1-S)} \\ \frac{1s}{E_{at}} &= \frac{1s}{E_{at}} \\ H_{AA} &= \int \varphi_A^* \hat{H}^0 \varphi_A d\vec{r} = H_{BB} \approx E_{at} \\ H_{AB} &= \int \varphi_A^* \hat{H}^0 \varphi_B d\vec{r} < 0 \end{split}$$

Homonuclear diatomic molecules, eg. H₂, Li₂, N₂, O₂

$$\Psi = c_A \varphi_A + c_B \varphi_B$$

$$S = \int \varphi_A \varphi_B \, d\vec{r} > 0 \quad \text{overlap integral}$$

$$\varepsilon_{\pm} = \frac{\int \Psi_{\pm}^* \hat{H}^0 \Psi_{\pm} d\vec{r}$$

$$\varepsilon_{\pm} = \frac{E_{at} - |H_{AB}|}{1 + S} \quad \text{bonding orbital}$$

$$\varepsilon_{\pm} = \frac{E_{at} + |H_{AB}|}{1 - S} \quad \text{antibonding orbital}$$

$$H_{AA} = \int \varphi_A^* \hat{H}^0 \varphi_B d\vec{r} < 0$$

Homonuclear diatomic molecules, eg. H₂, Li₂, N₂, O₂

Because molecule is diatomic we are looking for a combination of two orbitals φ_A and φ_B .

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Orbital symbols

• $\lambda = |m_l|$ orbital angular momentum around the internuclear axis

• $\lambda = 0 - \sigma$ -orbitals. These orbitals are not affected by the rotation around the axis of the molecule • $\lambda = 1 - \pi$ -orbitals. These orbitals changes sign after the rotation around the axis of the molecule by π .

• *g* – gerade (even, *parzyste*) parity, inversion through the center of the molecule

• *u* – ungerade (odd, *nieparzyste*).

 $\bullet \pm$ - reflection symmetry with respect to any plane containing the axis of the molecule.

• The number at the beginning – the serial number of the particular orbital type.

Homonuclear diatomic molecules, eg. H₂, Li₂, N₂, O₂

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Fig. 8.13 The parity classification of orbitals in a homonuclear diatomic molecule: (a) g, (b) u.

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Fig. 8.20 The origin of the +/- symmetry classification: (a) a π_- -orbital, (b) a π_+ -orbital.

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H₂⁺ ion

Trial functions of the hydrogen atom (variational method)

 $1\sigma_{u}^{+}$

E

 $1\sigma_{g}^{+}$

 \mathcal{E}_+

 $\Psi_+ = N_+ (1s_A + 1s_B)$

 $\Psi_{-} = N_{-}(1s_A - 1s_B)$





Fig. 8.6 Contour diagrams of the (a) bonding and (b) antibonding orbitals (1σ and 2σ , respectively) of the hydrogen molecule–ion in the LCAO approximation.

1*s*

 E_{at}

H₂⁺ ion

Trial functions of the hydrogen atom (variational method)

 $\Psi_+ = N_+(1s_A + 1s_B)$

 $\Psi_{-}=N_{-}(1s_{A}-1s_{B})$





Fig. 8.5 The molecular potential energy curves for the hydrogen molecule-ion.



Homonuclear diatomic molecules molecular orbital energy scheme

Light molecules (incl. N₂)

Most of the molecules
LCAO

Numerical solution of electronic Hamiltonian

$$H_{el}(\vec{r},\vec{R})\Psi_{el}^{k}(\vec{r},\vec{R}) = \left[\hat{T}_{e} + V(\vec{r},\vec{R}) + V_{e}(\vec{r})\right]\Psi_{el}^{k}(\vec{r},\vec{R}) = E_{el}^{k}(\vec{R})\Psi_{el}^{k}(\vec{r},\vec{R})$$

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Term symbols

Term symbols ${}^{2s+1}\Lambda$

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See: Atkins, Fridman Molecular Quantum Mechanics

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See: Atkins, Fridman Molecular Quantum Mechanics



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Term symbols



Homonuclear diatomic molecules, eg. H₂, Li₂, N₂, O₂

Term symbols



Homonuclear diatomic molecules, eg. H₂, Li₂, N₂, O₂

Term symbols



Electrons energy strongly depends on the distance between nuclei.

E(R) - usually in numerical form.

Approximations: Morse potential eg. Lithium

 $V(r) = D_e [1 - e^{-\alpha(r - r_0)}] + V(r_0)$

Approximations: Lenard-Jones potential

$$V(r) = 4\varepsilon \left[\left(\frac{\sigma}{r}\right)^{12} - \left(\frac{\sigma}{r}\right)^{6} \right] + V(r_{0})$$



P. Kowalczyk

Electrons energy strongly depends on the distance between nuclei.



Electrons energy strongly depends on the distance between nuclei.

E(R) - usually in numerical form.

Approximations: Morse potential eg. Lithium

$$V(r) = D_e [1 - e^{-\alpha(r - r_0)}] + V(r_0)$$

Approximations: Lenard-Jones potential

$$V(r) = 4\varepsilon \left[\left(\frac{\sigma}{r}\right)^{12} - \left(\frac{\sigma}{r}\right)^{6} \right] + V(r_0)$$



Homonuclear diatomic molecules, eg. H₂, Li₂, N₂, O₂

$$\begin{split} \Psi &= c_A \varphi_A + c_B \varphi_B & |c_A|^2 = |c_B|^2 \Rightarrow c_A = \pm c_B \\ S &= \int \varphi_A \varphi_B \ d\vec{r} > 0 & \text{overlap integral} \end{split}$$

 $E_{at,B}$

 $E_{at,A}$



These were

Homonuclear diatomic molecules, eg. H₂, Li₂, N₂, O₂

The molecule is diatomic so we are looking for a combination of two orbitals φ_A and φ_B .



Homonuclear diatomic molecules, eg. H₂, Li₂, N₂, O₂

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 $\Psi = c_A \varphi_A + c_B \varphi_B \qquad |c_A|^2 \neq |c_B|^2$ variational method $\varepsilon < \frac{\int \Psi_{\pm}^* H^0 \Psi_{\pm} d\vec{r}}{\int \Psi_{\pm}^* \Psi_{\pm} d\vec{r}}$ $S = \int \varphi_A \varphi_B \, d\vec{r} > 0$ $\varepsilon(c_A^2 + c_B^2 + 2c_A c_B S) = c_A^2 H_{AA} + c_B^2 H_{BB} + 2c_A c_B S H_{AB}$ $\frac{\partial \varepsilon}{\partial c_A} = \frac{\partial \varepsilon}{\partial c_B} = 0$ $\begin{bmatrix} H_{AA} - \varepsilon & H_{AB} - \varepsilon S \\ H_{AB} - \varepsilon S & H_{BB} - \varepsilon \end{bmatrix} \begin{pmatrix} C_A \\ C_B \end{pmatrix} = 0$ \mathcal{E}_2 $E_{at,B}$ $H_{AA} \approx E_{at,A}$ $E_{at,A}$ $H_{BB} \approx E_{at,B}$ \mathcal{E}_1 Let's assume that $E_{at,A} < E_{at,B}$

Homonuclear diatomic molecules, eg. H₂, Li₂, N₂, O₂

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 $\Psi = c_A \varphi_A + c_B \varphi_B \qquad |c_A|^2 \neq |c_B|^2$ variational method $\varepsilon < \frac{\int \Psi_{\pm}^* H^0 \Psi_{\pm} d\vec{r}}{\int \Psi_{\pm}^* \Psi_{\pm} d\vec{r}}$ $S = \int \varphi_A \varphi_B \, d\vec{r} > 0$ $\varepsilon(c_A^2 + c_B^2 + 2c_A c_B S) = c_A^2 H_{AA} + c_B^2 H_{BB} + 2c_A c_B S H_{AB}$ $\frac{\partial \varepsilon}{\partial c_A} = \frac{\partial \varepsilon}{\partial c_B} = 0$ $\begin{bmatrix} H_{AA} - \varepsilon & H_{AB} - \varepsilon S \\ H_{AB} - \varepsilon S & H_{BB} - \varepsilon \end{bmatrix} \begin{pmatrix} C_A \\ C_B \end{pmatrix} = 0$ \mathcal{E}_2 $E_{at,B}$ $\varepsilon_1 \approx E_{at,A} - \frac{\left(H_{AB} - E_{at,A}S\right)^2}{E_{at,B} - E_{at,A}}$ $E_{at,A}$ $\varepsilon_2 \approx E_{at,B} - \frac{\left(H_{AB} - E_{at,B}S\right)^2}{E_{at,B} - E_{at,B}}$ \mathcal{E}_1

The bonding is strong when:

The large value of the overlap integral S and proportional to it integral H_{AB} . The small difference of the energy of atomic orbitals $E_{at,A}$, $E_{at,B}$. Molecular orbitals **do not have to** be constructed with atomic orbitals of the same type (s - s or p - p).



$$\frac{\partial \varepsilon}{\partial c_A} = \frac{\partial \varepsilon}{\partial c_B} = 0$$

$$\begin{bmatrix} H_{AA} - \varepsilon & H_{AB} - \varepsilon S \\ H_{AB} - \varepsilon S & H_{BB} - \varepsilon \end{bmatrix} \begin{pmatrix} c_A \\ c_B \end{pmatrix} = 0$$

$$\varepsilon_1 \approx E_{at,A} - \frac{\left(H_{AB} - E_{at,A}S\right)^2}{E_{at,B} - E_{at,A}}$$

$$\varepsilon_2 \approx E_{at,B} - \frac{\left(H_{AB} - E_{at,B}S\right)^2}{E_{at,B} - E_{at,A}}$$

 $\varepsilon(c_A^2 + c_B^2 + 2c_A c_B S) = c_A^2 H_{AA} + c_B^2 H_{BB} + 2c_A c_B S H_{AB}$

Example: HF molecule

$F: (1s)^2(2s)^2(2p)^5$ $H: (1s)^1$

- 1. Similar energy values have 2p of F and 1s of H.
- 2. Only $2p_z$ orbital gives non-zero overlap integral with 1s (bonding orbital σ).
- 3. 2 Fluorine electrons $2p_x$ i 2 electrons $2p_y$ are not involved in the HF molecular bonding and are called **lone pair** (*wolna para elektronowa*)
- 4. Similarly fluorine 1s and 2s atomic orbitals do not form a bond with the 1s hydrogen electron because of the large energy difference
- 5. Ground state: ${}^{1}\Sigma^{+}$



Hybridization and overlap integrals





2015-11-27

Hybridization sp, eg. BeH₂

The angle between the bonds is 180°.



Hybridization sp², eg. C_2H_4

The angle between the bonds is 120°.

Ethylene C₂H₄





Hybridization sp³, eg. CH₄

The angle between the bonds is 109,5°.

Methane CH₄

$$h_{1} = \frac{1}{2} (s + p_{x} + p_{y} + p_{z})$$
$$h_{2} = \frac{1}{2} (s + p_{x} - p_{y} - p_{z})$$
$$h_{3} = \frac{1}{2} (s - p_{x} + p_{y} - p_{z})$$
$$h_{4} = \frac{1}{2} (s - p_{x} - p_{y} + p_{z})$$



Hybridization sp³, eg. CH₄

The angle between the bonds is 109,5°.

$$h_{1} = \frac{1}{2} (s + p_{x} + p_{y} + p_{z})$$

$$h_{2} = \frac{1}{2} (s + p_{x} - p_{y} - p_{z})$$

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$$h_{4} = \frac{1}{2} (s - p_{x} - p_{y} + p_{z})$$



http://oen.dydaktyka.agh.edu.pl/dydaktyka/chemia/a_e_chemia/1_3_budowa_materii/01_04_03_2b.htm

Hybridization sp³, eg. CH₄

The angle between the bonds is 109,5°.

$$h_{1} = \frac{1}{2} (s + p_{x} + p_{y} + p_{z})$$

$$h_{2} = \frac{1}{2} (s + p_{x} - p_{y} - p_{z})$$

$$h_{3} = \frac{1}{2} (s - p_{x} + p_{y} - p_{z})$$

$$h_{4} = \frac{1}{2} (s - p_{x} - p_{y} + p_{z})$$



Hybridization

A summary of hybrid orbitals, valence bond theory, VSEPR, resonance structures, and octet rule. Trigonal Trigonal Linear Tetrahedral Octahedral bipyramidal planar sp^2 sp³ dsp³ d^2sp^3 sp BeH₂ BH₃ CH₄ PF₅ SF₆ BF₃ CF₄ PCI₅ IOF₅ BeF₂ CO_2 CH₂O **CCl**₄ **PFCl**₄ PF6 HCN (>C=O) CH₃Cl :SF₄ SiF62->C=C< **HC°CH** :TeF4 NH4⁺ :BrF5 CO32-::CIF3 :NH₃ :IF5 ::BrF3 benzene :PF3 ::XeF4 :::XeF2 graphite :SOF₂ fullerenes ::OH2 :::I3 •NO2 ::SF2 (:::I I2) N_3 :::ICh2 $:00_{2}(0_{3})$ SiO44-:SO₂ PO4³⁻ SO₃ SO42-ClO₄⁻ a lone odd electron : a lone electron pair

electron pairs and lone pairs Atomic around orbitals Hybrid orbitals central combined atom formed VSEPR geometry sp hybrid (2 orbitals) 1s orbital 2 & 1 p orbital linear sp² hybrid (3 orbitals) 1s orbital 3 8. 2 p orbitals trigonal planar sp³ hybrid (4 orbitals) 1 s orbital 4 & 3 p orbitals tetrahedral dsp³ hybrid (5 orbitals) 1 s orbital & 5 3 p orbitals & 1 d orbital trigonal bipyramidal d2sp3 hybrid (6 orbitals) 1 s orbital & 6 3 p orbitals 2 d orbitals

octahedral

http://sparkcharts.sparknotes.com/chemistry/organicchemistry1/section2.php

Bonding

http://www.science.uwaterloo.ca/~cchieh/cact/c120/hybrid.html

2015-1

Hybridization





2015-11-27

Benzene molecule

 σ -bonds (*sp*²) are "localized" and form a rigid skeleton, while π -electrons forming a bond are delocalized.

$$\Psi_{k} = \frac{1}{\sqrt{6}} \sum_{n=1}^{6} e^{\frac{2\pi i}{6}kn} p_{z,n}$$
$$E_{k} = \alpha + 2\beta \cos\left(\frac{2\pi i}{6}k\right)$$
$$k = 0, \pm 1, \pm 2, 3$$

Six of atomic orbitals $2p_z$ gives an equal contribution to all of the molecular orbitals.

These functions correspond to the waves running around the carbon atoms ring in opposite directions for positive and negative values of k



Benzene molecule

$$\Psi_{k} = \frac{1}{\sqrt{6}} \sum_{n=1}^{6} e^{\frac{2\pi i}{6}kn} p_{z,n}$$
$$E_{k} = \alpha + 2\beta \cos\left(\frac{2\pi i}{6}k\right)$$
$$k = 0, \pm 1, \pm 2, 3$$



Friedrich August Kekule 1829 - 1896













Line fit 876pm

dr Jacek Szczytko Michał Kluz Izabela Rytarowska





Topography - Scan forward 175nm Line fit 681 pm Fopography range Onm 0nm 175nm X*



Nanotubes



Different orientations:

- Armchair
- Zig-zag
- Chiral



J.Basak, D.Mitra, S.Sinha "Carbon nanotube: the next generation sensors" presentation

Paweł Tomasz Pęczkowski

2015-11-27

Nanotubes











Single Wall Nanotube (Zig-Zag Type)

Uprolling a Graphene (Zig-Zag Type)

Single Wall Nanotube (Arm-Chair Type)

Uprolling a Graphene (Arm-Chair Type)

Single Wall Nanotube (Chiral Type)





 $\phi = 0.246 (n^2 + nm + m^2)^{1/2} / \pi (nm)$

www.surf.nuqe.nagoya-u.ac.jp/nanotubes/omake/nanotubes/nanotubes.html

Nanomachines



Single – twist

http://www.ipt.arc.nasa.gov

2015-11-27


Single – bend

http://www.ipt.arc.nasa.gov



Single – compress

http://www.ipt.arc.nasa.gov



Multi – twist

http://www.ipt.arc.nasa.gov



Multi – bend

http://www.ipt.arc.nasa.gov



Multi – compress

http://www.ipt.arc.nasa.gov

Space elevator

Counterbalance —

merican Scientist JULY-AUGUST 1997

62,000 mi

MAGAZINE OF SIGMA XI, THE SCIENTIFIC RESEARCH SOCIETY



Space elevator

http://www.spaceelevator.com/

2015-:







Space elevator

LETTERS

Ultralong single-wall carbon nanotubes

L. X. ZHENG¹, M. J. O'CONNELL¹, S. K. DOORN¹, X. Z. LIAO¹, Y. H. ZHAO¹, E. A. AKHADOV¹, M. A. HOFFBAUER¹, B. J. ROOP¹, Q. X. JIA¹, R. C. DYE¹, D. E. PETERSON¹, S. M. HUANG², J. LI¹² AND Y. T. ZHU^{1*}

¹Los Alamos National Laboratory, Los Alamos, New Mexico 87545, USA ²Chemistry Department, Duke University, Durham, North Carolina 27708, USA *e-mail: yzhu@lanl.gov

nature materials | VOL 3 | OCTOBER 2004 | www.nature.com/naturematerials



Cincinnati









Buckminster Fuller pour un exposition en 1967 à Montréal







Solutions in toluene







fcc C_{60} crystals











X.D. Xiang, J.G. Hou, et al. Nature 361, 54, 1993



Zależność Tc od stałej sieci



Benzene + C₆₀



Za wolno



Za szybko



W sam raz

http://www.ipt.arc.nasa.gov

Nanomachines Benzen + CN



Za wolno



W sam raz



Gear Rotation in a Vacuum 200 rot/ns



Powletted //www.ipt.arc.nasa.gov



Gear Rotation at RT 50/70/100 rot/ns





Too fast > 100 rot/ns

http://www.ipt.arc.nasa.gov

Gear Rotation at RT 50 rot/ns

Large Gear Drives Small Gear





Gear and Shaft Operation



Rotation of Gears with Two Off-line Rows of Teeth





Zbyt szybko Long Gear Rotation at Room Temperature





92

Negatively Curved Graphitic Sheet Model of Amorphous Carbon



FIG. 1. Views of two new crystalline schwarzites. Each has 216 carbon atoms per primitive unit cell with 80 six-membered rings (blue) and 24 seven-membered rings (orange). The structure in (a) lies on a P minimal surface in a cubic cell 15.7 Å on a side. The structure in (b) lies on a D minimal surface in an fcc cell whose cubic lattice constant is 24.6 Å.

genus 12 per fcc supercell. The structure has 1248 carbons arranged into 38 five-membered rings (yellow), 394 six-membered rings (blue), 155 seven-membered rings (orange), 12 eightmembered rings (green), and 1 nine-sided ring (pink). Slower annealing produces a structure with many fewer five-membered rings. The cubic unit cell (4 times the volume of the fcc cell shown) is 42.9 Å on a side. Modern Physics Letters B, Vol. 9, No. 22 (1995) 1461-1470 © World Scientific Publishing Company

Schwartzite

IMAGE ANALYSIS OF A NEGATIVELY CURVED GRAPHITIC SHEET MODEL FOR AMORPHOUS CARBON

L. A. BURSILL AND LAURE N. BOURGEOIS School of Physics, The University of Melbourne, Parkville, Vic. 3052 Australia

Received 4 September 1995



QK, She 2

Fig. 2. Random schwartzite model of a surface of genus 12; the volume shown has the shape of a primitive f.c.c cell.

Magnetism in All-Carbon Nanostructures with Negative Gaussian Curvature

Noejung Park,^{1,2} Mina Yoon,³ Savas Berber,³ Jisoon Ihm,^{4,2} Eiji Osawa,⁵ and David Tománek^{3,*}

¹Research Organization for Information Science and Technology, 2-2-54 Naka-Meguro, Meguro-ku, Tokyo 153-0061, Japan ²Center for Nanotube and Nanostructured Composites, Sungkyunkwan University, Suwon, 440-746, Korea ³Department of Physics and Astronomy, Michigan State University, East Lansing, Michigan 48824-2320, USA ⁴School of Physics, Seoul National University, Seoul 151-742, Korea ⁵NanoCarbon Research Institute Limited, Chosei-mura, Chosei-gun, Chiba 2994395, Japan (Received 8 July 2003; published 5 December 2003)



(c)







FIG. 3 (color online). (a) Charge density associated with the four unpaired spins, which are unrelated to the edge states in an sp^2 terminated tetrapod. (b) The wave function of a spin-polarized edge state in an sp^2 terminated (9, 0) nanotube. We use color shading to represent the phase of the wave function.