

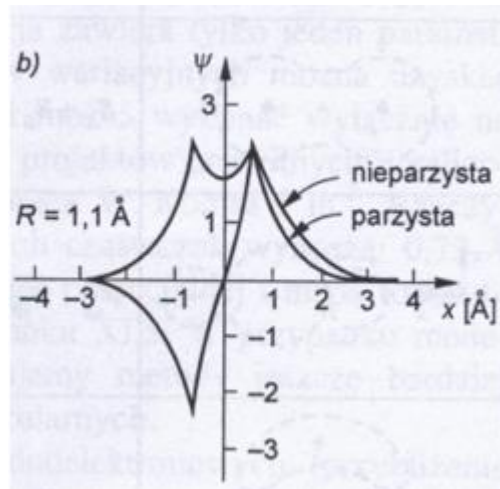
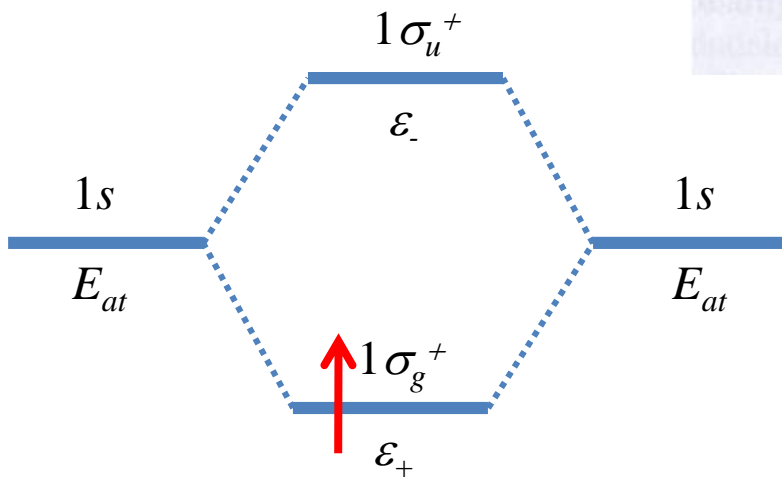
Molecules

H₂⁺ ion

Trial functions of the hydrogen atom
(variational method)

$$\Psi_+ = N_+(1s_A + 1s_B)$$

$$\Psi_- = N_-(1s_A - 1s_B)$$



P. Atkins

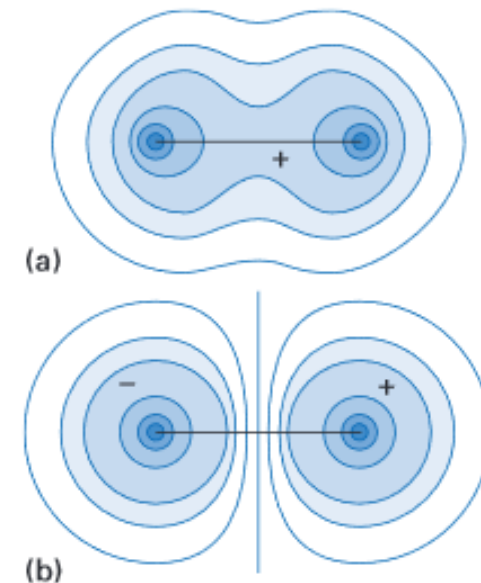


Fig. 8.6 Contour diagrams of the (a) bonding and (b) antibonding orbitals (1σ and 2σ , respectively) of the hydrogen molecule-ion in the LCAO approximation.

Molecules

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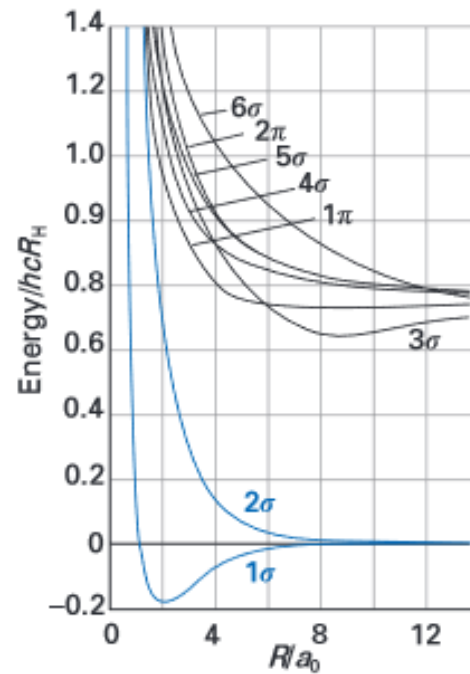
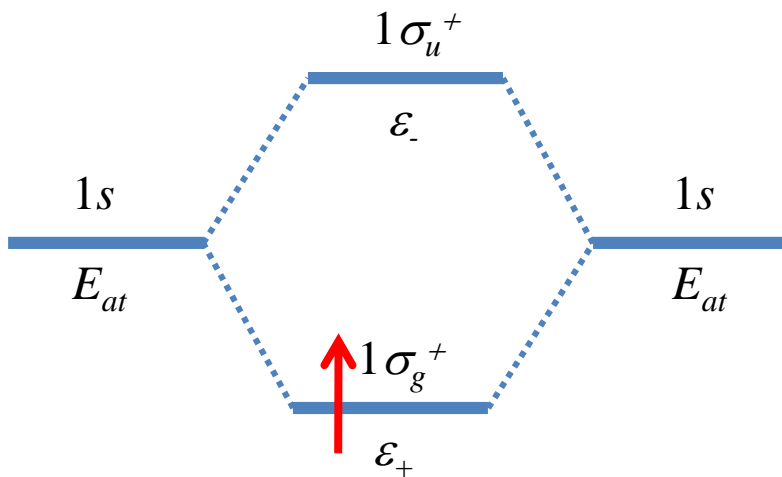
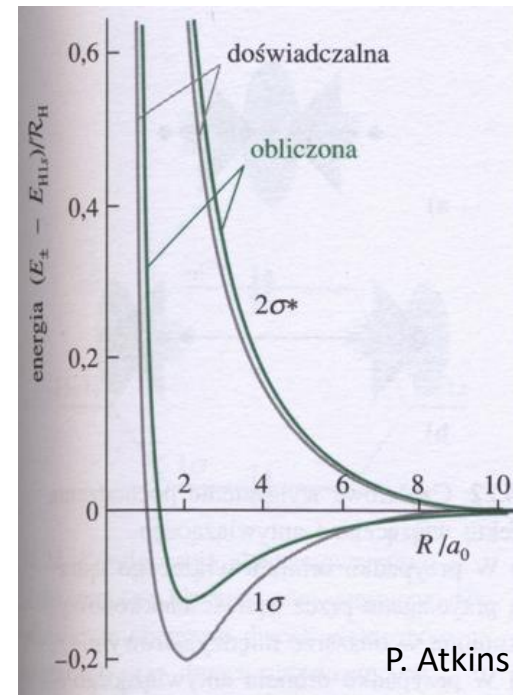


Fig. 8.5 The molecular potential energy curves for the hydrogen molecule-ion.



P. Atkins

Molecules

H₂⁺ ion

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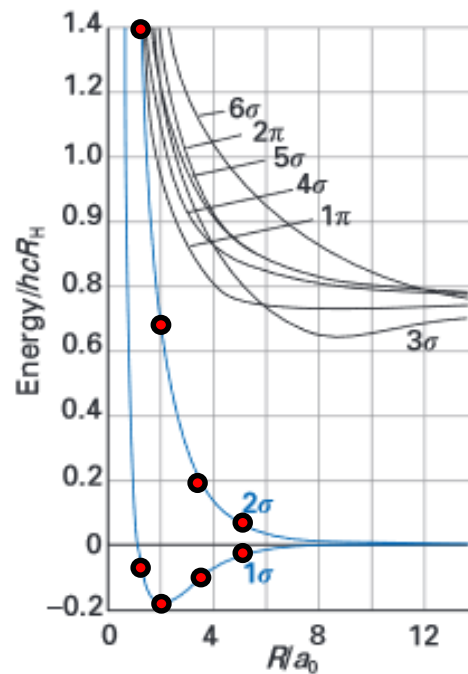
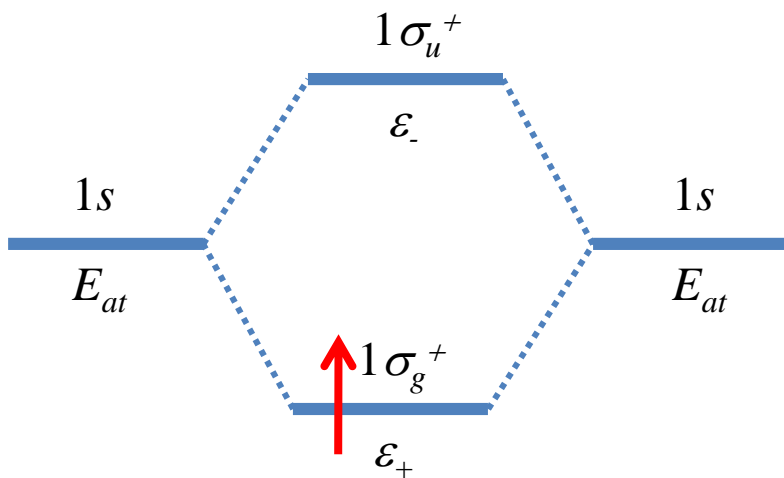
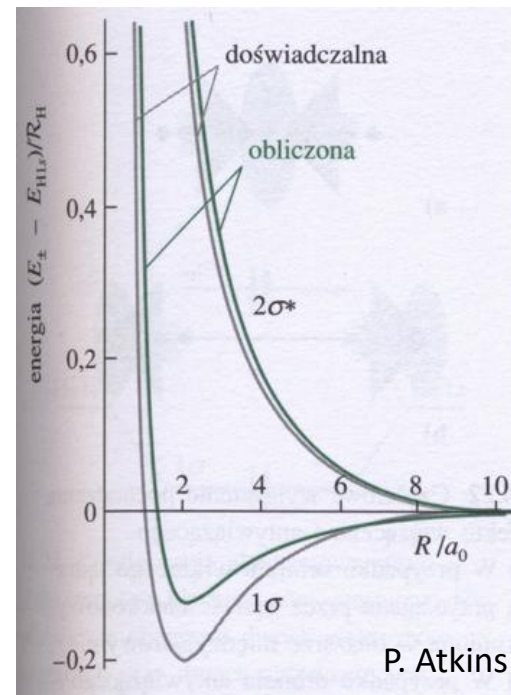


Fig. 8.5 The molecular potential energy curves for the hydrogen molecule-ion.



Electronic states

Electrons energy strongly depends on the distance between nuclei.

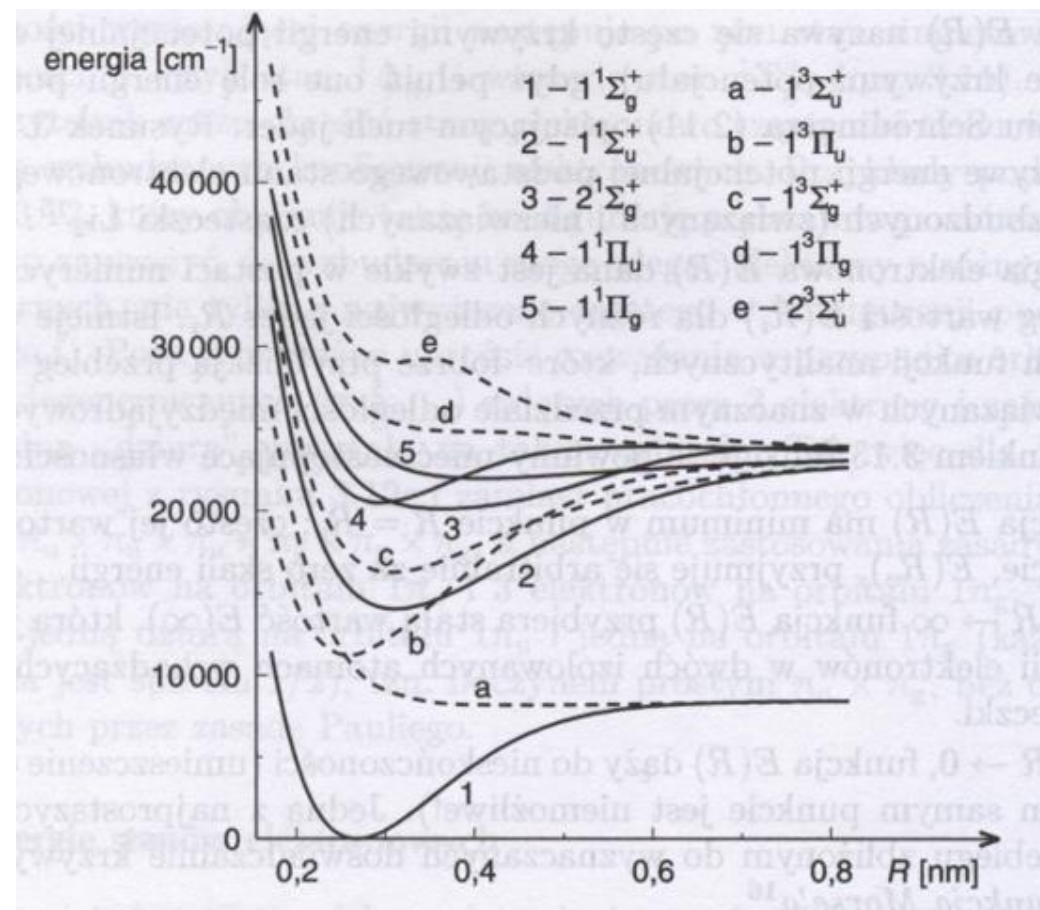
$E(R)$ - usually in numerical form.

Approximations: Morse potential
eg. Lithium

$$V(r) = D_e [1 - e^{-\alpha(r-r_0)}] + V(r_0)$$

Approximations: Lenard-Jones potential

$$V(r) = 4\varepsilon \left[\left(\frac{\sigma}{r} \right)^{12} - \left(\frac{\sigma}{r} \right)^6 \right] + V(r_0)$$



P. Kowalczyk

Electronic states

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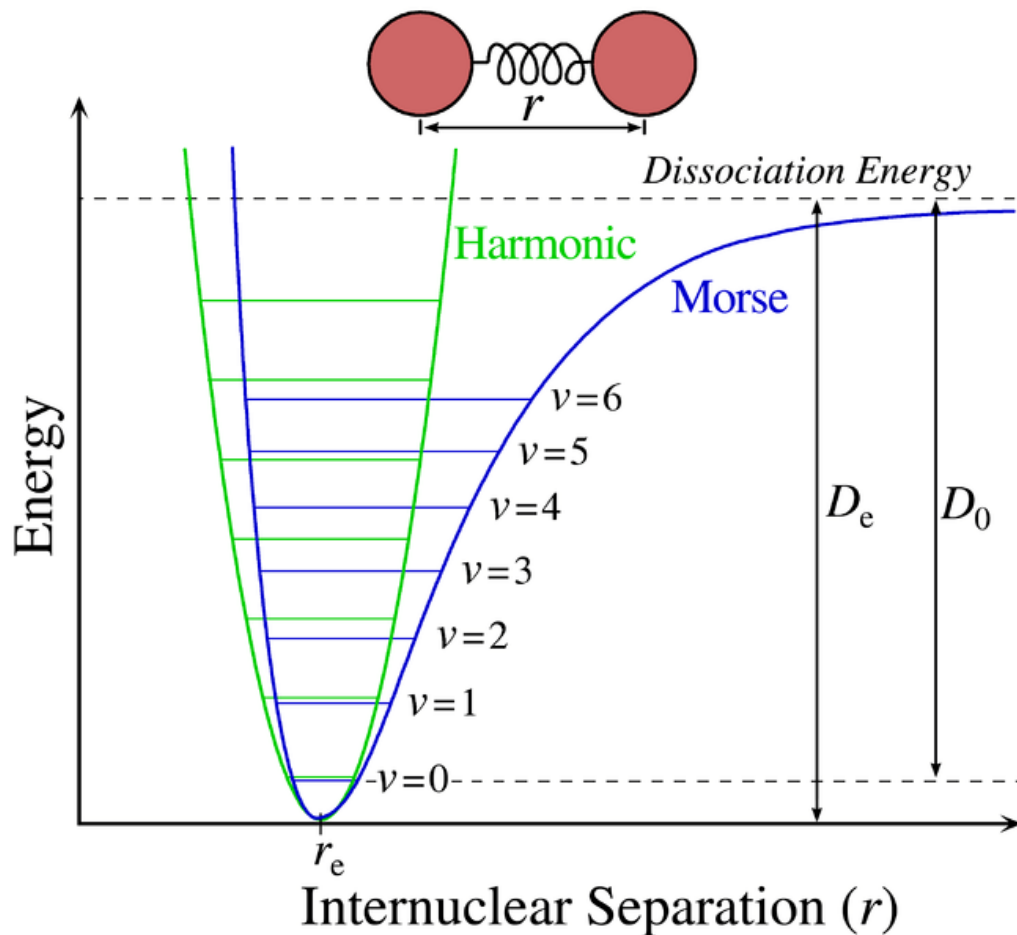
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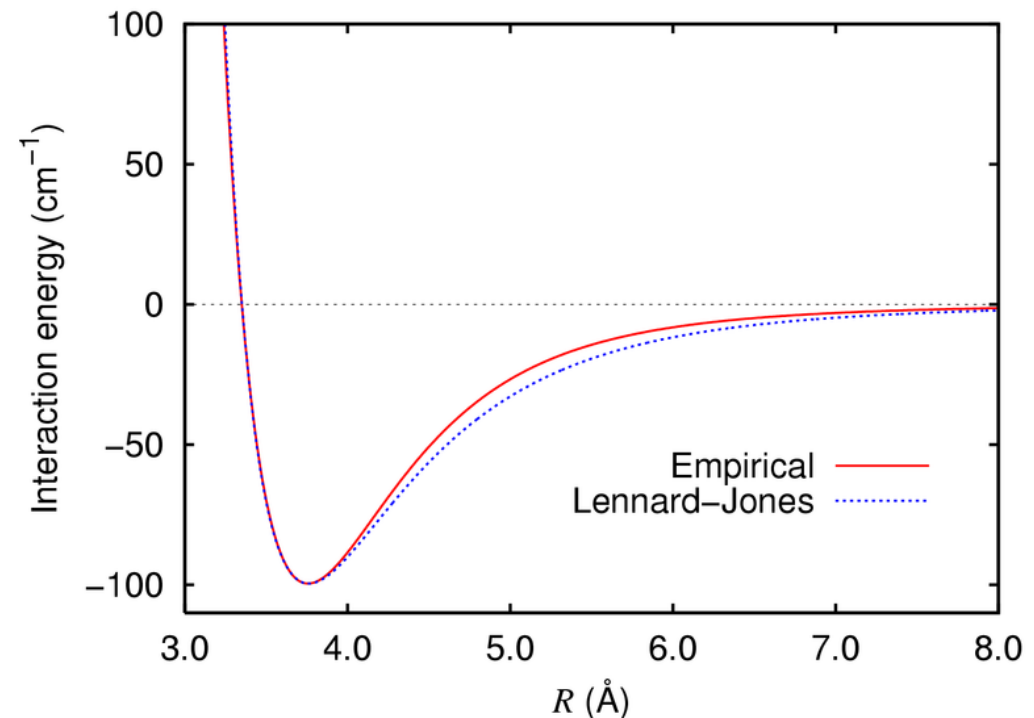
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Approximations: Morse potential
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Molecules

These were

Homonuclear diatomic molecules, eg. H_2 , Li_2 , N_2 , O_2

The molecule is diatomic so we are looking for a combination of two orbitals φ_A and φ_B .

$$\Psi = c_A \varphi_A + c_B \varphi_B \quad |c_A|^2 = |c_B|^2 \Rightarrow c_A = \pm c_B$$

$$S = \int \varphi_A \varphi_B d\vec{r} > 0 \quad \text{overlap integral}$$

$$N_+ = \frac{1}{\sqrt{2(1+S)}} \quad N_- = \frac{1}{\sqrt{2(1-S)}}$$

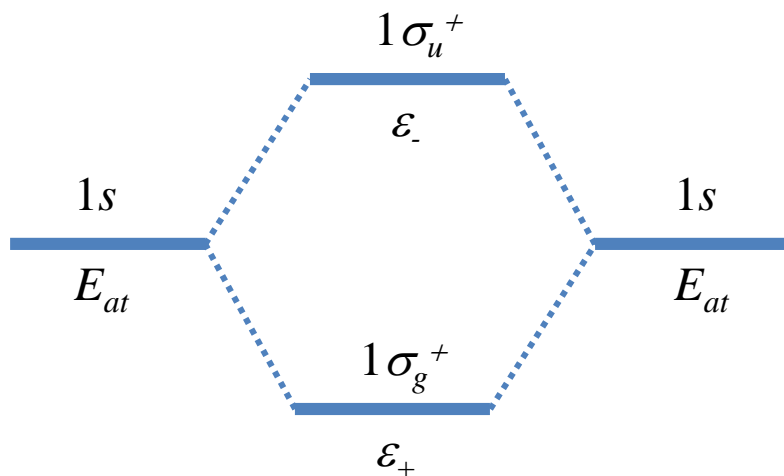
$$\varepsilon_{\pm} = \int \Psi_{\pm}^* \hat{H}^0 \Psi_{\pm} d\vec{r}$$

$$\varepsilon_+ = \frac{E_{at} - |H_{AB}|}{1 + S}$$

bonding orbital

$$\varepsilon_- = \frac{E_{at} + |H_{AB}|}{1 - S}$$

antibonding orbital



$$H_{AA} = \int \varphi_A^* \hat{H}^0 \varphi_A d\vec{r} = H_{BB} \approx E_{at}$$

$$H_{AB} = \int \varphi_A^* \hat{H}^0 \varphi_B d\vec{r} < 0$$

Molecules

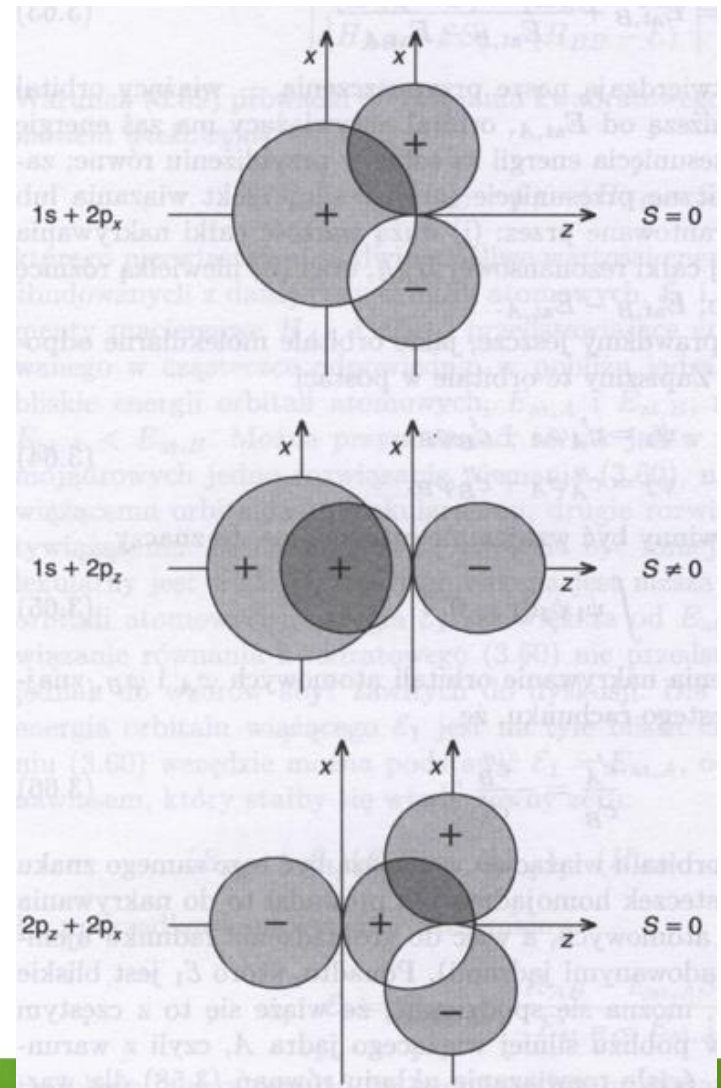
Heteronuclear diatomic molecules, eg. **CO, NO, HCl, HF**

$$\Psi = c_A\varphi_A + c_B\varphi_B \quad |c_A|^2 = |c_B|^2 \Rightarrow c_A = \pm c_B$$

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$E_{at,B}$

$E_{at,A}$



Molecules

Heteronuclear diatomic molecules, eg. **CO, NO, HCl, HF**

The molecule is diatomic so we are looking for a combination of two orbitals φ_A and φ_B .

$$\Psi = c_A\varphi_A + c_B\varphi_B \quad |c_A|^2 \neq |c_B|^2$$

$$S = \int \varphi_A\varphi_B d\vec{r} > 0$$

$$\text{variational method } \varepsilon < \frac{\int \Psi_{\pm}^* \hat{H}^0 \Psi_{\pm} d\vec{r}}{\int \Psi_{\pm}^* \Psi_{\pm} d\vec{r}}$$

$$\varepsilon(c_A^2 + c_B^2 + 2c_Ac_BS) = c_A^2H_{AA} + c_B^2H_{BB} + 2c_Ac_BH_{AB}$$

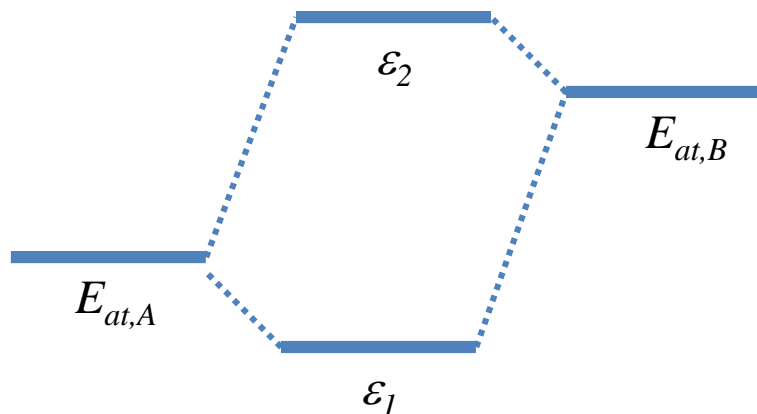
$$\frac{\partial \varepsilon}{\partial c_A} = \frac{\partial \varepsilon}{\partial c_B} = 0$$

$$\begin{bmatrix} H_{AA} - \varepsilon & H_{AB} - \varepsilon S \\ H_{AB} - \varepsilon S & H_{BB} - \varepsilon \end{bmatrix} \begin{pmatrix} c_A \\ c_B \end{pmatrix} = 0$$

$$H_{AA} \approx E_{at,A}$$

$$H_{BB} \approx E_{at,B}$$

Let's assume that $E_{at,A} < E_{at,B}$



Molecules

Heteronuclear diatomic molecules, eg. **CO, NO, HCl, HF**

The molecule is diatomic so we are looking for a combination of two orbitals φ_A and φ_B .

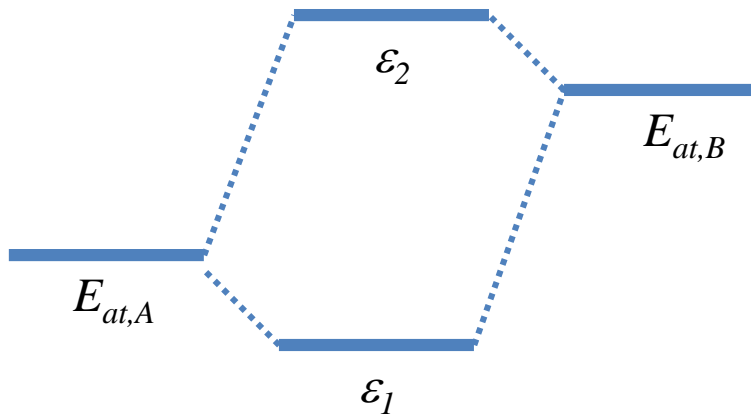
$$\Psi = c_A \varphi_A + c_B \varphi_B \quad |c_A|^2 \neq |c_B|^2$$

$$S = \int \varphi_A \varphi_B d\vec{r} > 0$$

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$$\varepsilon(c_A^2 + c_B^2 + 2c_A c_B S) = c_A^2 H_{AA} + c_B^2 H_{BB} + 2c_A c_B H_{AB}$$

$$\frac{\partial \varepsilon}{\partial c_A} = \frac{\partial \varepsilon}{\partial c_B} = 0$$



$$\begin{bmatrix} H_{AA} - \varepsilon & H_{AB} - \varepsilon S \\ H_{AB} - \varepsilon S & H_{BB} - \varepsilon \end{bmatrix} \begin{pmatrix} c_A \\ c_B \end{pmatrix} = 0$$

$$\varepsilon_1 \approx E_{at,A} - \frac{(H_{AB} - E_{at,A} S)^2}{E_{at,B} - E_{at,A}}$$

$$\varepsilon_2 \approx E_{at,B} + \frac{(H_{AB} - E_{at,B} S)^2}{E_{at,B} - E_{at,A}}$$

Molecules

The bonding is strong when:

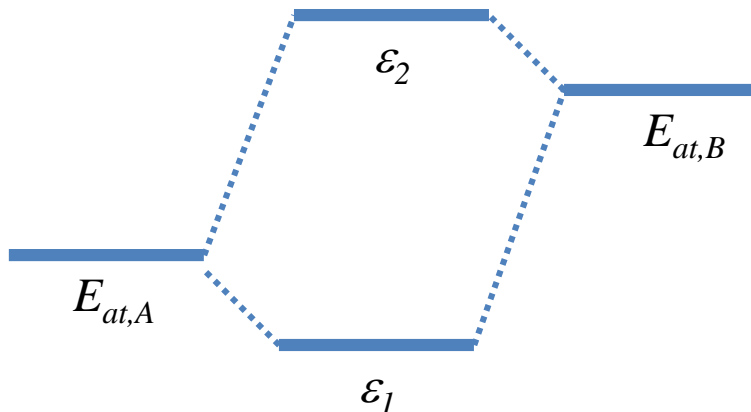
The large value of the overlap integral S and proportional to it integral H_{AB} .

The small difference of the energy of atomic orbitals $E_{at,A}$, $E_{at,B}$.

Molecular orbitals **do not have to be** constructed with atomic orbitals of the same type ($s - s$ or $p - p$).

$$\varepsilon(c_A^2 + c_B^2 + 2c_Ac_BS) = c_A^2H_{AA} + c_B^2H_{BB} + 2c_Ac_BH_{AB}$$

$$\frac{\partial \varepsilon}{\partial c_A} = \frac{\partial \varepsilon}{\partial c_B} = 0$$



$$\begin{bmatrix} H_{AA} - \varepsilon & H_{AB} - \varepsilon S \\ H_{AB} - \varepsilon S & H_{BB} - \varepsilon \end{bmatrix} \begin{pmatrix} c_A \\ c_B \end{pmatrix} = 0$$

$$\varepsilon_1 \approx E_{at,A} - \frac{(H_{AB} - E_{at,A}S)^2}{E_{at,B} - E_{at,A}}$$

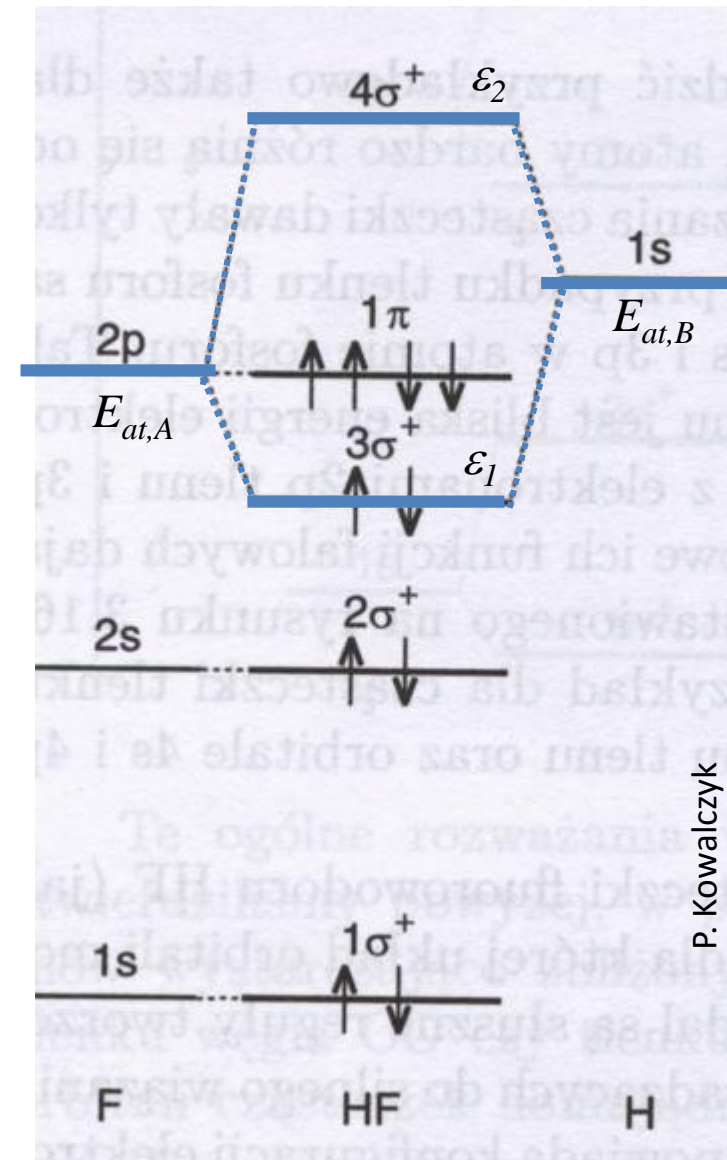
$$\varepsilon_2 \approx E_{at,B} + \frac{(H_{AB} - E_{at,B}S)^2}{E_{at,B} - E_{at,A}}$$

Molecules

Example: HF molecule

F: $(1s)^2(2s)^2(2p)^5$ H: $(1s)^1$

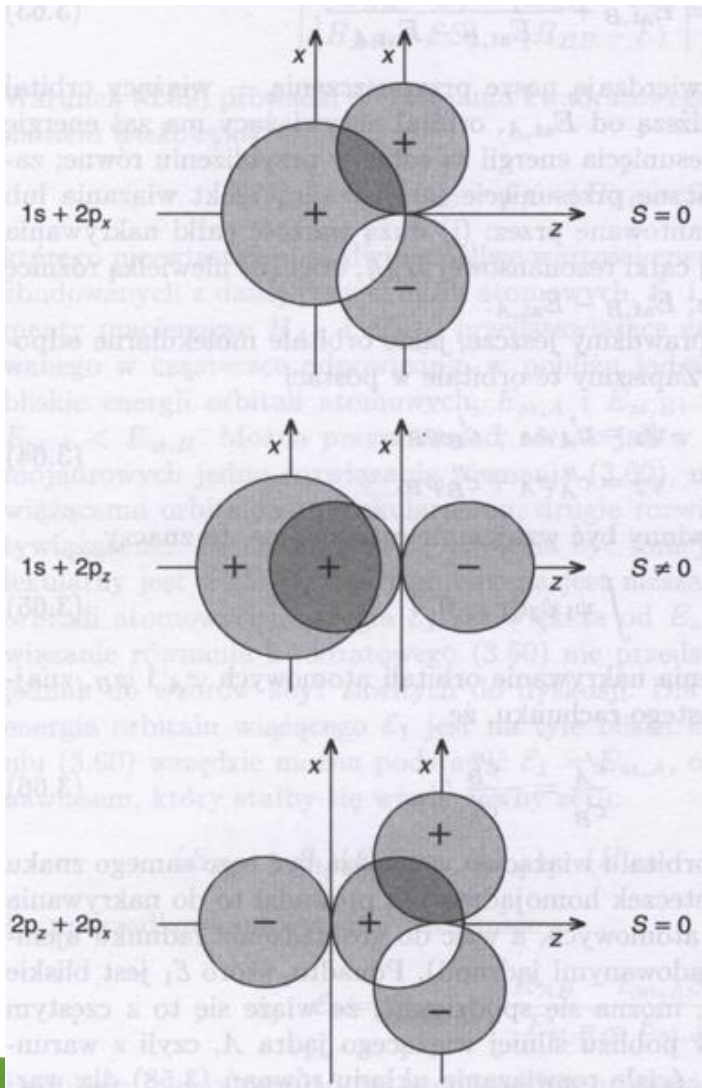
1. Similar energy values have $2p$ of F and $1s$ of H.
2. Only $2p_z$ orbital gives non-zero overlap integral with $1s$ (bonding orbital σ).
3. 2 Fluorine electrons $2p_x$ i 2 electrons $2p_y$ are not involved in the HF molecular bonding and are called **lone pair** (*wolna para elektronowa*)
4. Similarly fluorine $1s$ and $2s$ atomic orbitals do not form a bond with the $1s$ hydrogen electron because of the large energy difference
5. Ground state: $^1\Sigma^+$



P. Kowalczyk

Molecules

Hybridization and overlap integrals



P. Kowalczyk

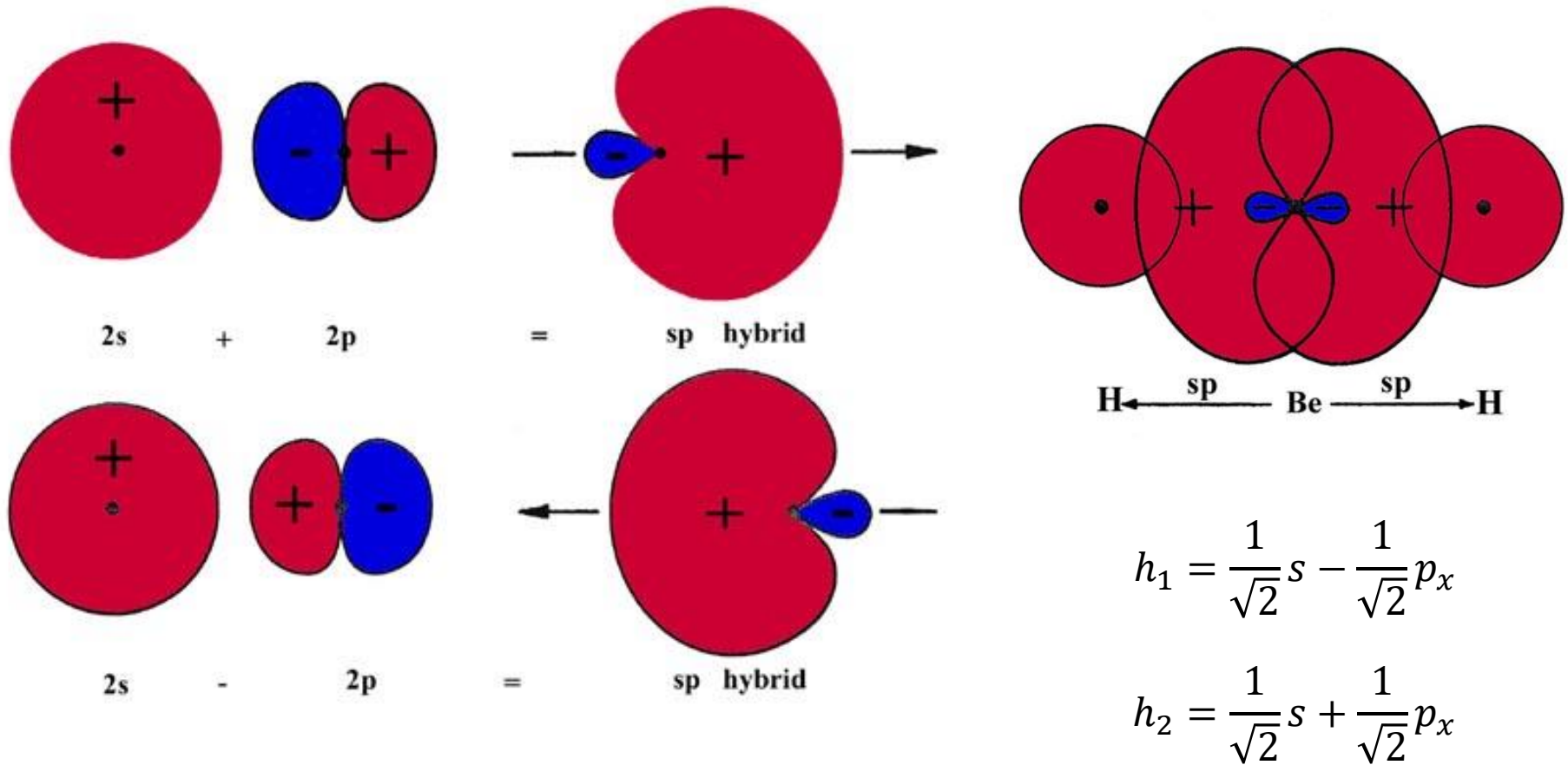
<http://sparkcharts.sparknotes.com/chemistry/organicchemistry1/section2.php>

Atomic orbitals combined	Hybrid orbitals formed	Bonding electron pairs and lone pairs around central atom	VSEPR geometry
1 s orbital & 1 p orbital	sp hybrid (2 orbitals) 	2	linear
1 s orbital & 2 p orbitals	sp ² hybrid (3 orbitals) 	3	trigonal planar
1 s orbital & 3 p orbitals	sp ³ hybrid (4 orbitals) 	4	tetrahedral
1 s orbital & 3 p orbitals & 1 d orbital	dsp ³ hybrid (5 orbitals) 	5	trigonal bipyramidal
1 s orbital & 3 p orbitals & 2 d orbitals	d ² sp ³ hybrid (6 orbitals) 	6	octahedral

Molecules

Hybridization sp, eg. BeH₂

The angle between the bonds is 180°.



Molecules

Hybridization sp^2 , eg. C_2H_4

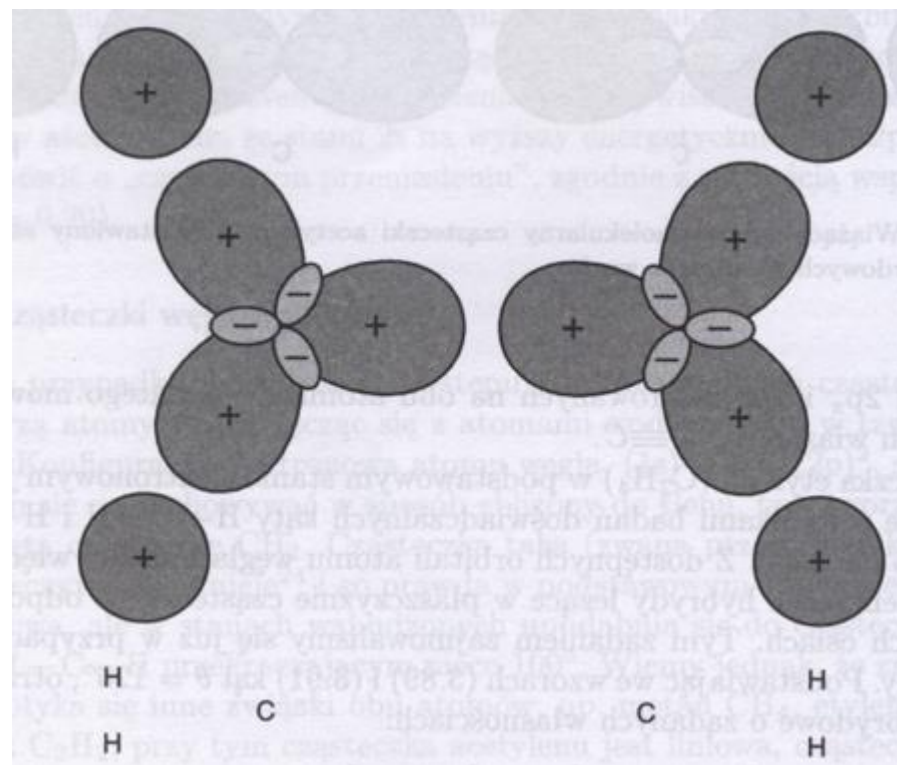
The angle between the bonds is 120° .

$$h_1 = \frac{1}{\sqrt{3}}s - \frac{1}{\sqrt{2}}p_x - \frac{1}{\sqrt{6}}p_z$$

$$h_2 = \frac{1}{\sqrt{3}}s + \frac{1}{\sqrt{2}}p_x - \frac{1}{\sqrt{6}}p_z$$

$$h_3 = \frac{1}{\sqrt{3}}s + \frac{1}{\sqrt{2}}p_z$$

Ethylene C_2H_4



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Molecules

Hybridization sp^3 , eg. CH_4

The angle between the bonds is $109,5^\circ$.

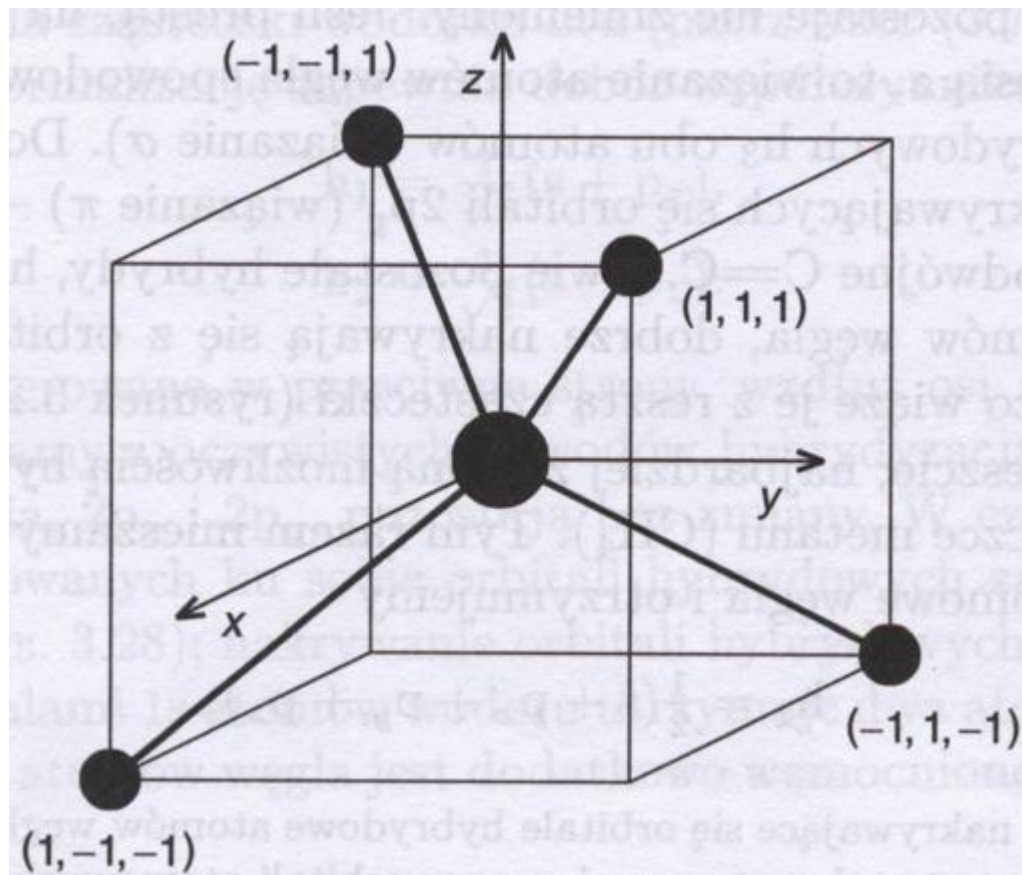
$$h_1 = \frac{1}{2}(s + p_x + p_y + p_z)$$

$$h_2 = \frac{1}{2}(s + p_x - p_y - p_z)$$

$$h_3 = \frac{1}{2}(s - p_x + p_y - p_z)$$

$$h_4 = \frac{1}{2}(s - p_x - p_y + p_z)$$

Methane CH_4



Molecules

Hybridization sp^3 , eg. CH_4

The angle between the bonds is $109,5^\circ$.

$$h_1 = \frac{1}{2}(s + p_x + p_y + p_z)$$

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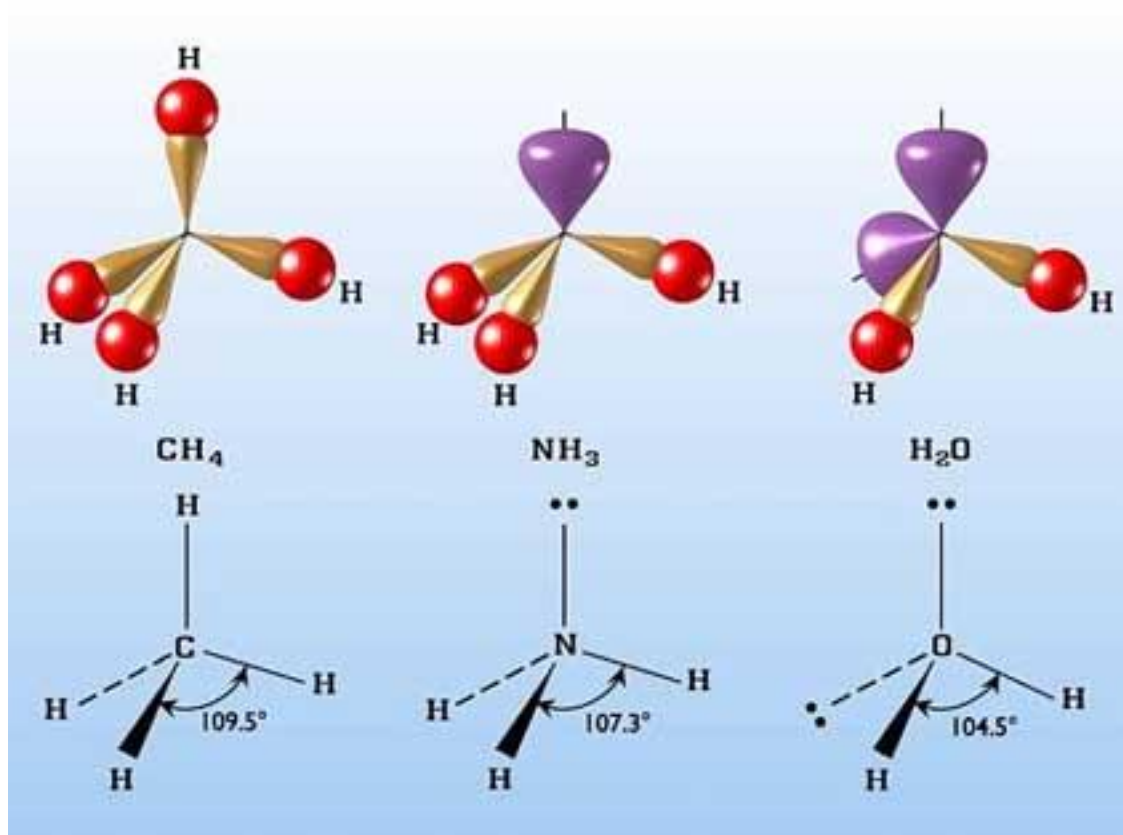
$$h_3 = \frac{1}{2}(s - p_x + p_y - p_z)$$

$$h_4 = \frac{1}{2}(s - p_x - p_y + p_z)$$

Methane CH_4

Ammonia NH_3

Water H_2O



http://oen.dydaktyka.agh.edu.pl/dydaktyka/chemia/a_e_chemia/1_3_budowa_materii/01_04_03_2b.htm

Molecules

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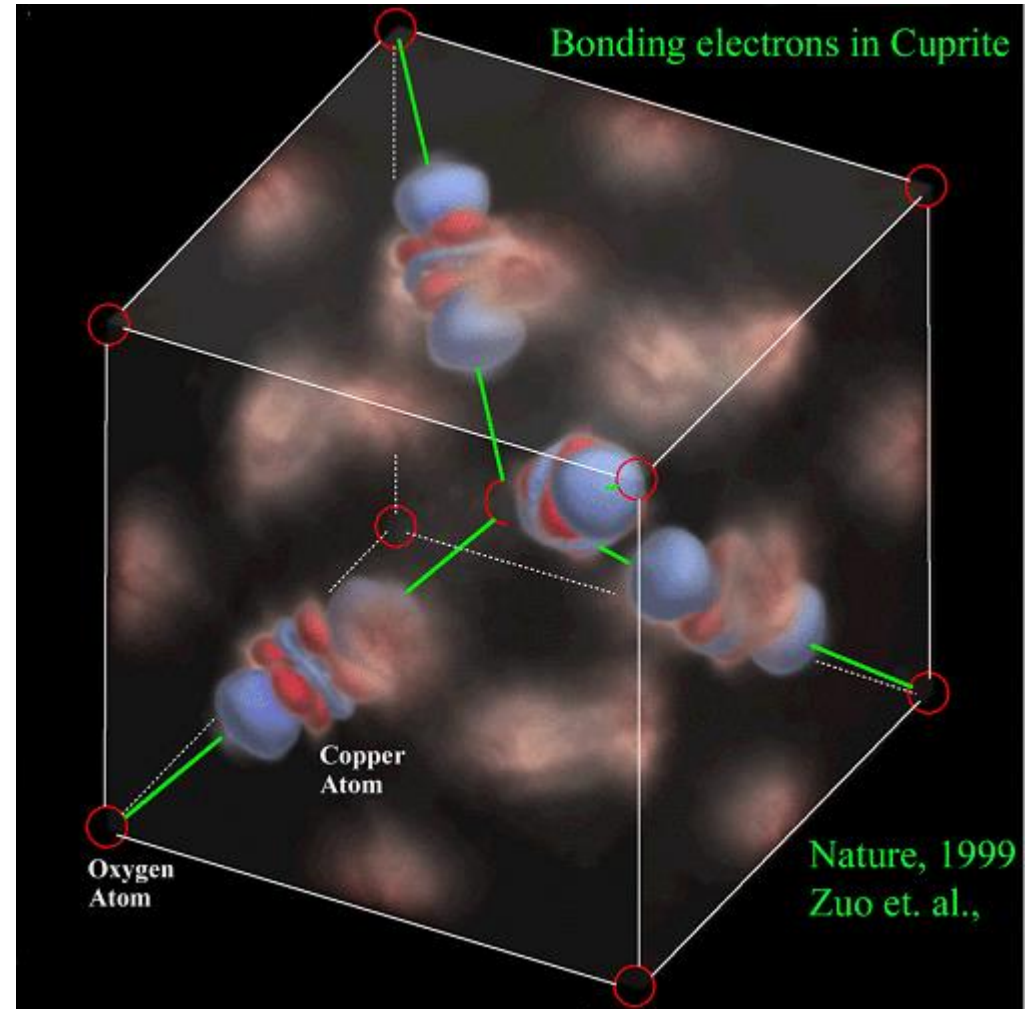
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$$h_4 = \frac{1}{2}(s - p_x - p_y + p_z)$$



Molecules

Hybridization

A summary of hybrid orbitals, valence bond theory, VSEPR, resonance structures, and octet rule.

Linear	Trigonal planar	Tetrahedral	Trigonal bipyramidal	Octahedral
sp	sp^2	sp^3	dsp^3	d^2sp^3
BeH_2	BH_3	CH_4	PF_5	SF_6
BeF_2	BF_3	CF_4	PCl_5	IOF_5
CO_2	CH_2O	CCl_4	$PFCl_4$	PF_6^-
HCN	$(>C=O)$	CH_3Cl	$:SF_4$	SiF_6^{2-}
$HC^{\bullet}CH$	$>C=C<$	NH_4^+	$:TeF_4$	$:BrF_5$
	CO_3^{2-}	$:NH_3$	$::ClF_3$	$:IF_5$
	benzene	$:PF_3$	$::BrF_3$	$::XeF_4$
	graphite	$:SOF_2$	$::XeF_2$	
	fullerenes	$::OH_2$	$::I_3^-$	
	$\bullet NO_2$	$::SF_2$	$(::I I_2)$	
	N_3^-		$::ICl_2^-$	
	$:OO_2 (O_3)$	SiO_4^{4-}		
	$:SO_2$	PO_4^{3-}		
	SO_3	SO_4^{2-}		
		ClO_4^-		

• a lone odd electron : a lone electron pair

<http://sparkcharts.sparknotes.com/chemistry/organicchemistry1/section2.php>

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<http://www.science.uwaterloo.ca/~cchieh/cact/c120/hybrid.html>

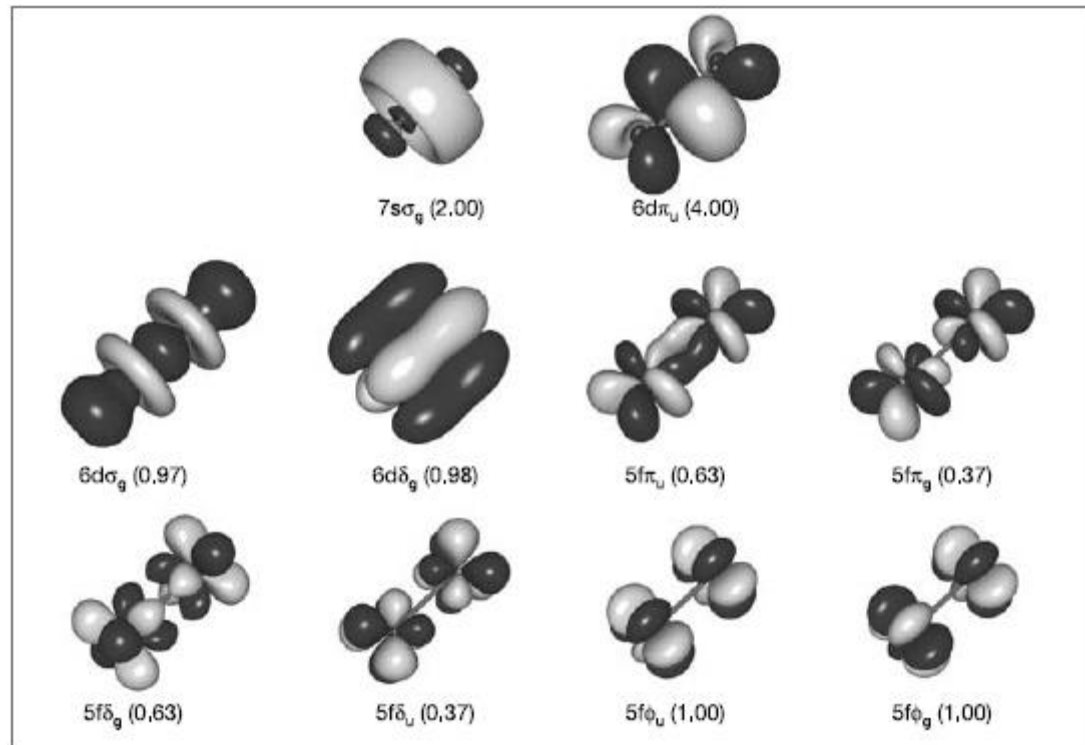
Molecules

Hybridization

Uranium, a member of the actinide group of elements, can form molecules with five covalent bonds.

Each uranium atom has a total of 16 atomic orbitals that are available for bond formation. Gagliardi and Roos used an approach called CASSCF/CASPT2 to model how all the valence orbitals in one atom merge with those in the other atom to form the most stable chemical bond -- that is, the one with minimum energy.

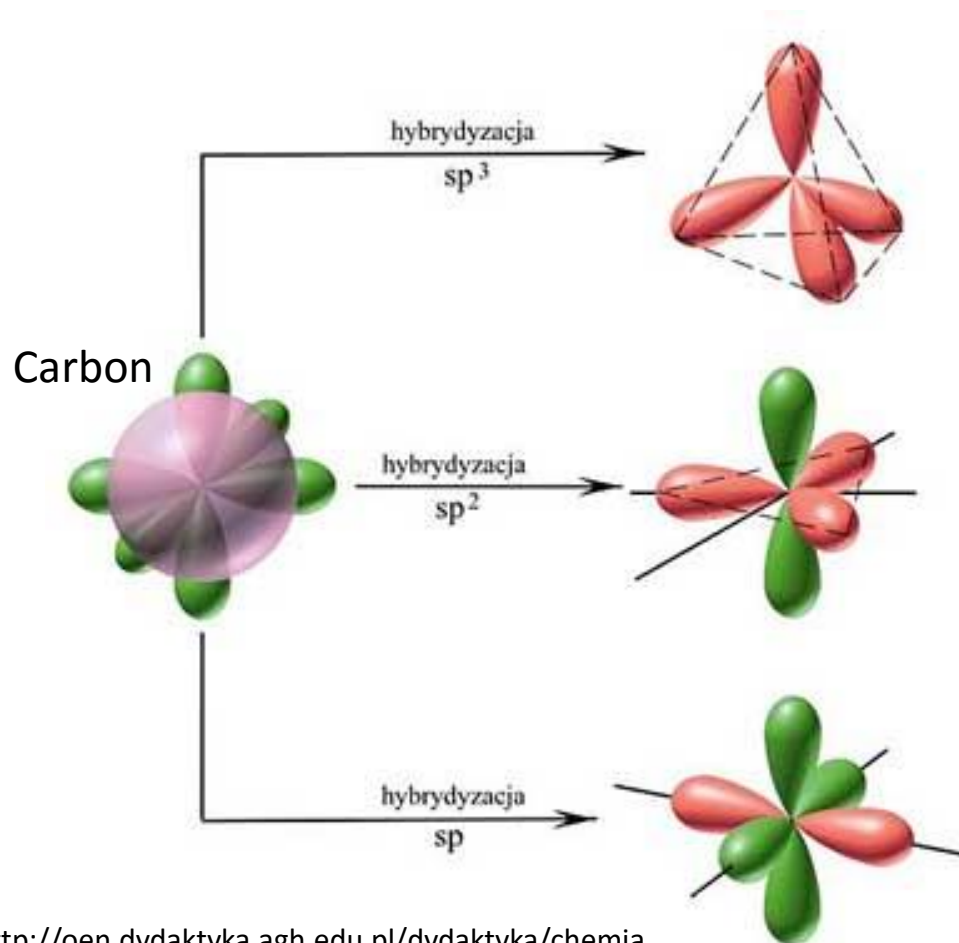
Gagliardi and Roos found that the uranium-uranium bond is more complex than any other known diatomic bond: it contains three normal electron-pair bonds and four weaker one-electron bonds. They also find evidence for ferromagnetic coupling between two electrons, each localized on one of the atoms. This means that all the known forms of covalent bonding are found in the molecule.



The active molecular orbitals forming the chemical bond between two uranium atoms. The orbital label is given below each orbital, together with the number of electrons occupying this orbital or pair of orbitals in the case of degeneracy (image courtesy: *Nature* **433** 848).

Molecules

Hybridization



<http://sparkcharts.sparknotes.com/chemistry/organicchemistry1/section2.php>

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<http://oen.dydaktyka.agh.edu.pl/dydaktyka/chemia>

Molecules

Benzene molecule

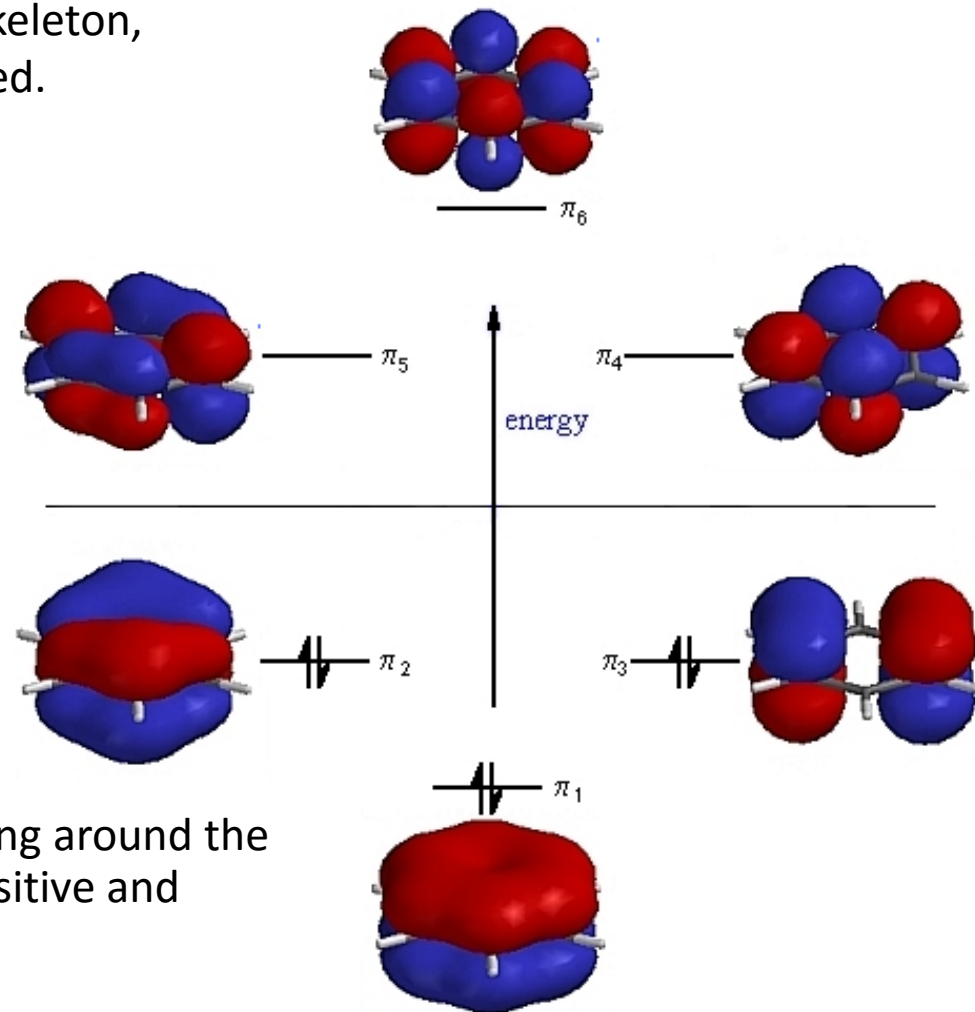
σ -bonds (sp^2) are "localized" and form a rigid skeleton, while π -electrons forming a bond are delocalized.

$$\Psi_k = \frac{1}{\sqrt{6}} \sum_{n=1}^6 e^{\frac{2\pi i}{6} kn} p_{z,n}$$
$$E_k = \alpha + 2\beta \cos\left(\frac{2\pi i}{6} k\right)$$
$$k = 0, \pm 1, \pm 2, 3$$

Six of atomic orbitals $2p_z$ gives an equal contribution to all of the molecular orbitals.

These functions correspond to the waves running around the carbon atoms ring in opposite directions for positive and negative values of k

Benzene



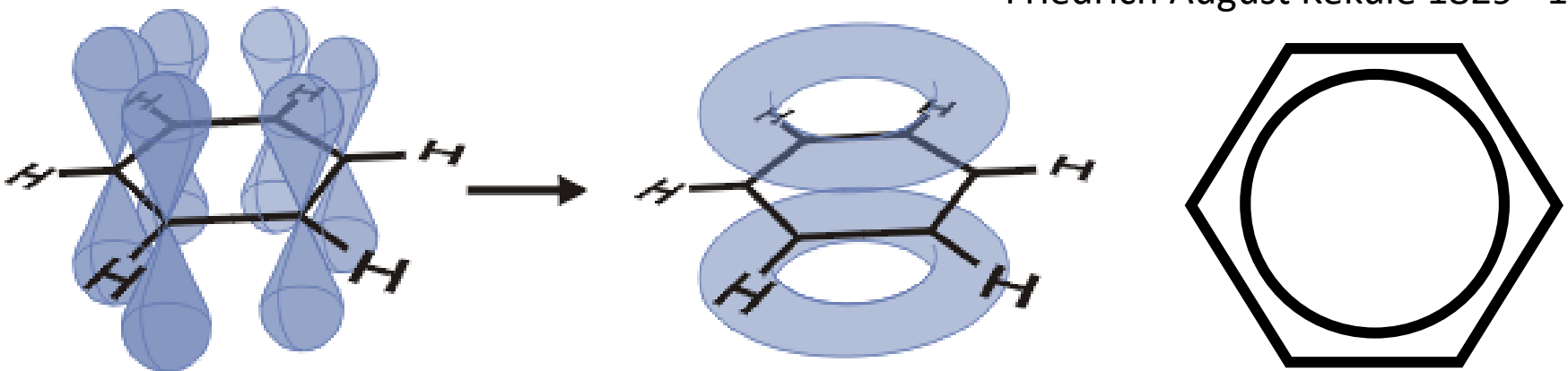
Molecules

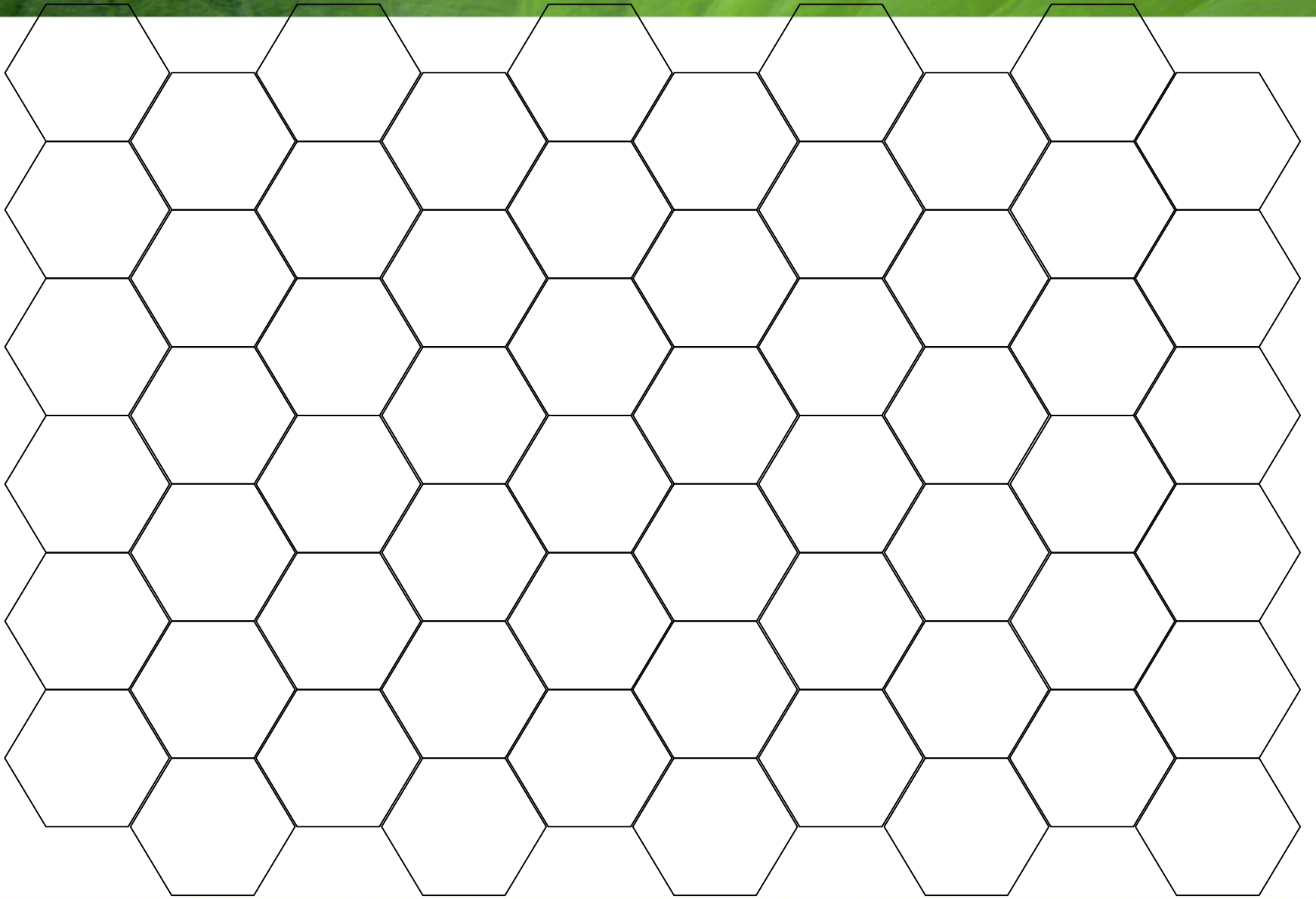
Benzene molecule

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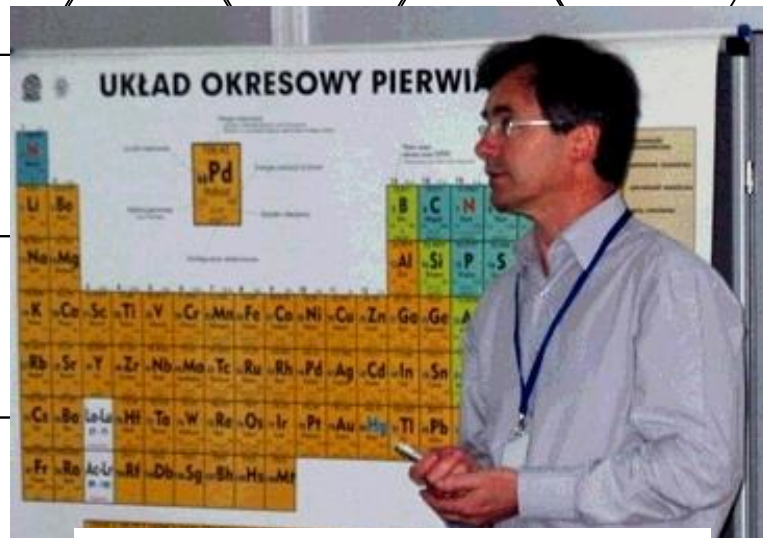
Friedrich August Kekule 1829 - 1896







The Nobel Prize in Physics 2010
Andre Geim, Konstantin Novoselov



dr inż. Włodzimierz Strupiński,



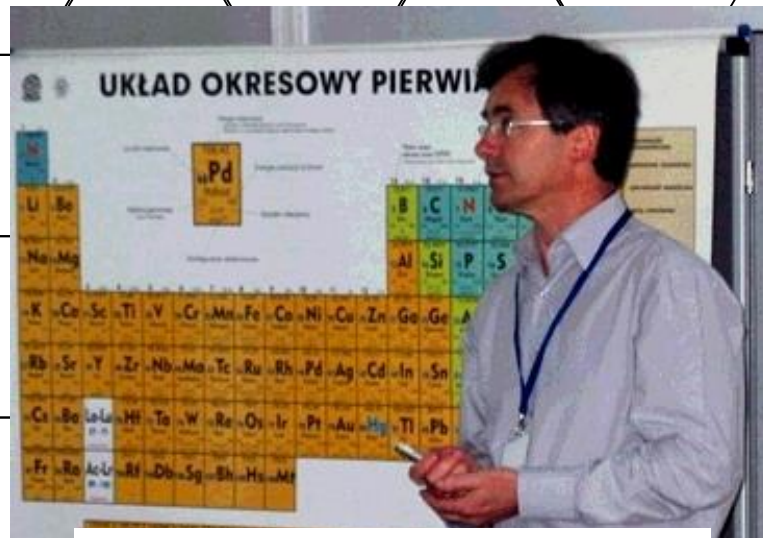
dr hab. Andrzej Wymotek





The Nobel Prize in Physics 2010

Andre Geim, Konstantin Novoselov

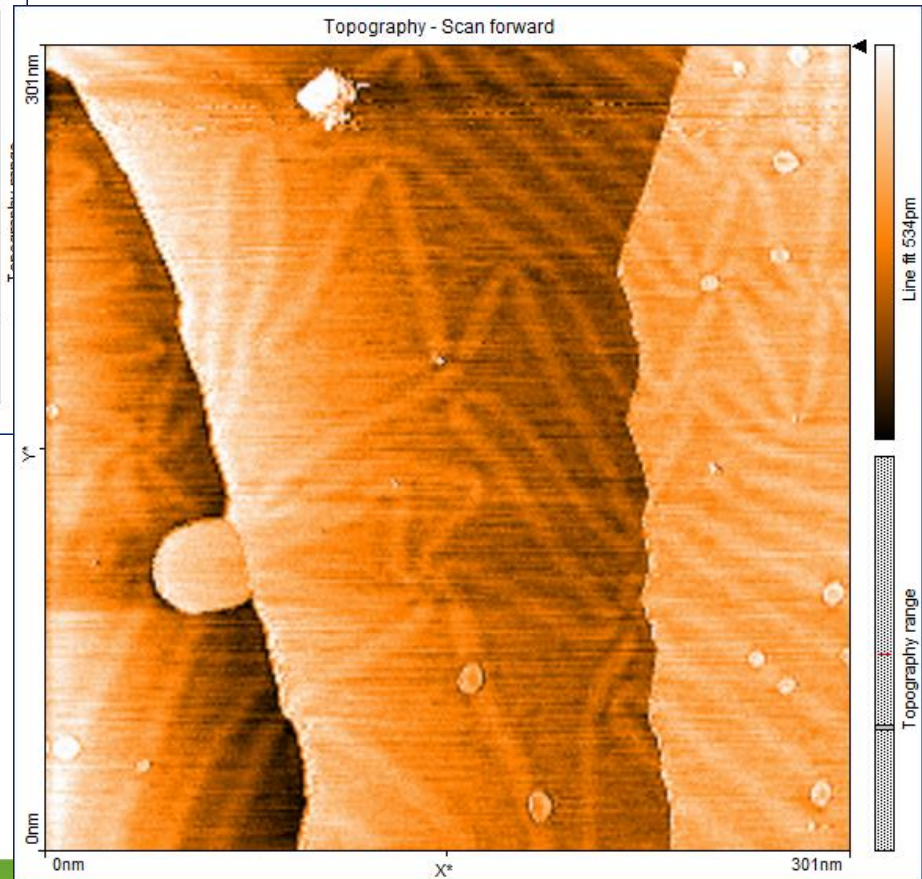
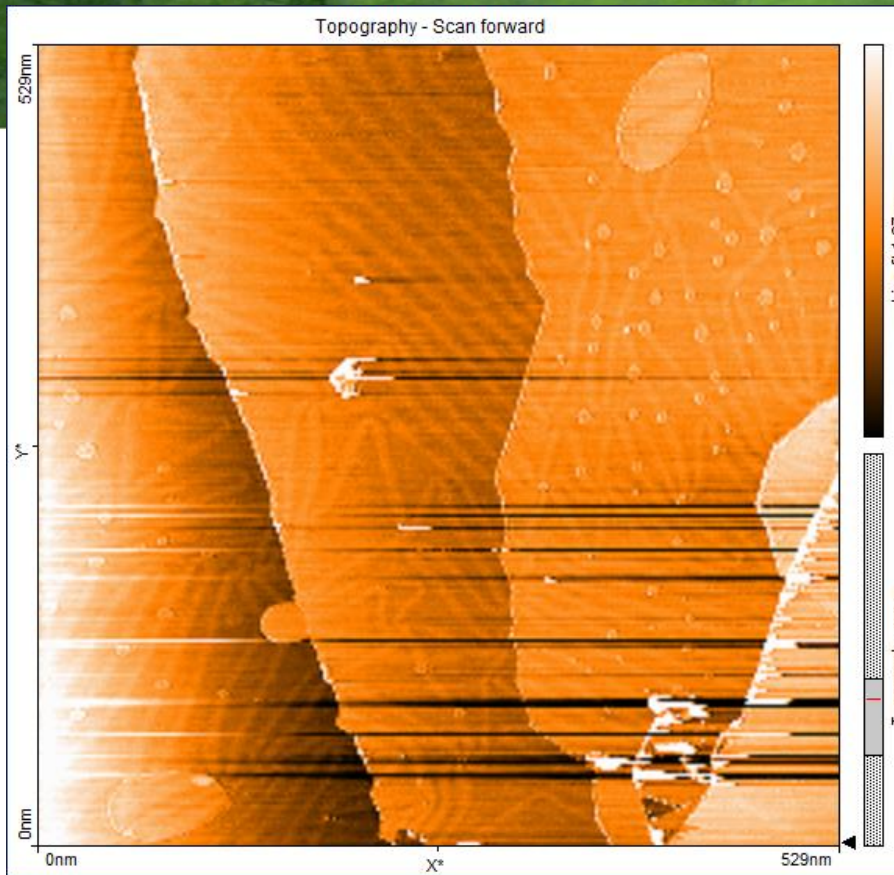


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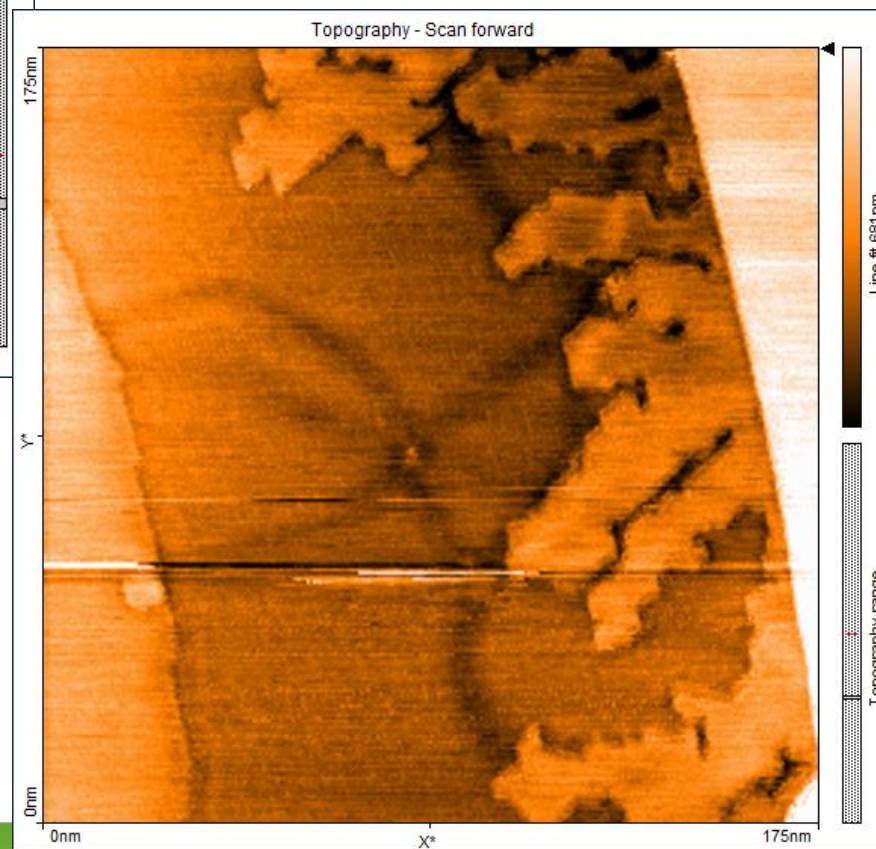
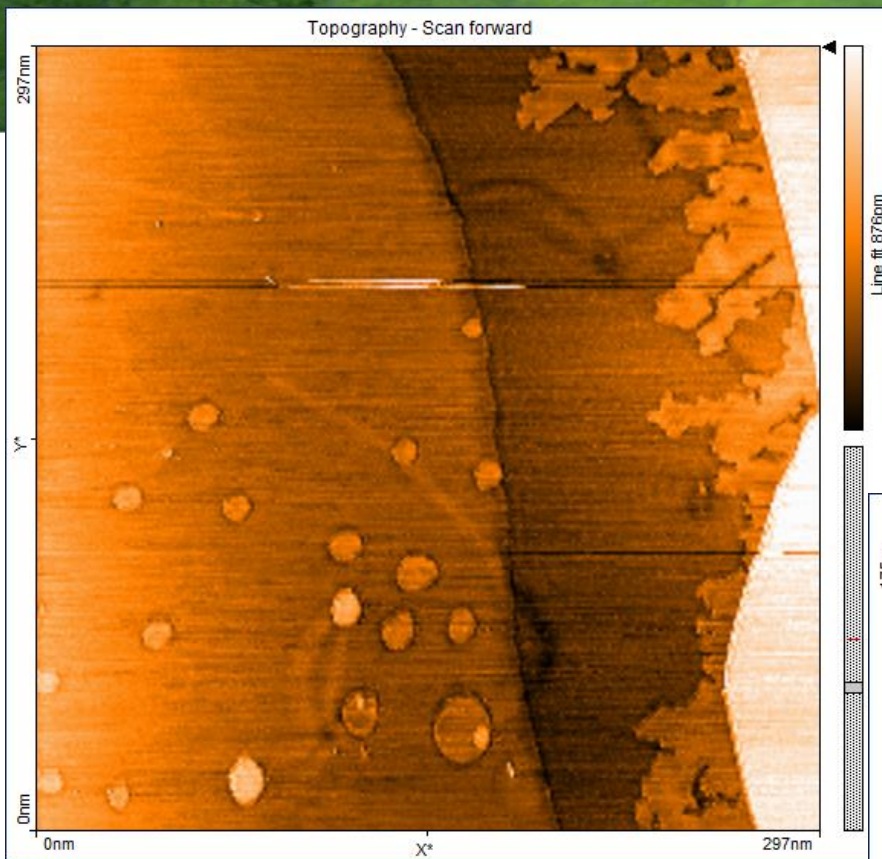
dr hab. Andrzej Wysmołek





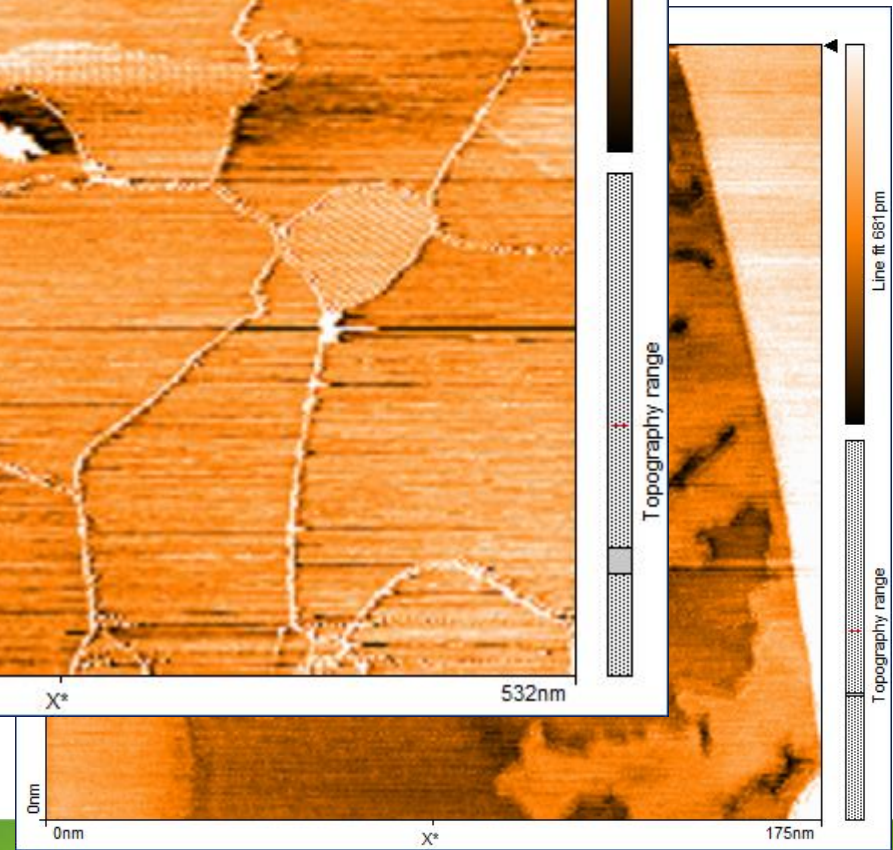
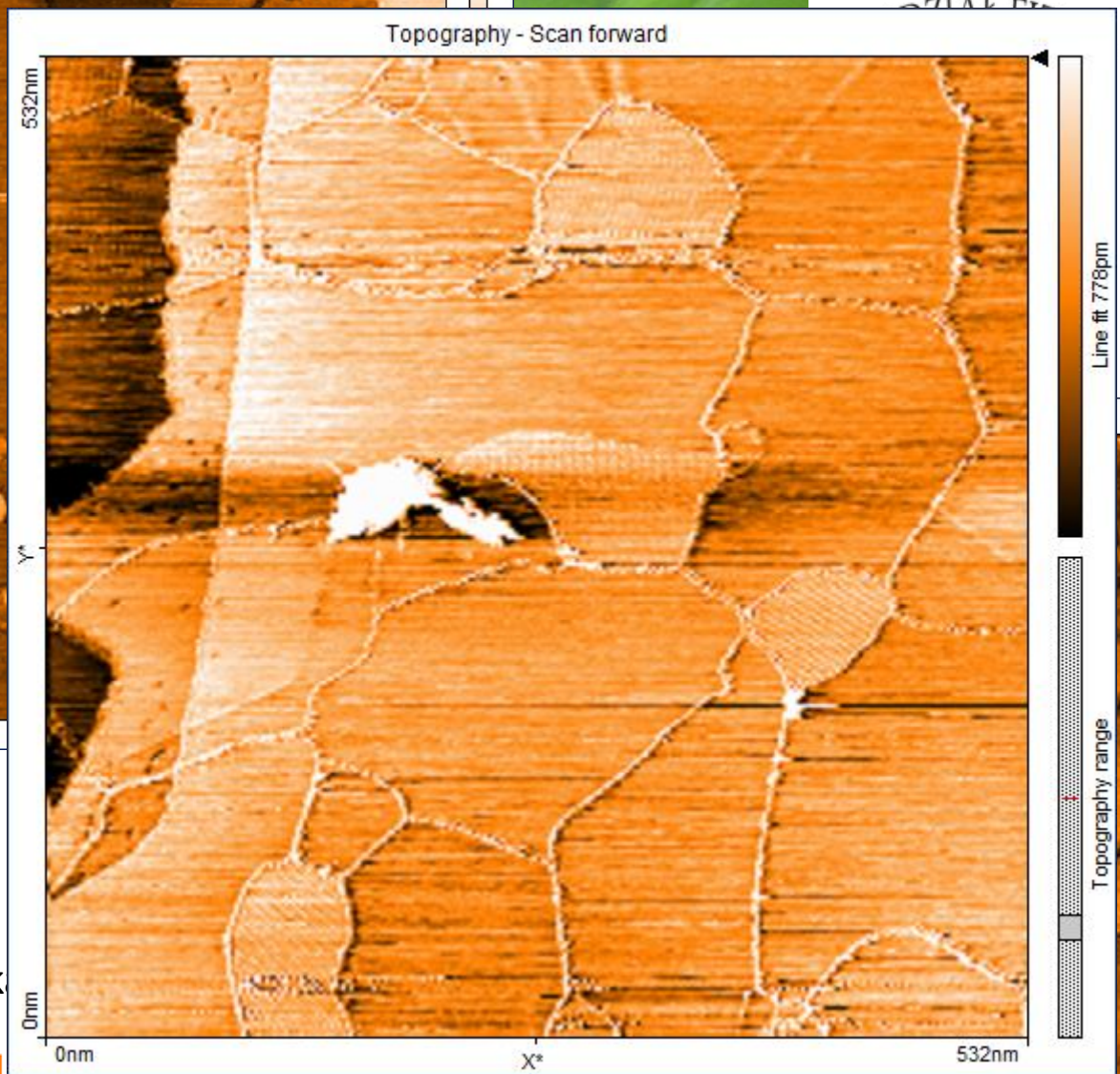
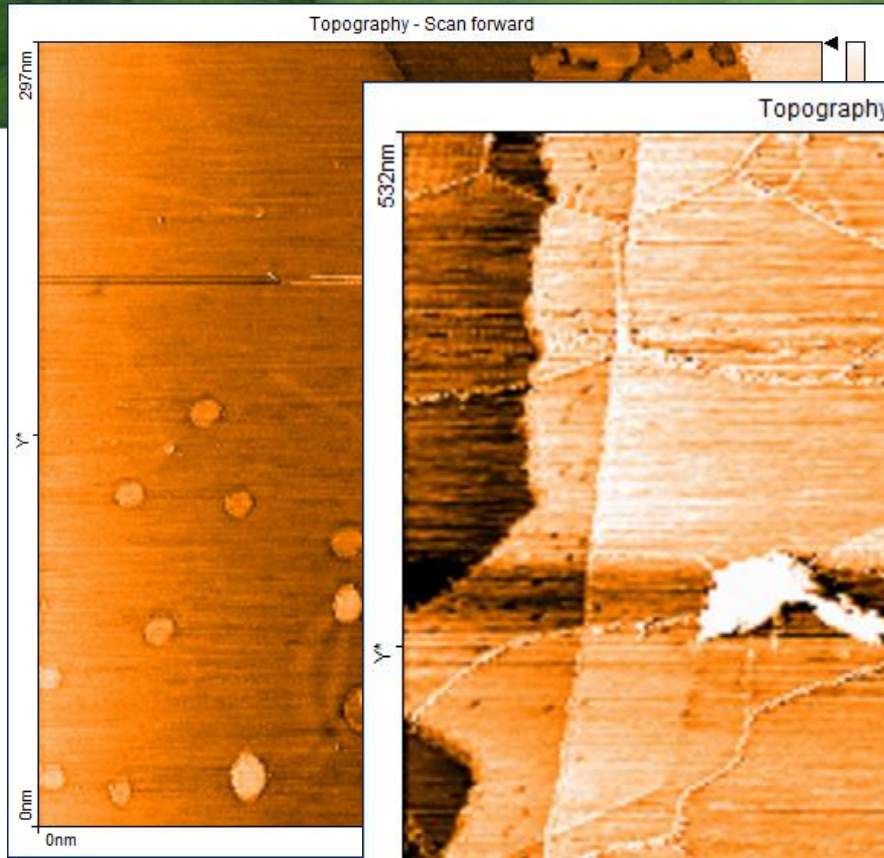
dr Jacek Szczytko
 Michał Kluz
 Izabela Rytarowska





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 Izabela Rytarowska

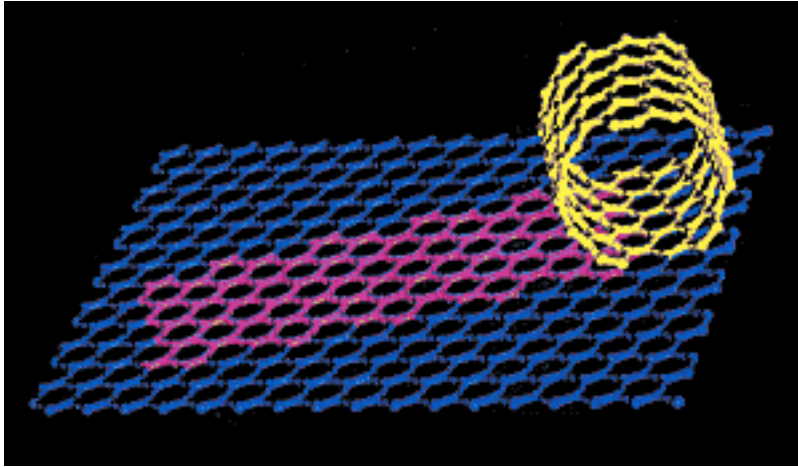




dr Jacek Szczytko
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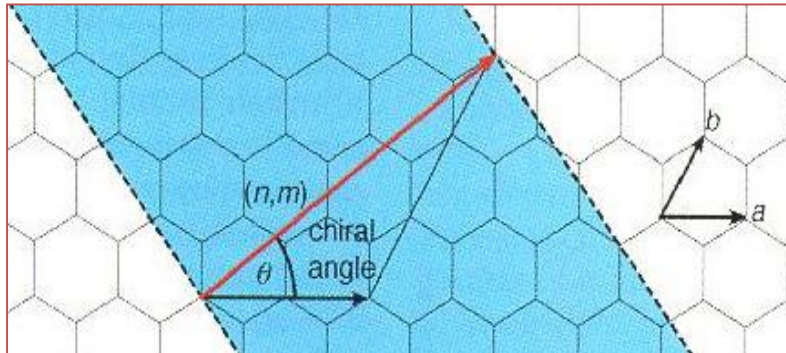


Nanotubes

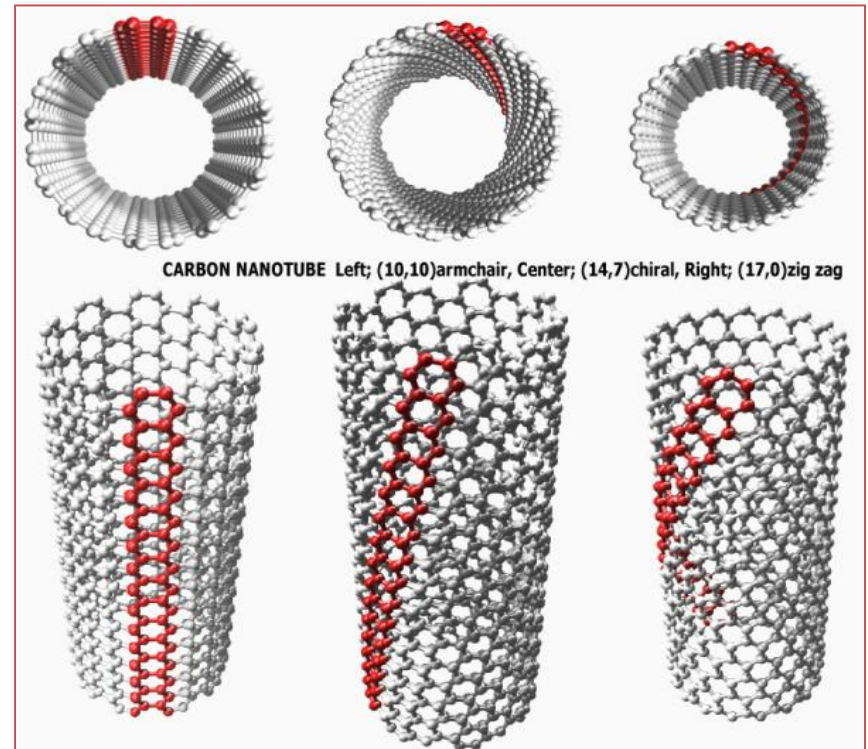


Different orientations:

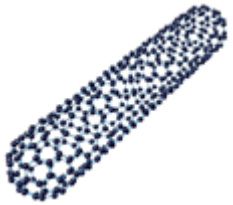
- Armchair
- Zig-zag
- Chiral



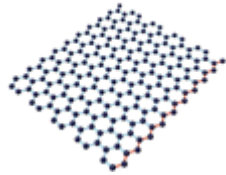
Orientation is defined by the chiral vector (n, m) : $c_h = n a + m b$



Nanotubes



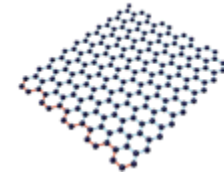
Single Wall Nanotube
(Zig-Zag Type)



Uprolling a Graphene
(Zig-Zag Type)



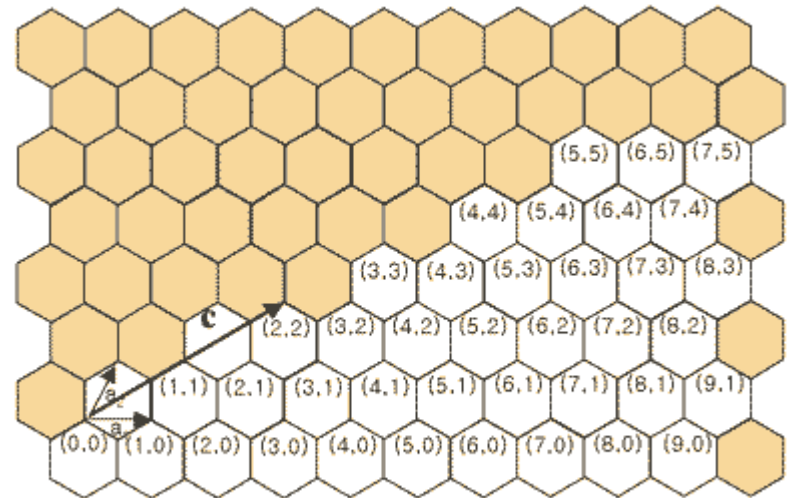
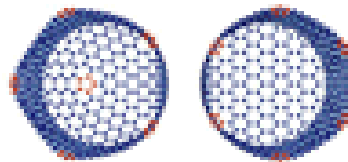
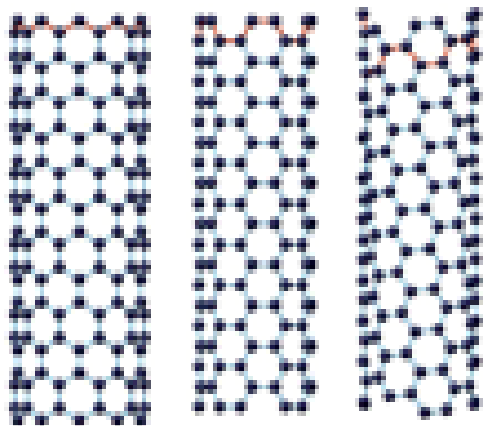
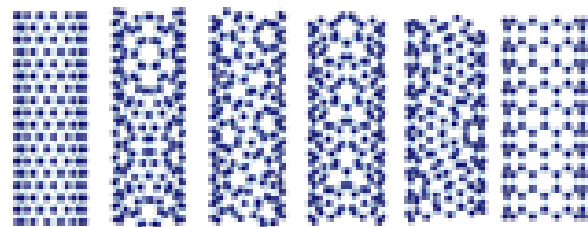
Single Wall Nanotube
(Arm-Chair Type)



Uprolling a Graphene
(Arm-Chair Type)



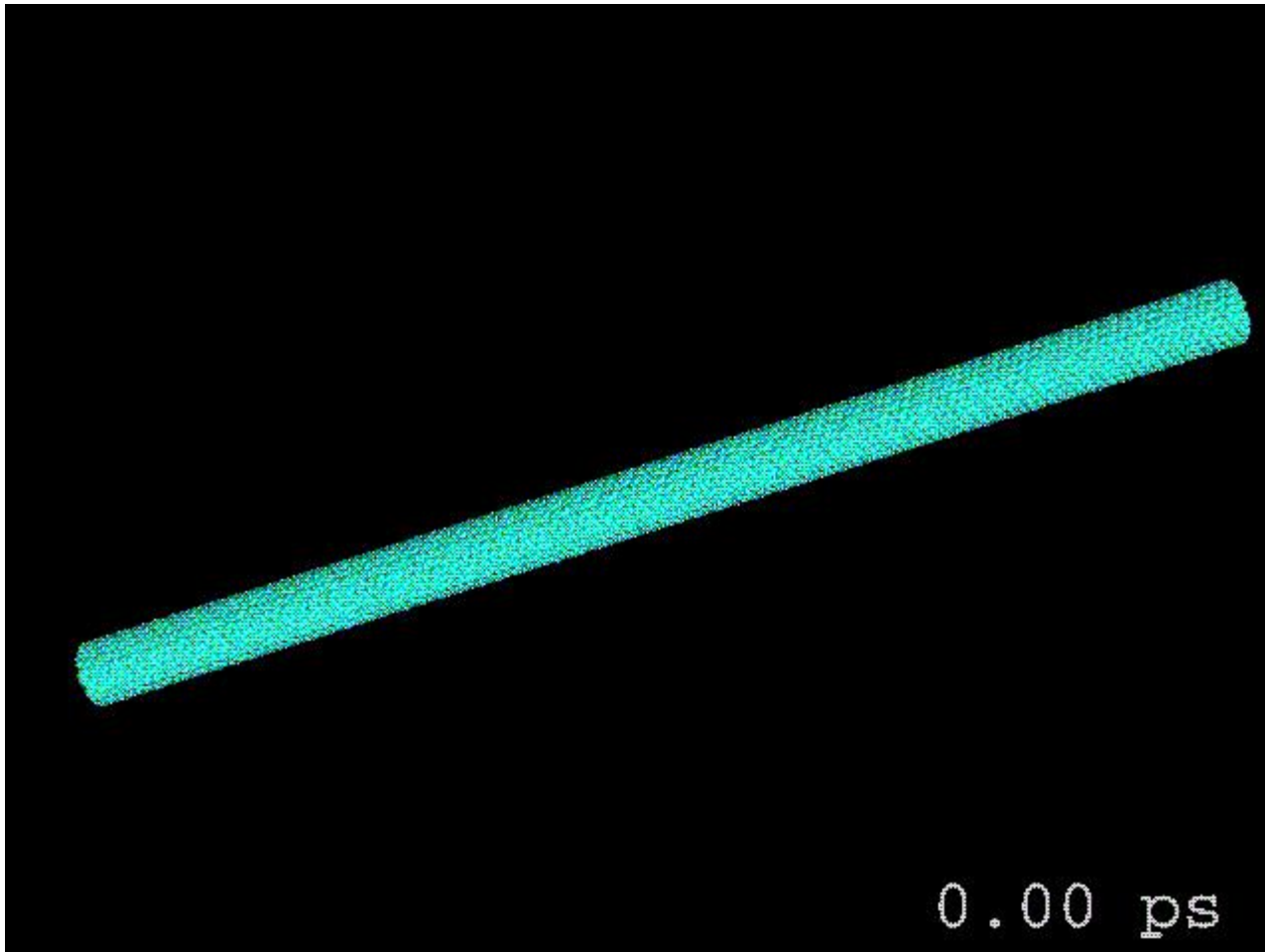
Single Wall Nanotube
(Chiral Type)



$$\phi = 0.246 (n^2 + nm + m^2)^{1/2} / \pi \text{ (nm)}$$

www.surf.nuqe.nagoya-u.ac.jp/nanotubes/omake/nanotubes/nanotubes.html

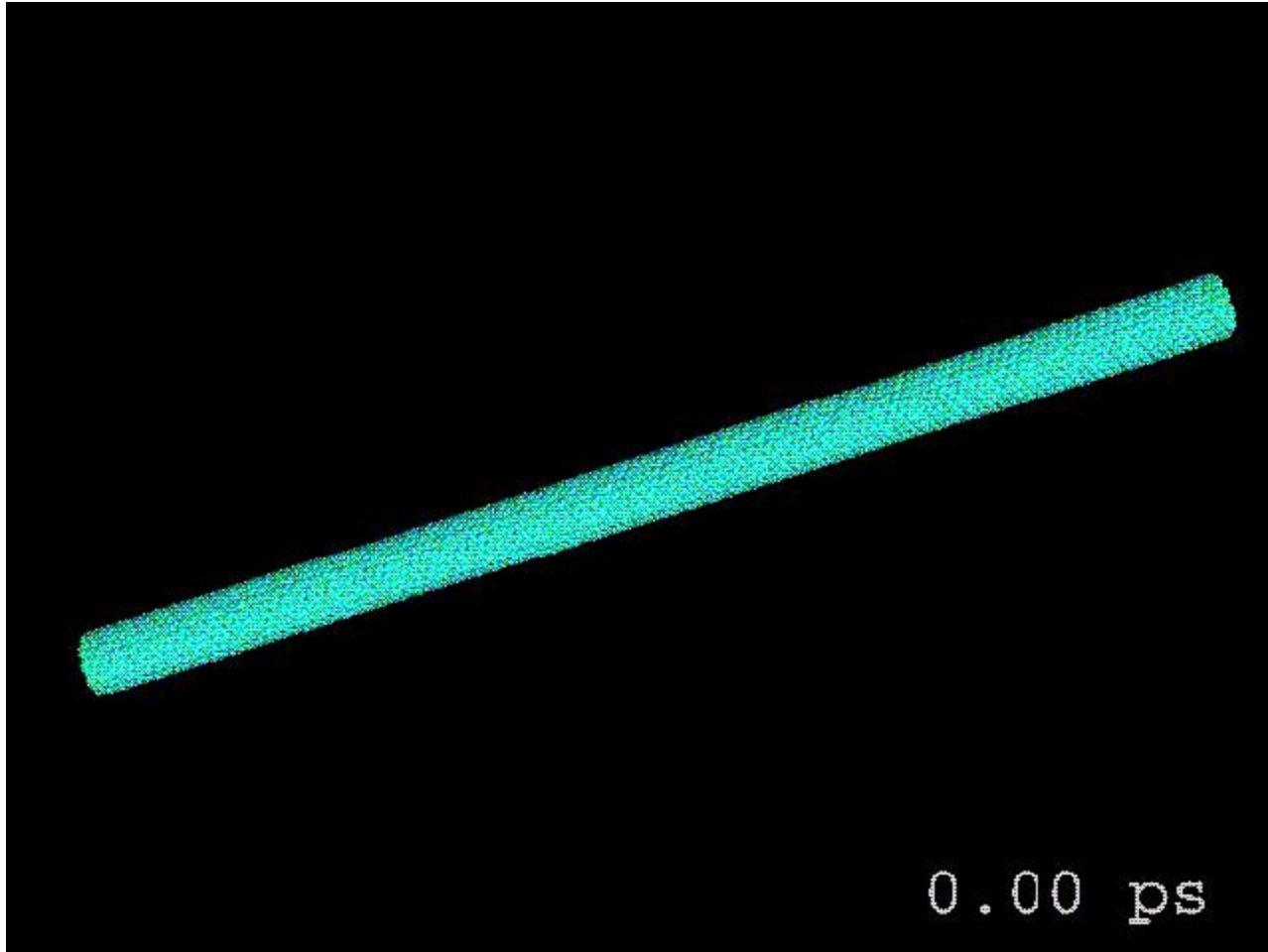
Nanomachines



Single – twist

<http://www.ipt.arc.nasa.gov>

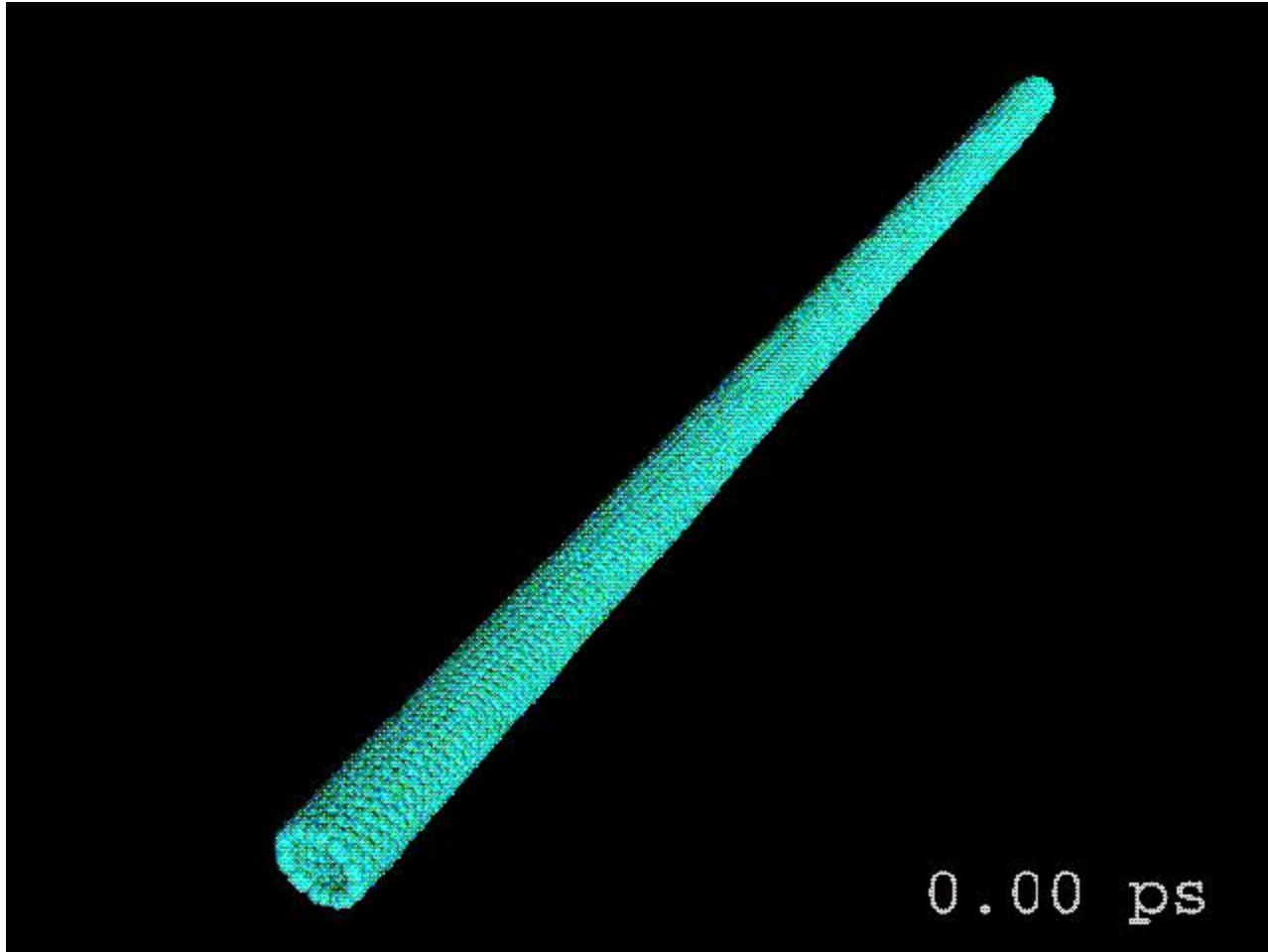
Nanomachines



Single – bend

<http://www.ipt.arc.nasa.gov>

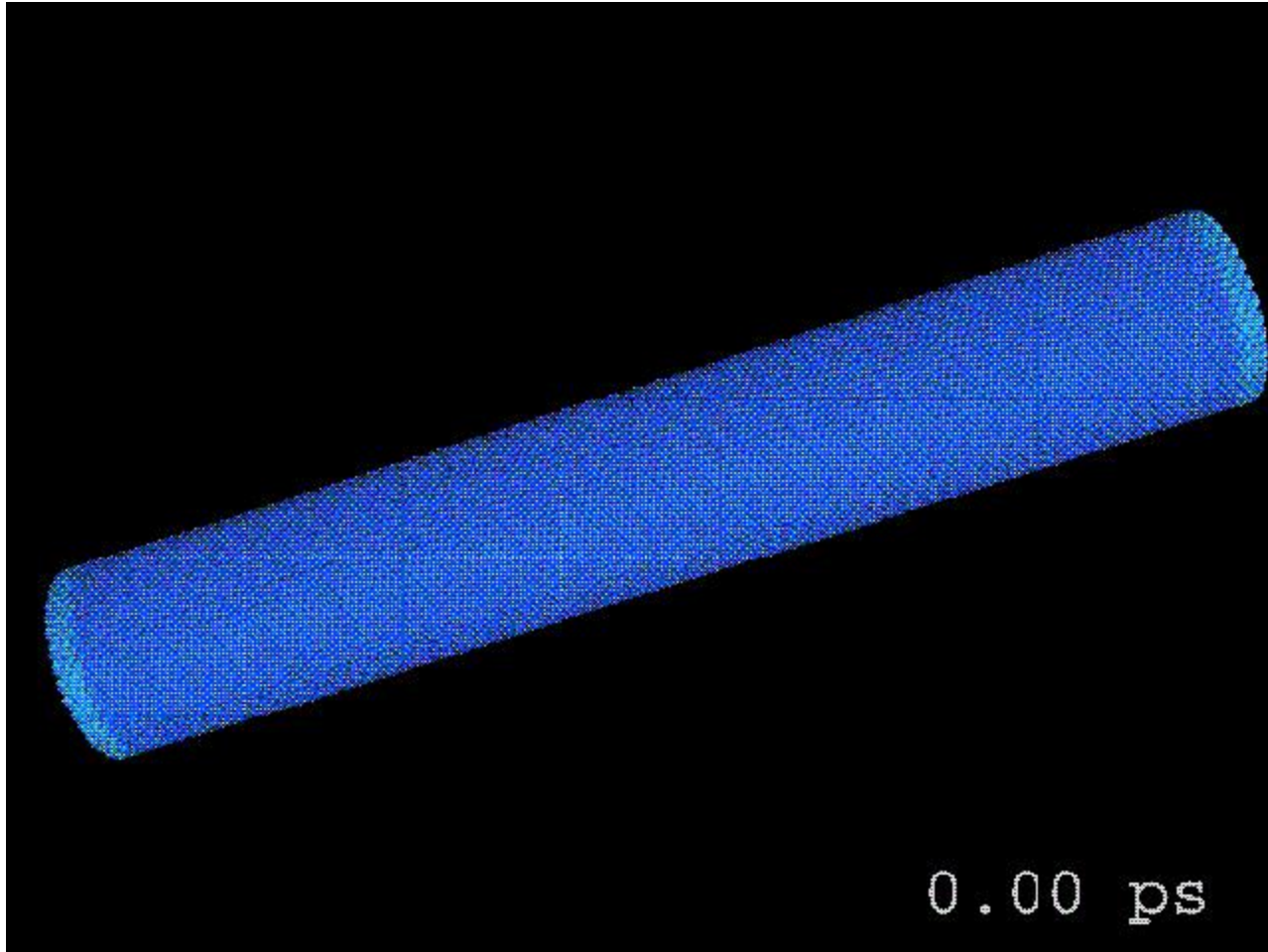
Nanomachines



Single – compress

<http://www.ipt.arc.nasa.gov>

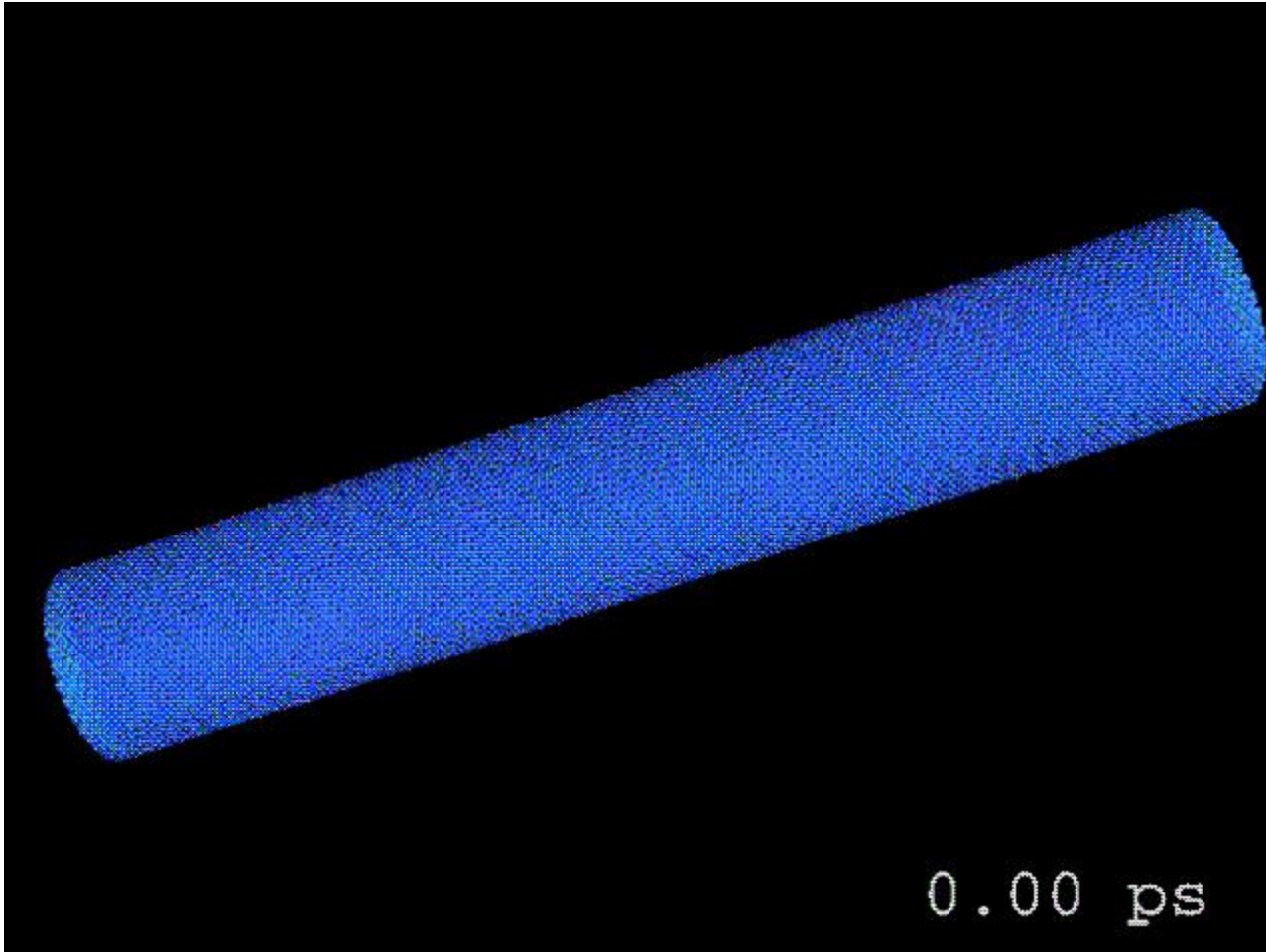
Nanomachines



Multi – twist

<http://www.ipt.arc.nasa.gov>

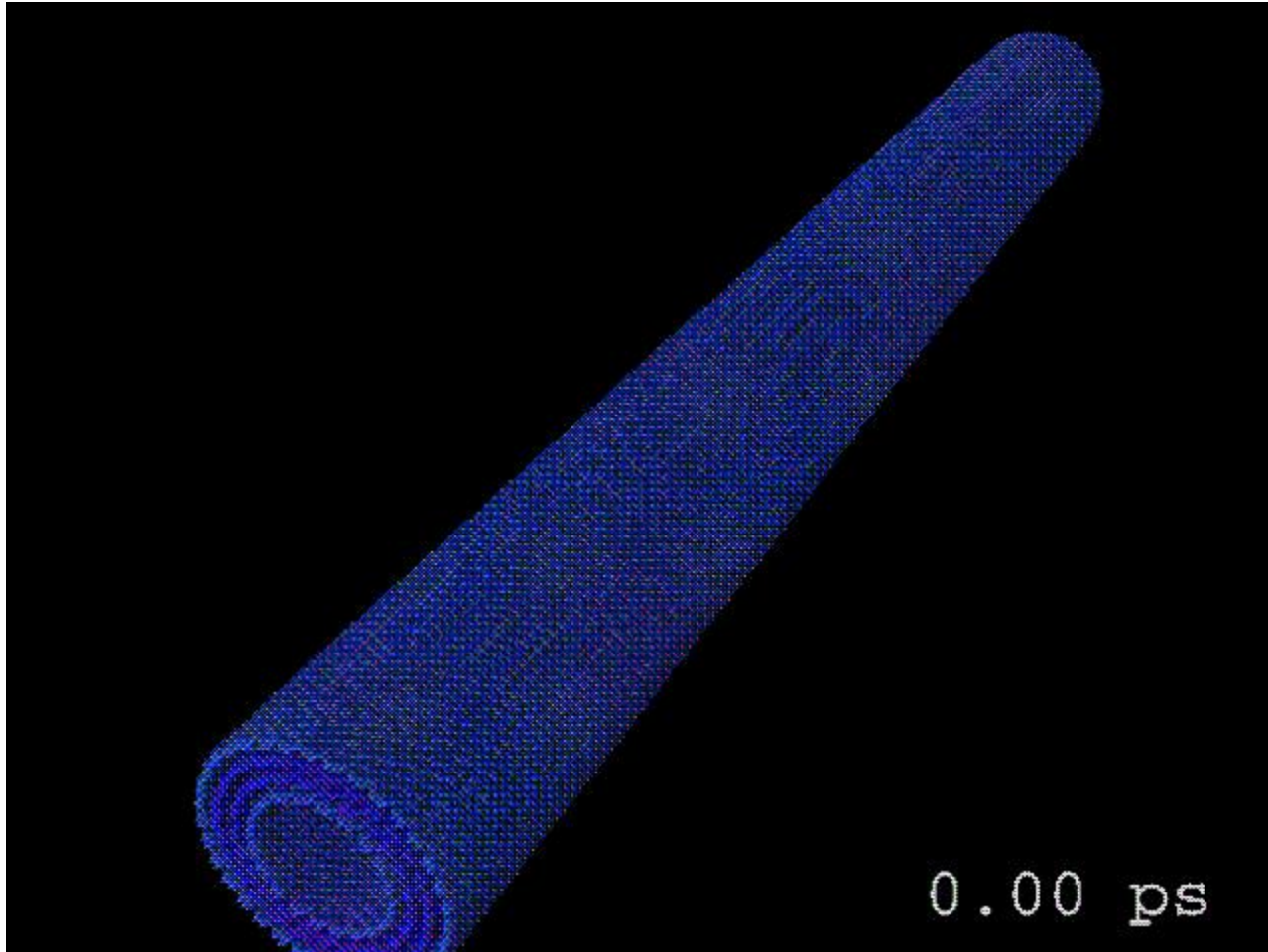
Nanomachines



Multi – bend

<http://www.ipt.arc.nasa.gov>

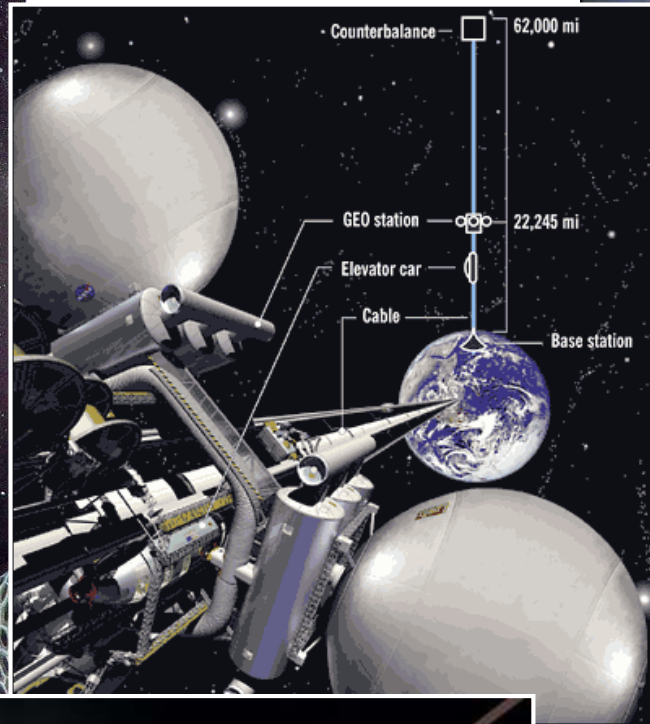
Nanomachines



Multi – compress

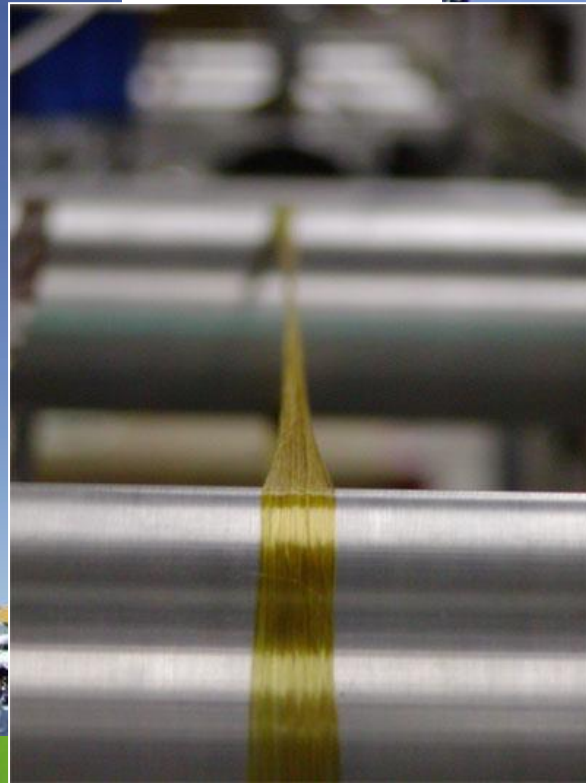
<http://www.ipt.arc.nasa.gov>

Space elevator



Space elevator

<http://www.spaceelevator.com/>



Space elevator

LETTERS

Ultralong single-wall carbon nanotubes

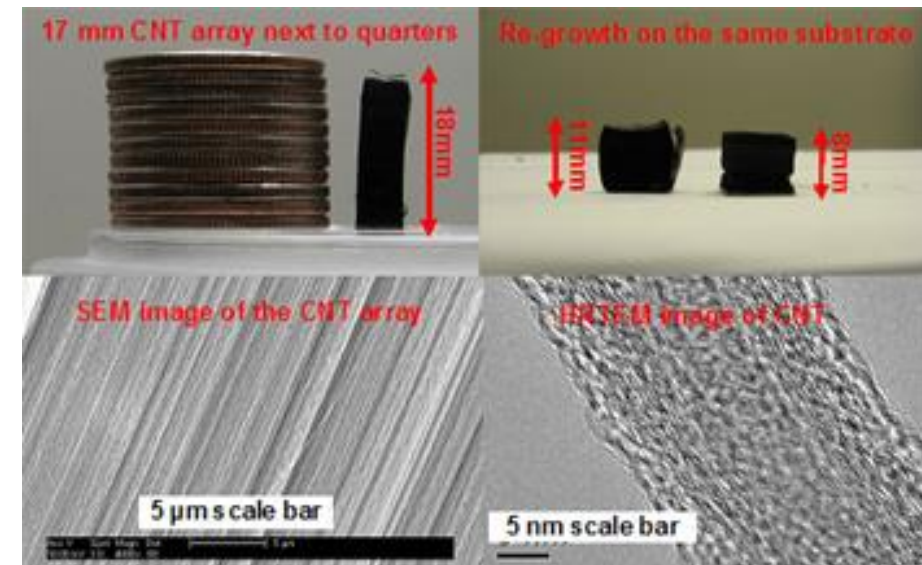
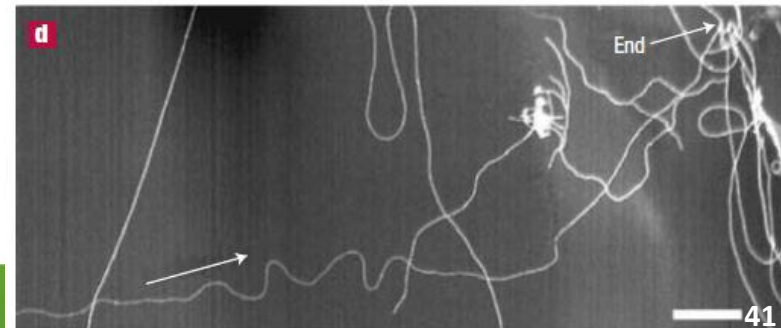
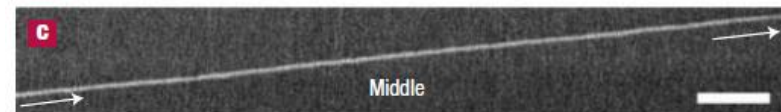
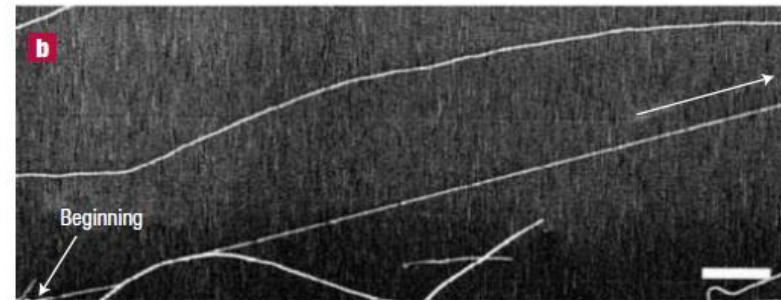
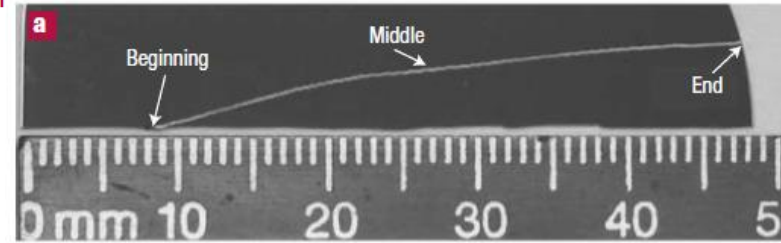
L. X. ZHENG¹, M. J. O'CONNELL¹, S. K. DOORN¹, X. Z. LIAO¹, Y. H. ZHAO¹, E. A. AKHADOV¹,
M. A. HOFFBAUER¹, B. J. ROOP¹, Q. X. JIA¹, R. C. DYE¹, D. E. PETERSON¹, S. M. HUANG², J. LI^{1,2}
AND Y. T. ZHU^{1*}

¹Los Alamos National Laboratory, Los Alamos, New Mexico 87545, USA

²Chemistry Department, Duke University, Durham, North Carolina 27708, USA

*e-mail: yzhu@lanl.gov

nature materials | VOL 3 | OCTOBER 2004 | www.nature.com/naturematerials



17 mm CNT array next to quarters

Re-growth on the same substrate

SEM image of the CNT array

HRTEM image of CNT

5 μ m scale bar

5 nm scale bar

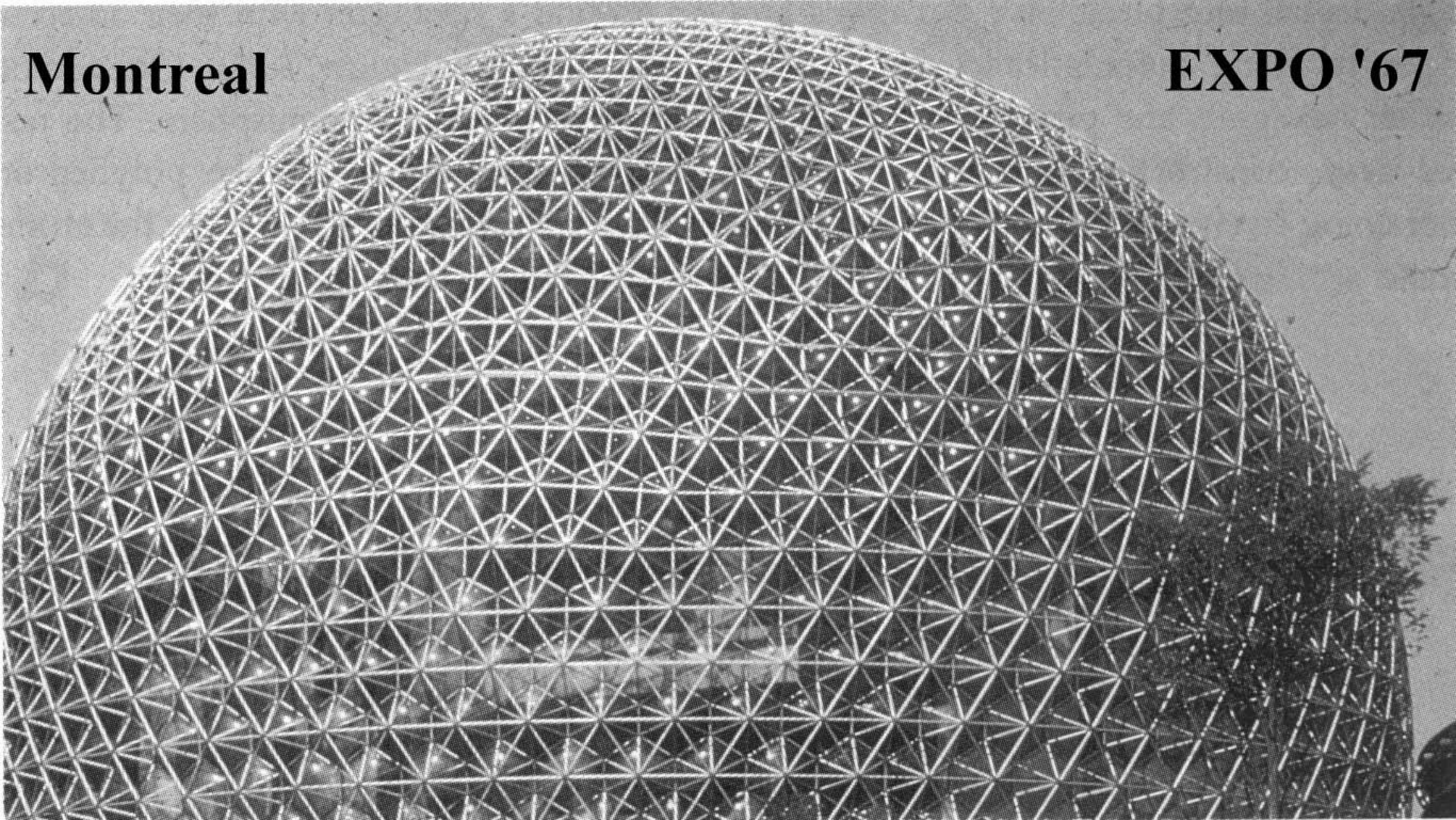
<http://www.uc.edu/news/NR.asp?id=5700>

Fullerenes

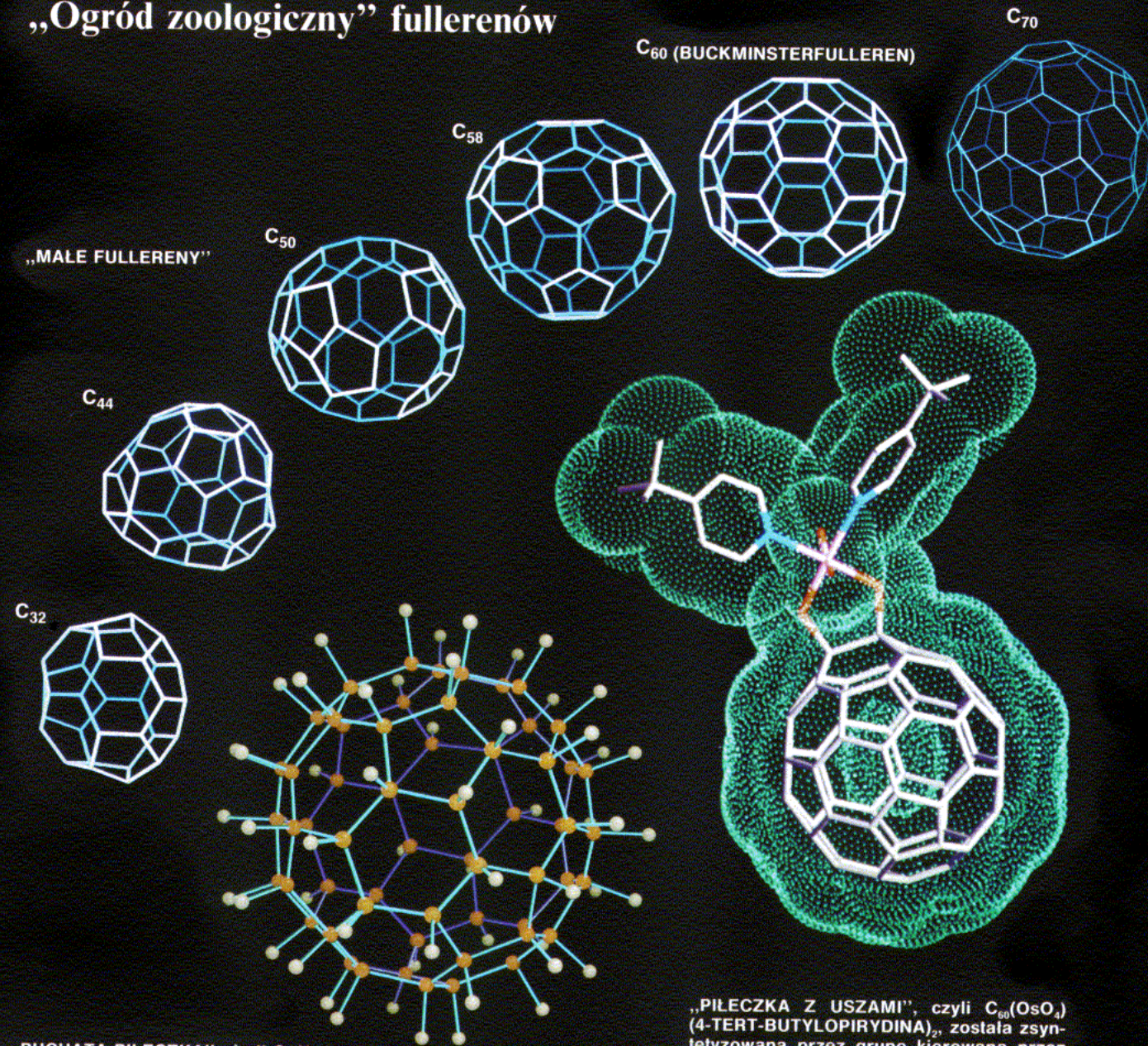
Buckminster Fuller pour un exposition en 1967 à Montréal

Montreal

EXPO '67



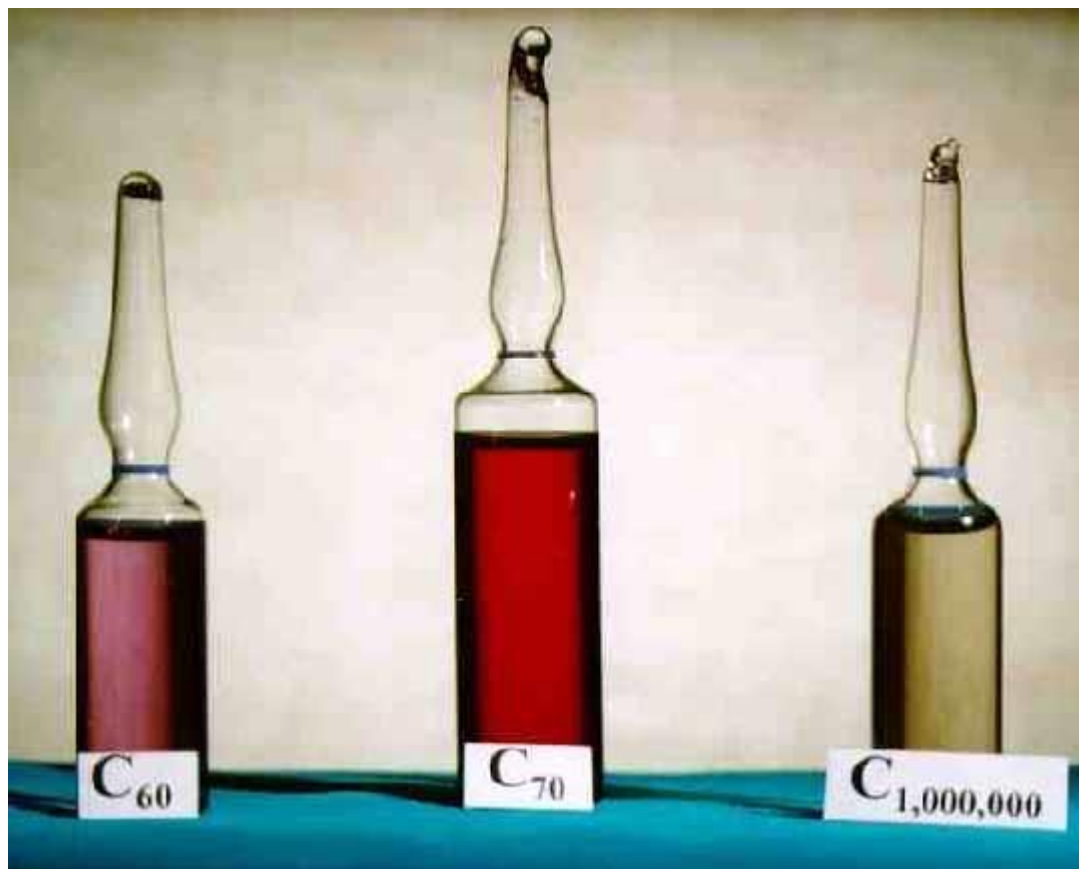
„Ogród zoologiczny” fullerenów



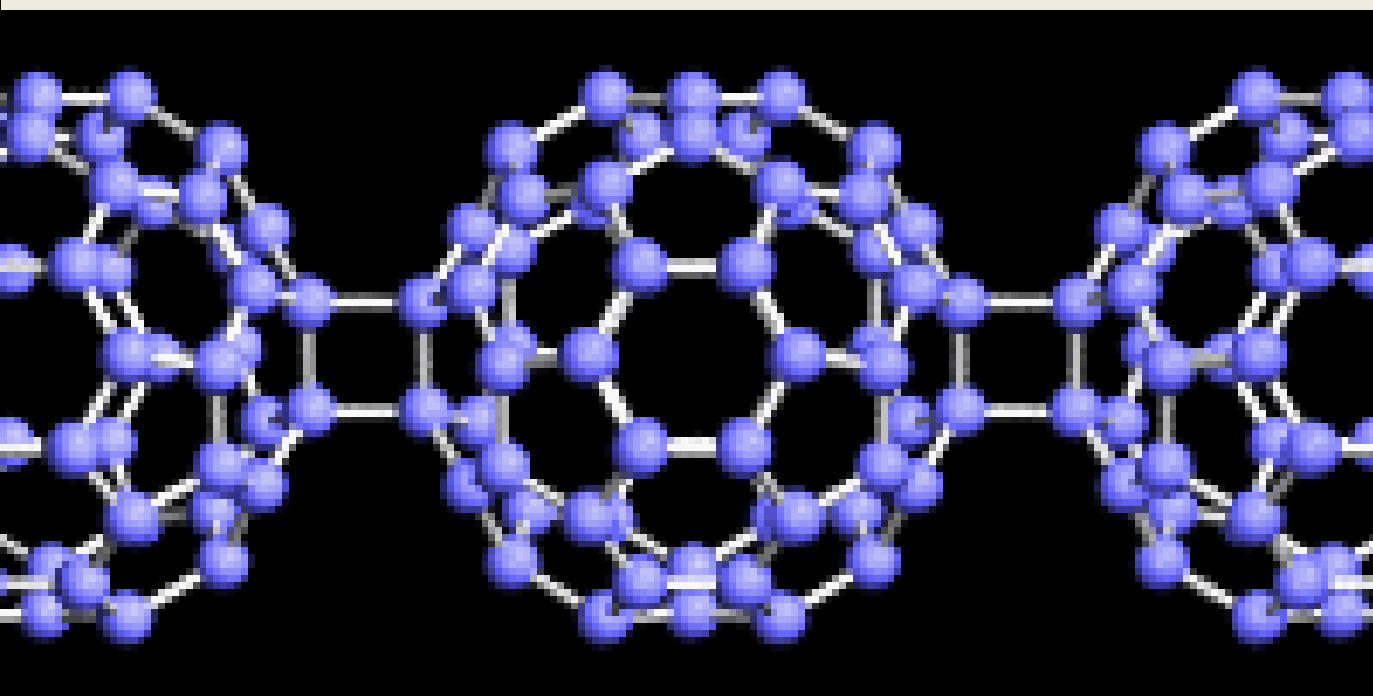
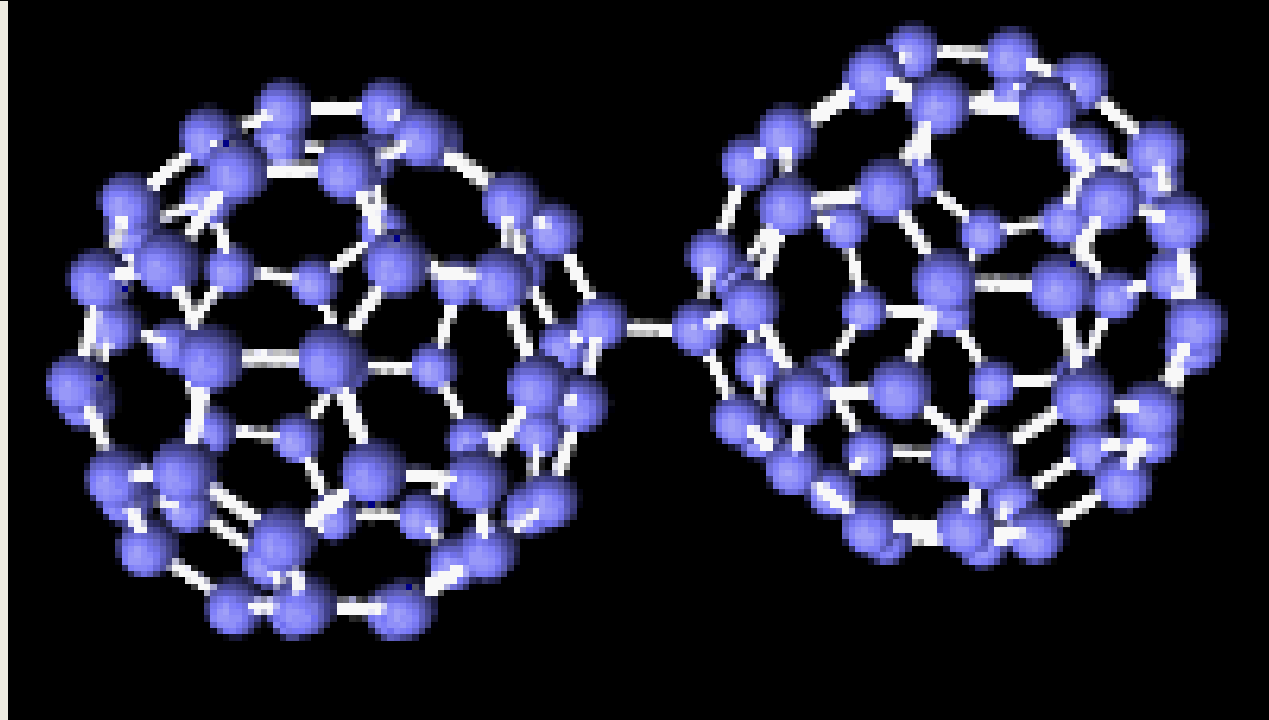
„PUCHATA PILECZKA”, czyli $C_{60}H_{90}$
jest to przewidywana postać
w pełni uwodornionego
buckminsterfullerenu C_{60} .

„PILECZKA Z USZAMI”, czyli $C_{60}(\text{OsO}_4)$
(4-TERT-BUTYLOPIRYDINA)₂, została zsyn-
tetyzowana przez grupę kierowaną przez
Joel M. Hawkinsa z University of California
w Berkeley.

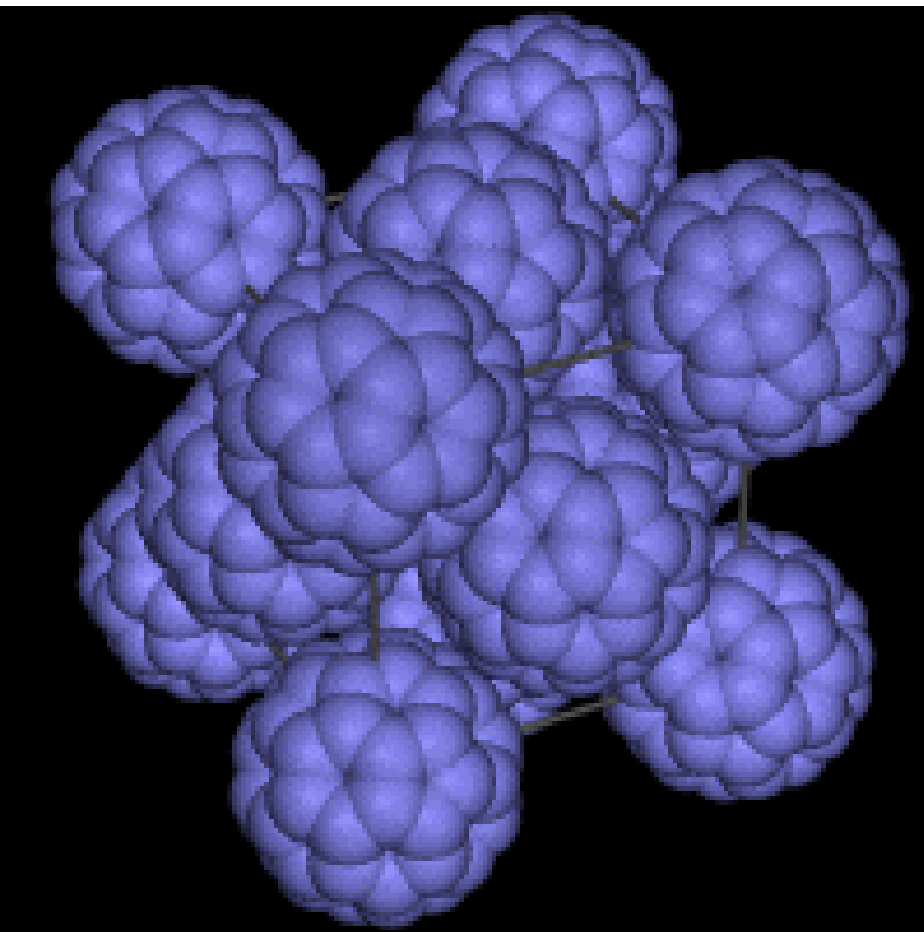
Fullerenes



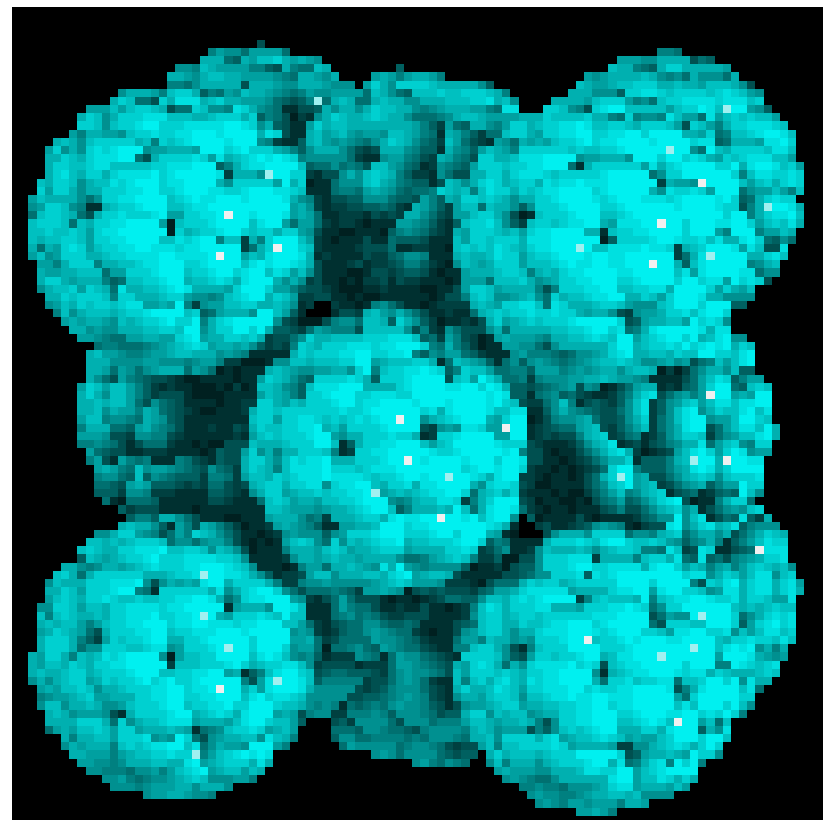
Solutions in toluene



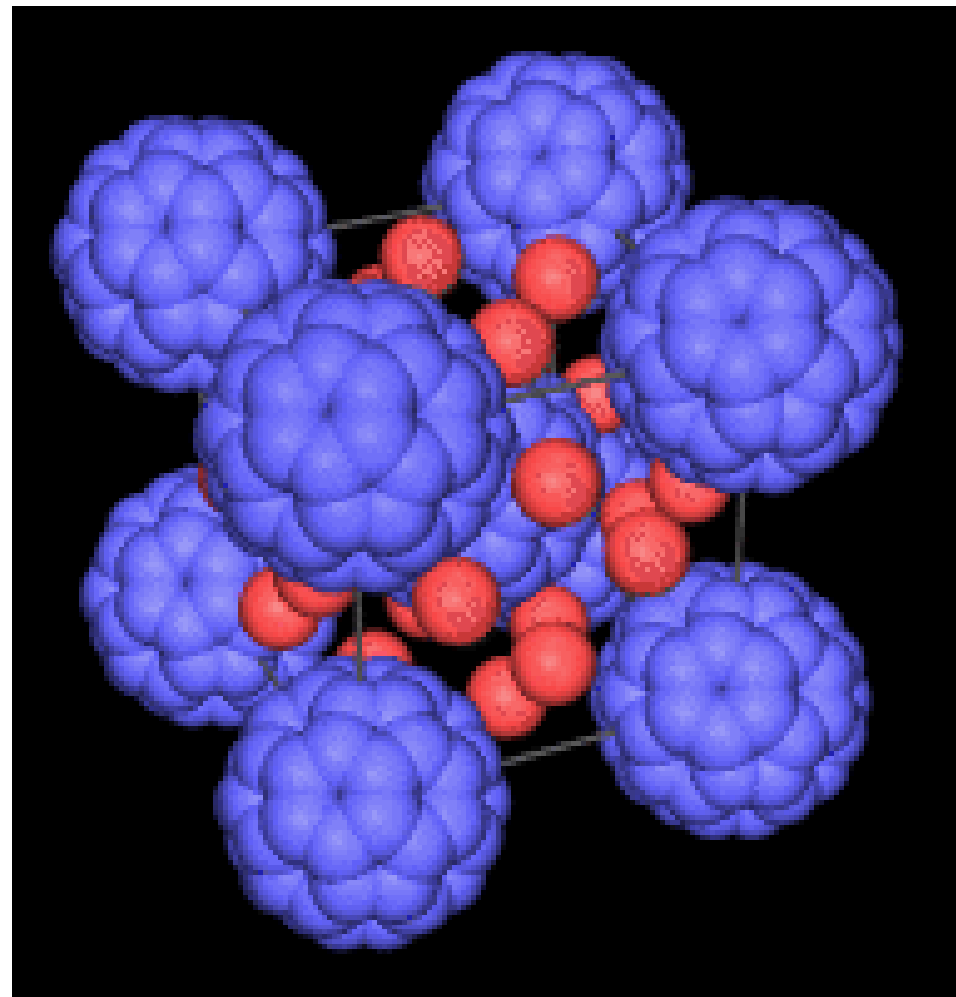
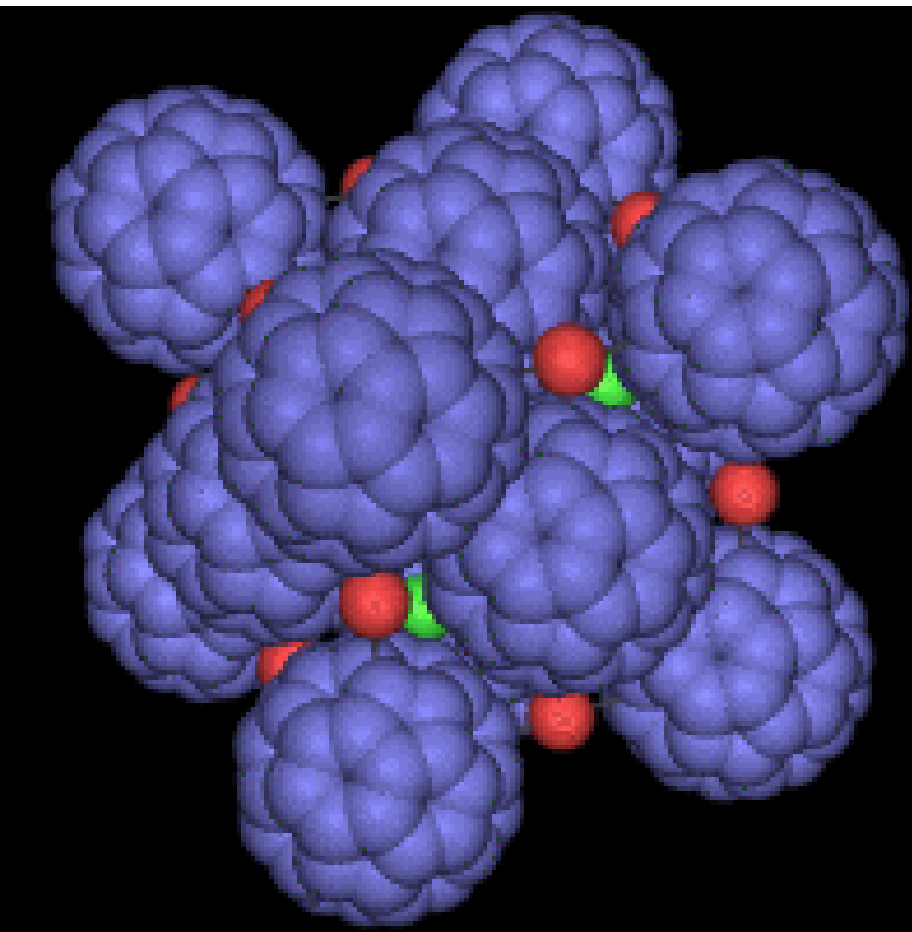
Fullerenes



fcc C₆₀ crystals



Fullerenes

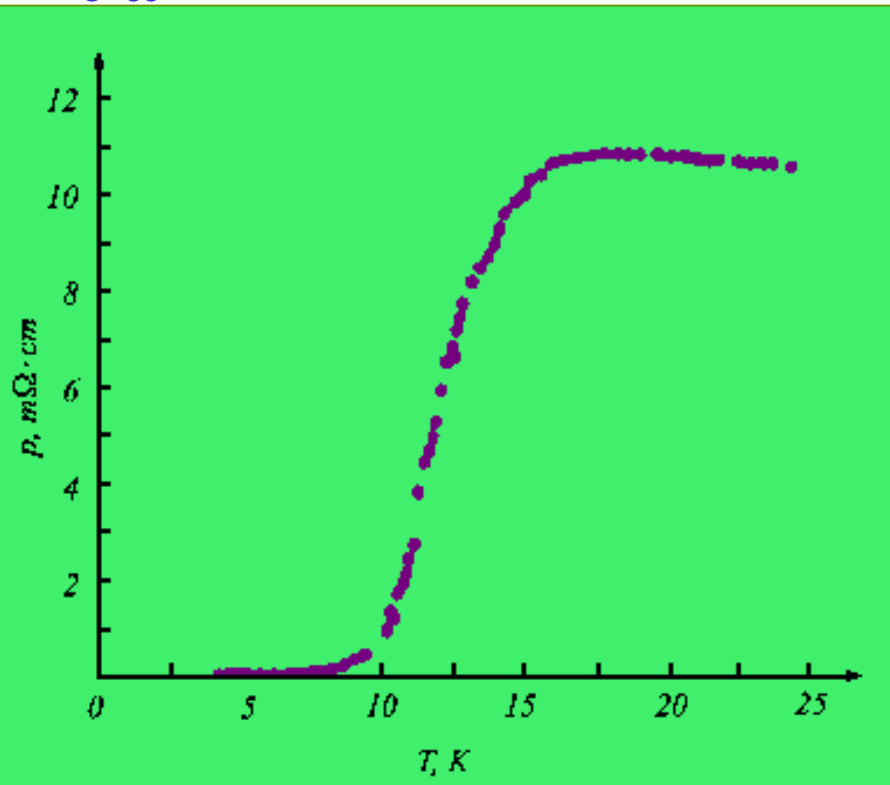


Fullerenes

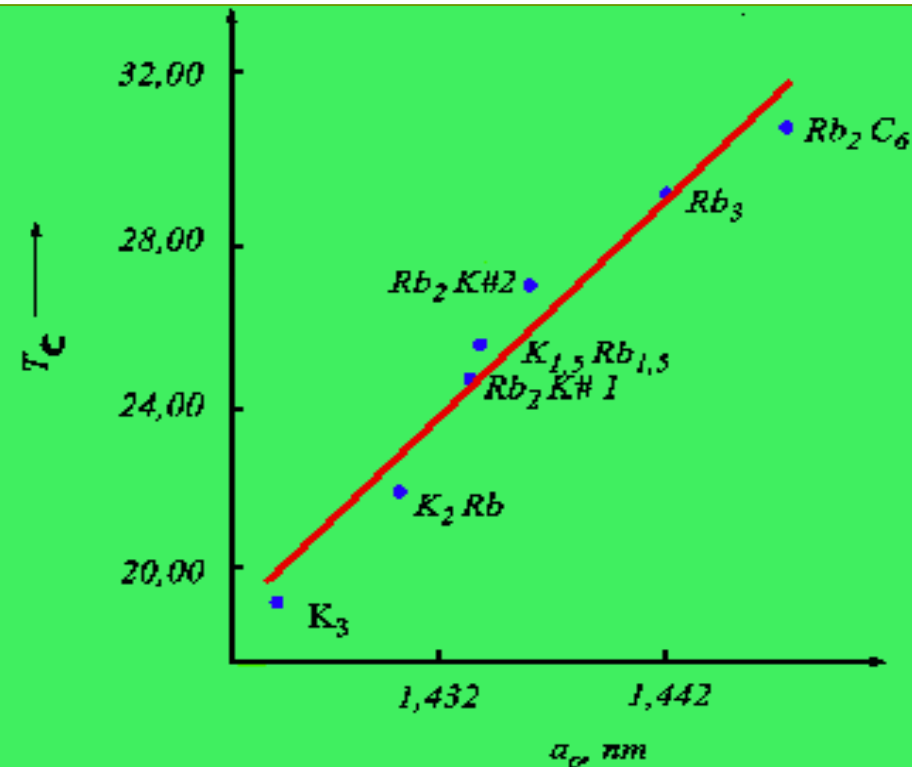
Superconductivity K_3C_{60}

X.D. Xiang, J.G. Hou, et al. Nature 361, 54, 1993

Zależność oporu właściwego K_3C_{60} od temperatury

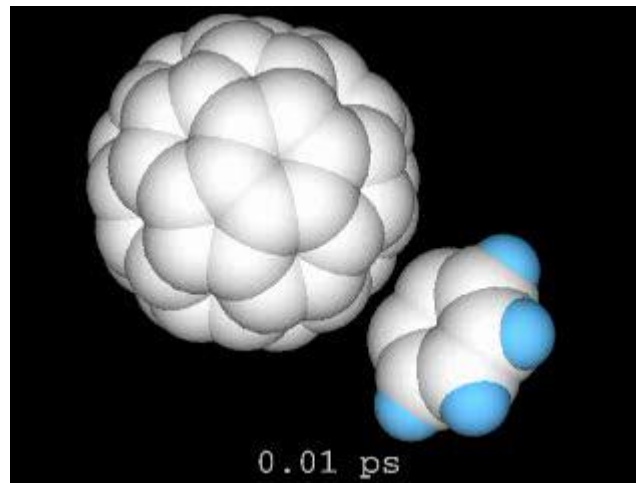
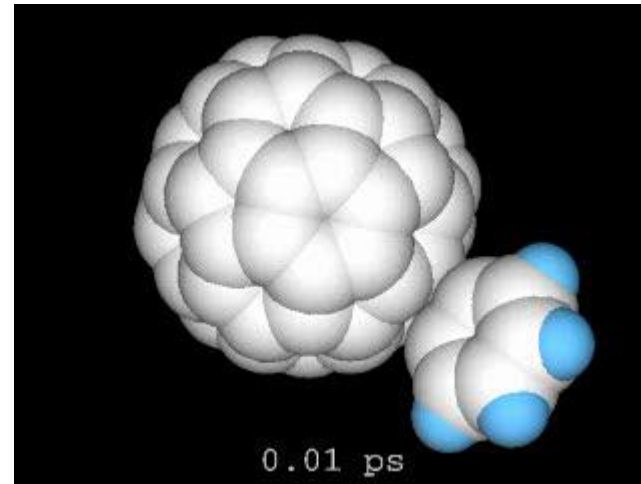
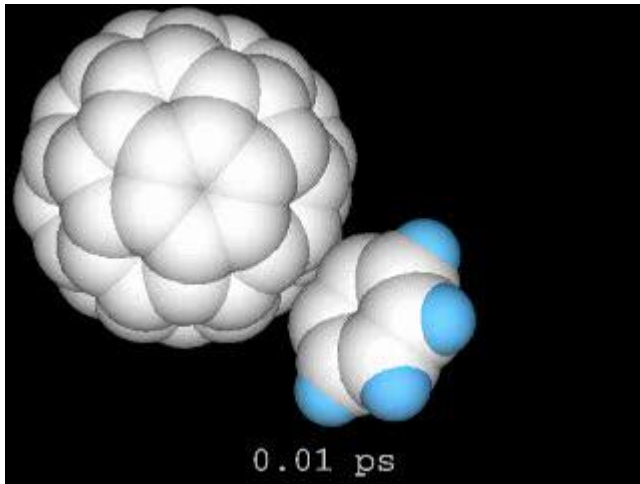


Zależność T_c od stałej sieci



Nanomachines

Benzene + C₆₀

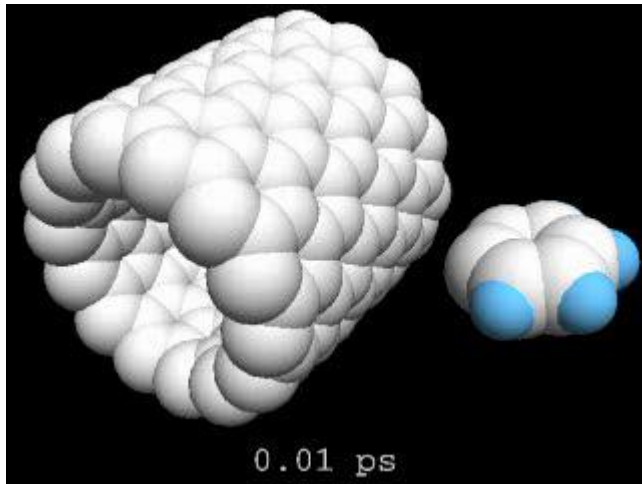


Accurately

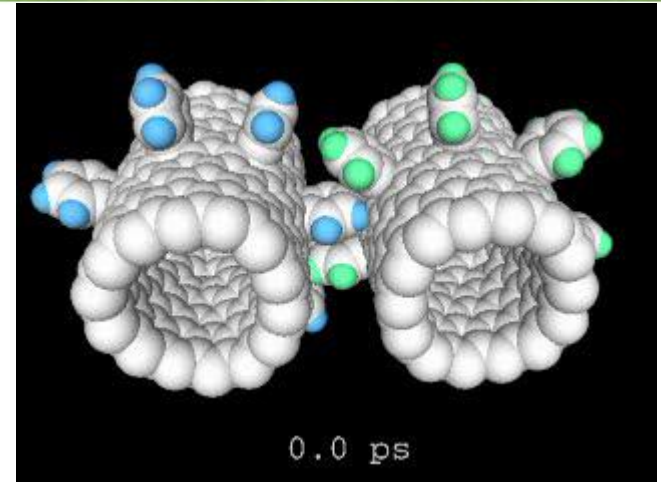
<http://www.ipt.arc.nasa.gov>

Nanomachines

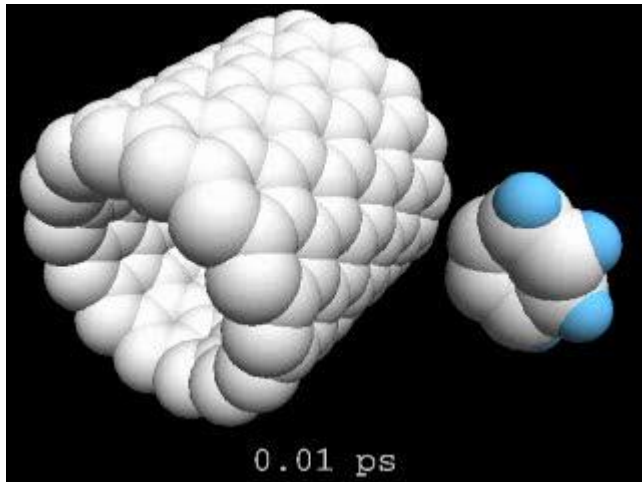
Benzen + CN



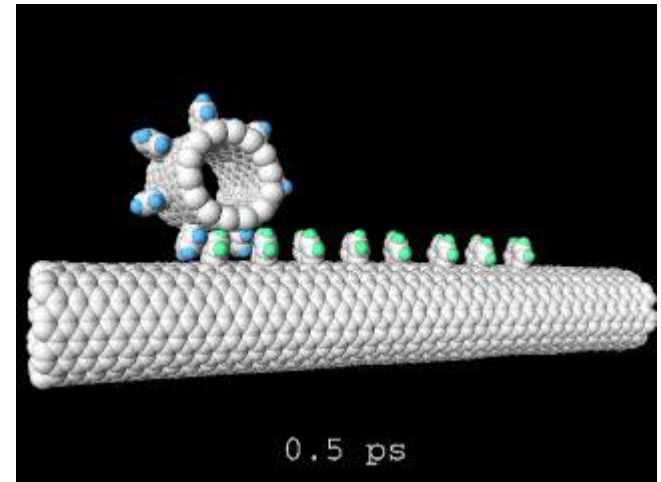
Too slow



Gear Rotation in a Vacuum 200 rot/ns



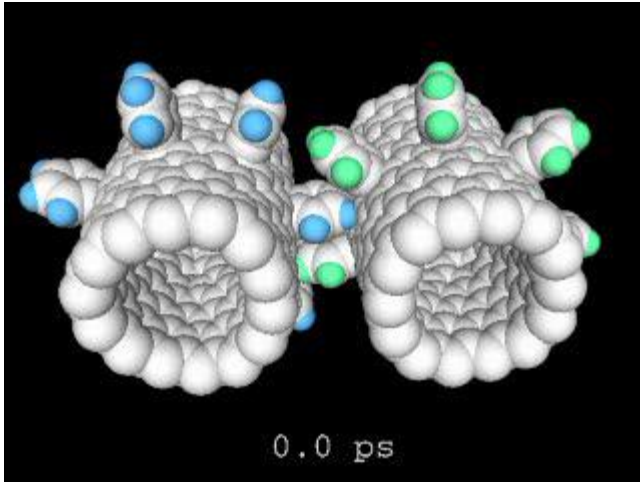
Accurately



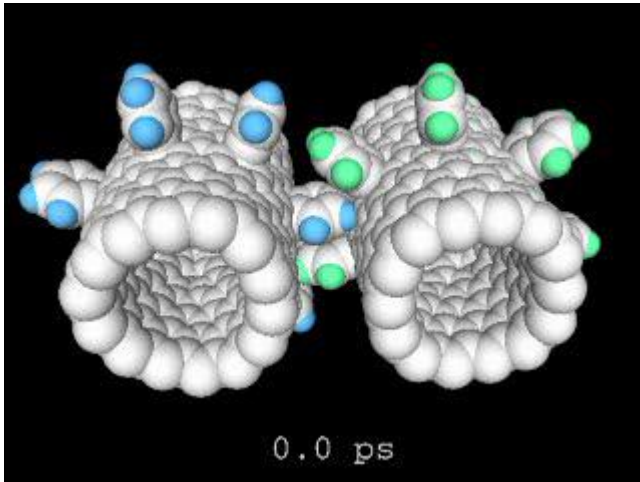
<http://www.ipt.arc.nasa.gov>

Powered Sharf

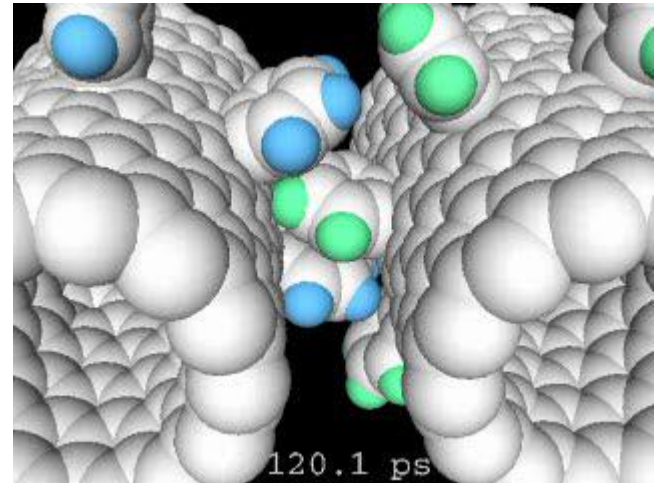
Nanomachines



Gear Rotation at RT 50/70/100 rot/ns



Gear Rotation at RT 50 rot/ns

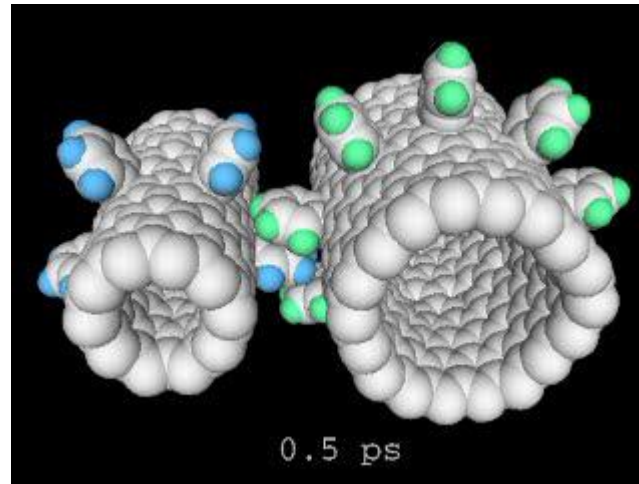
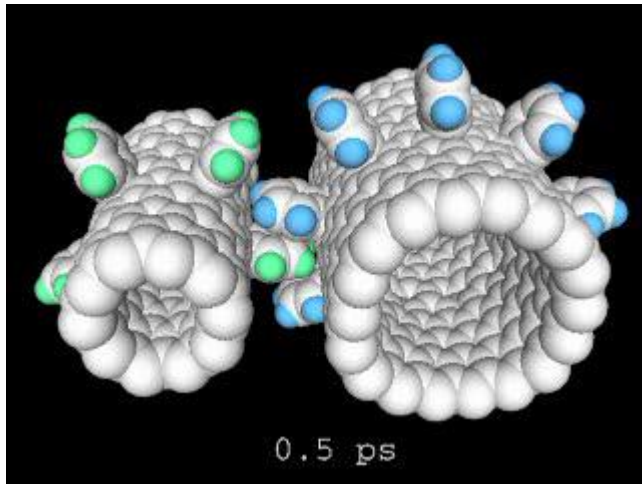


Too fast > 100 rot/ns

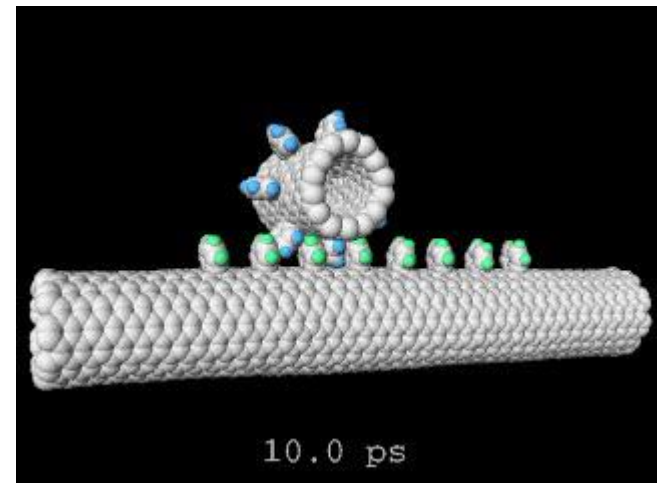
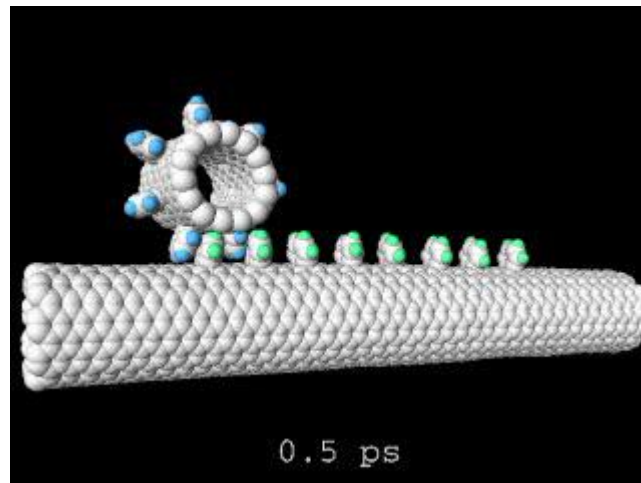
<http://www.ipt.arc.nasa.gov>

Nanomachines

Large Gear Drives Small Gear



Gear and Shaft Operation

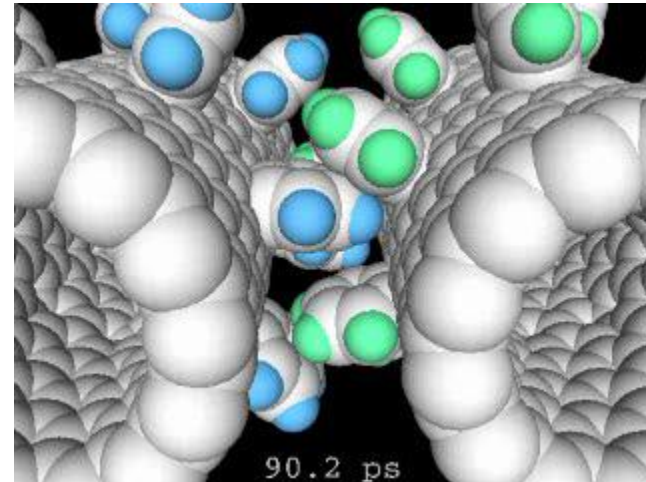
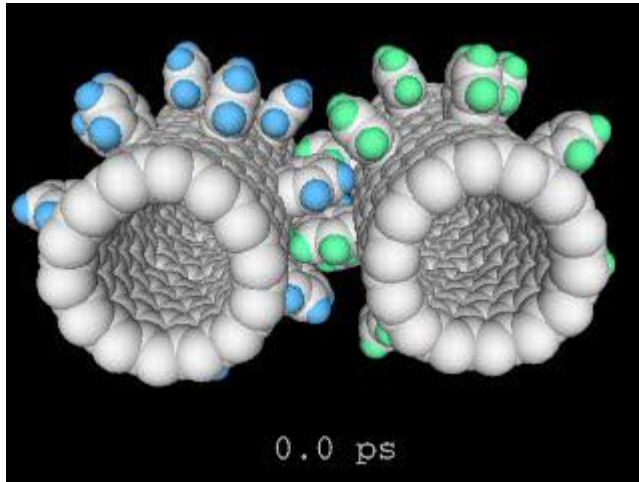


Powered Shaft

Powered Gear

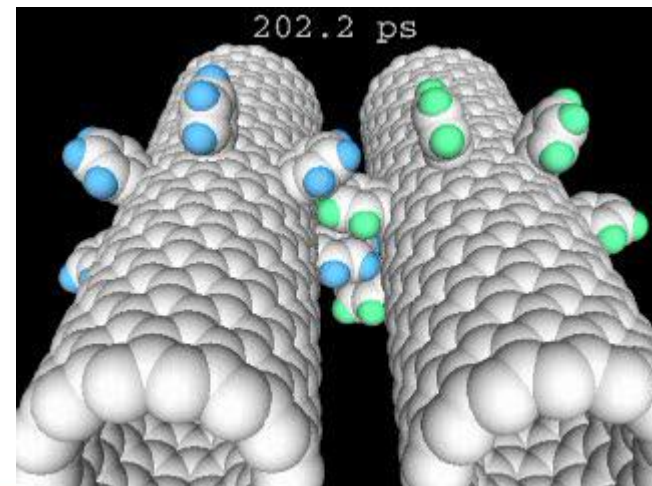
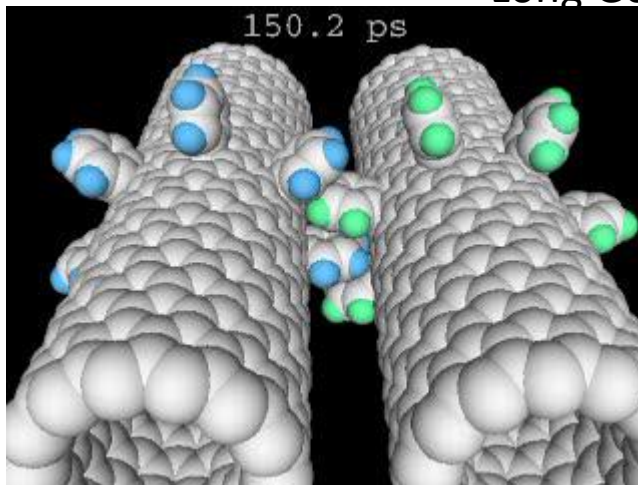
Nanomachines

Rotation of Gears with Two Off-line Rows of Teeth



Zbyt szybko

Long Gear Rotation at Room Temperature



Negatively Curved Graphitic Sheet Model of Amorphous Carbon

S. J. Townsend,^(a) T. J. Lenosky,^(a) D. A. Muller,^(a) C. S. Nichols,^(b) and V. Elser^(a)

Cornell University, Ithaca, New York 14853

(Received 9 April 1992)

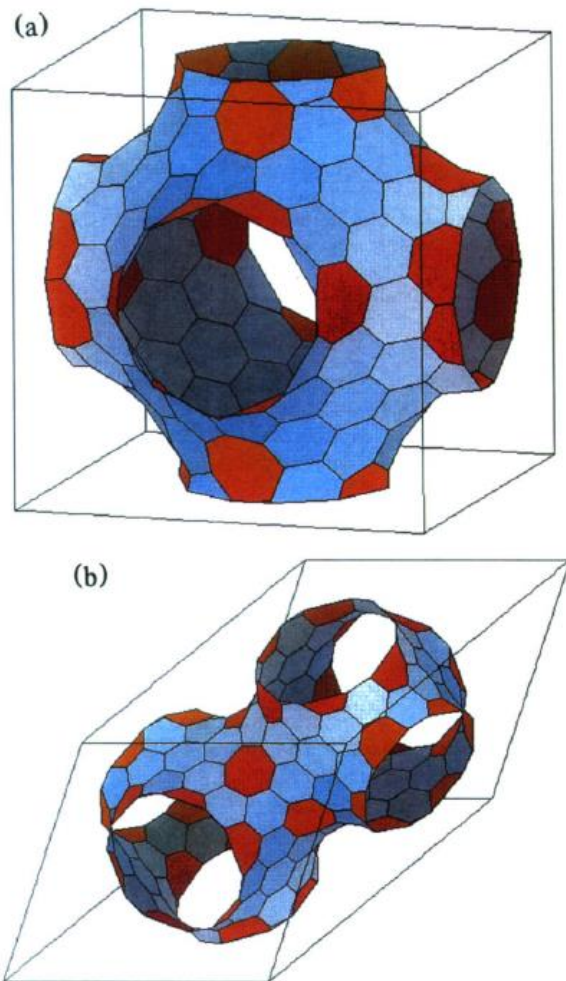


FIG. 1. Views of two new crystalline schwarzites. Each has 216 carbon atoms per primitive unit cell with 80 six-membered rings (blue) and 24 seven-membered rings (orange). The structure in (a) lies on a *P* minimal surface in a cubic cell 15.7 Å on a side. The structure in (b) lies on a *D* minimal surface in an fcc cell whose cubic lattice constant is 24.6 Å.

„plumber’s nightmare”

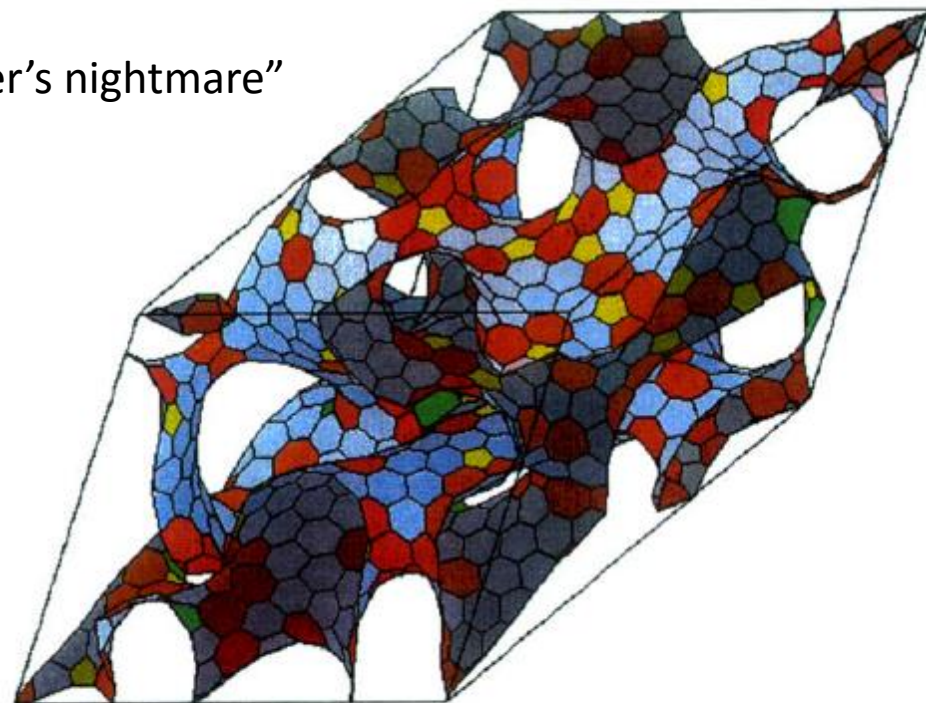


FIG. 2. View of a random schwarzite model on a surface of genus 12 per fcc supercell. The structure has 1248 carbons arranged into 38 five-membered rings (yellow), 394 six-membered rings (blue), 155 seven-membered rings (orange), 12 eight-membered rings (green), and 1 nine-sided ring (pink). Slower annealing produces a structure with many fewer five-membered rings. The cubic unit cell (4 times the volume of the fcc cell shown) is 42.9 Å on a side.

Ok,
Shu

Schwartzite

IMAGE ANALYSIS OF A NEGATIVELY CURVED GRAPHITIC SHEET MODEL FOR AMORPHOUS CARBON

L. A. BURSILL AND LAURE N. BOURGEOIS

*School of Physics, The University of Melbourne, Parkville,
Vic. 3052 Australia*

Received 4 September 1995

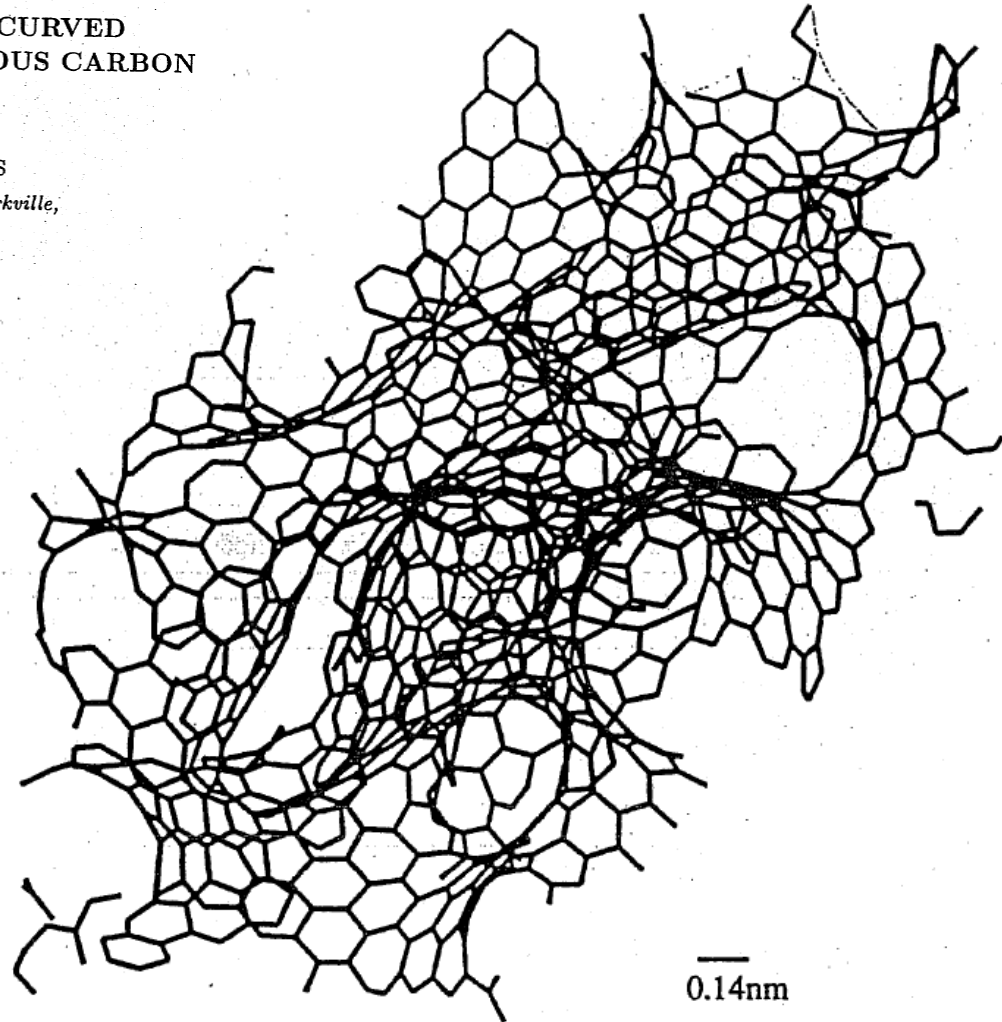


Fig. 2. Random schwartzite model of a surface of genus 12; the volume shown has the shape of a primitive f.c.c. cell.

Magnetism in All-Carbon Nanostructures with Negative Gaussian Curvature

Noejung Park,^{1,2} Mina Yoon,³ Savas Berber,³ Jisoon Ihm,^{4,2} Eiji Osawa,⁵ and David Tománek^{3,*}

¹Research Organization for Information Science and Technology, 2-2-54 Naka-Meguro, Meguro-ku, Tokyo 153-0061, Japan

²Center for Nanotube and Nanostructured Composites, Sungkyunkwan University, Suwon, 440-746, Korea

³Department of Physics and Astronomy, Michigan State University, East Lansing, Michigan 48824-2320, USA

⁴School of Physics, Seoul National University, Seoul 151-742, Korea

⁵NanoCarbon Research Institute Limited, Chosei-mura, Chosei-gun, Chiba 2994395, Japan

(Received 8 July 2003; published 5 December 2003)

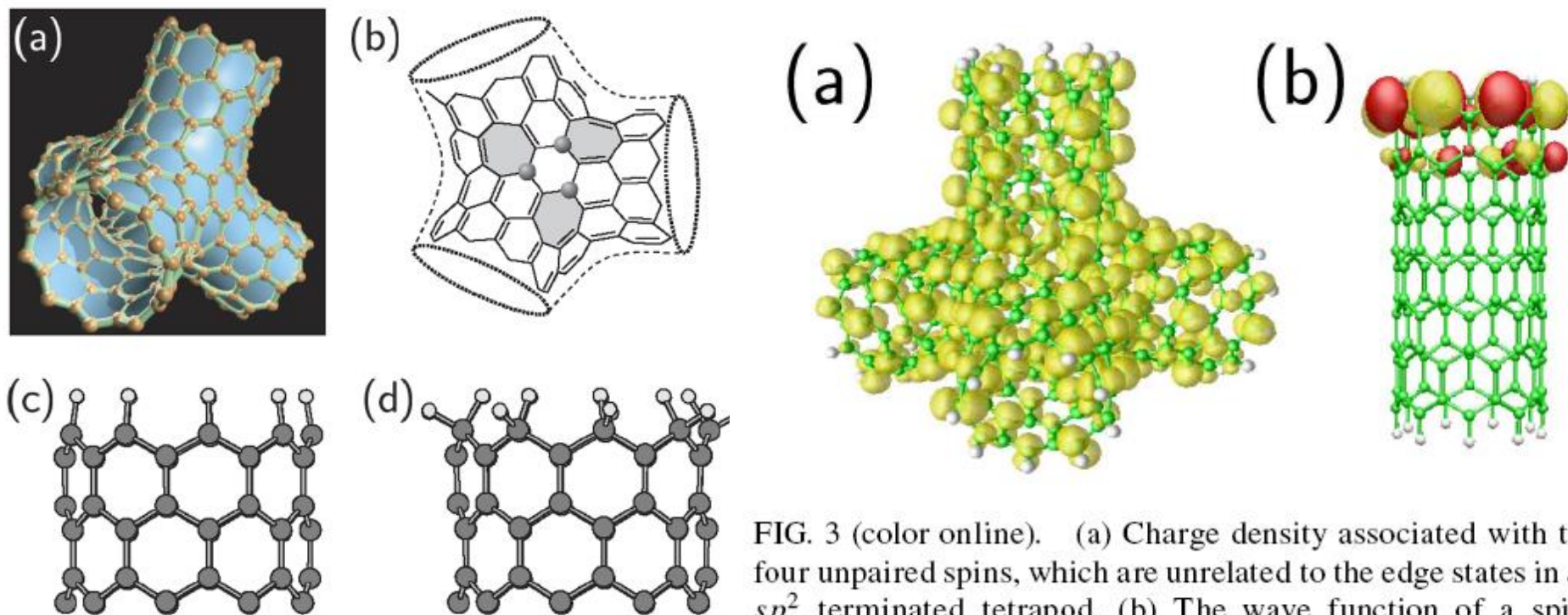


FIG. 3 (color online). (a) Charge density associated with the four unpaired spins, which are unrelated to the edge states in an sp^2 terminated tetrapod. (b) The wave function of a spin-polarized edge state in an sp^2 terminated (9,0) nanotube. We use color shading to represent the phase of the wave function.