

# Racetrack inflation and $F$ -term uplifting

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in collaboration with Marek Olechowski

- 1 Racetrack inflation
- 2 Constraints for the Kähler potential
- 3  $F$ -term uplifted racetrack inflation

F-term potential in 4D SUGRA

$$V = e^K \left( K^{I\bar{J}} D_I W \overline{D_{\bar{J}} W} - 3 |W|^2 \right)$$

Kähler potential for **the volume modulus**

$$K = -3 \ln(T + \bar{T})$$

For fixed dilaton and CSM **fluxes** contribute a constant term to the superpotential

$$W = A$$

Introducing **non-perturbative** correction (e.g. gaugino condensation) to the superpotential

$$W = A + C e^{-cT}$$

volume modulus can be stabilized at AdS SUSY minimum.

We live in dS space  $\Rightarrow$   $\overline{D3}$ -branes introduced to **uplift** minimum to dS space:

$$\Delta V = \frac{E}{(T + \bar{T})^2}$$

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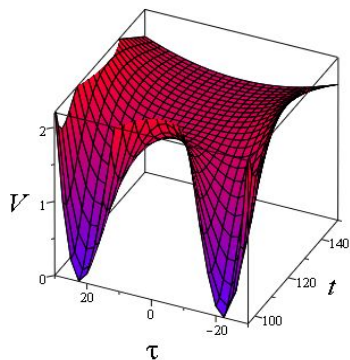
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- Moduli stabilization allow for constructing inflationary models inspired by string theory.
- Moduli fields can be considered as candidates for the inflaton (moduli inflation).
- KKLT potential is too steep ( $|\eta| > 1$ ) and does not fulfil the slow-roll conditions  $\Rightarrow$  inflation cannot be realized.
- Inflation can be realized with the racetrack superpotential:

$$W = A + Ce^{-cT} + De^{-dT}$$



# Racetrack Inflation - Saddle Point Model



Blanco-Pillado et al. '04

Inflation in the vicinity of a  
saddle point

Axion  $\tau$  is the inflaton

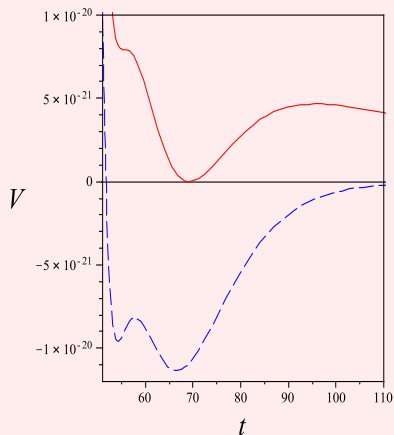
Fine-tuning

Flux parameter  $A$  fine-tuned at  
the level of  $10^{-4}$

CMB signatures

- $n_s \lesssim 0.95$
- $r \ll 1$

# Racetrack Inflation - Inflection Point Model



Linde, Westphal '07

Inflation in the vicinity of an **inflection point**  
 $t$  is the inflaton

## Fine-tuning

Fine-tuning of parameters related to the height of the barrier

*MB, Olechowski '08*

Avoiding overshooting problem requires fine-tuning at the level of  $10^{-8}$

## CMB signatures

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- $r \ll 1$

# Uplifting in Racetrack Inflation

In both racetrack inflation models SUSY is broken explicitly by  $\overline{D3}$ -branes

Most of the existing uplifting mechanisms have not been applied to inflationary models

## Goal

Construct racetrack inflation models in a fully supersymmetric framework with the hidden sector matter field as a source of uplifting and SUSY breaking

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# Constraints for the Kähler Potential

The maximal value of  $\eta$  is related to the curvature of the Kähler manifold spanned by the scalar fields appearing in the theory.

*MB, Olechowski '08; Covi et al. '08*

The **necessary** condition for  $|\eta| \ll 1$ :

$$R(f^i) < \frac{2}{\widehat{G}^2} < \frac{2}{3}$$

where  $G = K + \log |W|^2$  and  $\widehat{G}^2 \equiv \sqrt{G^i G_i} = 3 + e^{-G} V$

$R(f^i) \equiv R_{i\bar{j}\bar{p}\bar{q}} f^i f^{\bar{j}} f^{\bar{p}} f^{\bar{q}}$  is the sectional curvature along the

direction of the SUSY breaking ( $f_i \equiv G_i / \widehat{G}^2$  is the unit vector defining that direction).

Note:  $\widehat{G}^2 = 3$  for Minkowski,  $\widehat{G}^2 > 3$  for de Sitter.

**The above condition can be used to eliminate some models even without specifying the superpotential!**

# One Field Case - the Role of $\overline{D3}$ -brane Uplifting

In the one field case the necessary condition simplifies:

$$R_T < \frac{2}{\widehat{G}^2} < \frac{2}{3}$$

Kähler potential for the volume modulus:

$$K = -3 \ln(T + \overline{T})$$

The curvature scalar for the volume modulus takes the form:

$$R_T = \frac{2}{3}$$

The trace of the  $\eta$ -matrix is constant and negative: *MB, Olechowski '08*

$$\text{Tr}(\hat{\eta}) = -\frac{4}{3}$$

$\eta \leq -2/3 \Rightarrow$  **slow-roll conditions violated!**

How is it possible that racetrack inflation works?

Uplifting from  $\overline{D3}$ -branes is non-supersymmetric and gives additional, positive contribution to  $\text{Tr}(\hat{\eta})$

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For the no-scale Kähler potential

$$K = -3 \ln(T + \bar{T} - |\Phi|^2)$$

the Kähler manifold is a maximally symmetric coset space with a constant curvature  $R(f^i) = 2/3$

*Gomez-Reino, Scrucce '06*



Necessary condition for slow-roll inflation violated  $\Rightarrow$  Racetrack inflation cannot be uplifted for any kind of coupling between the volume modulus and the matter field in the superpotential

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For the separable Kähler potential:

$$K = K^{(T)}(T, \bar{T}) + K^{(\Phi)}(\Phi, \bar{\Phi})$$

the necessary condition for slow-roll inflation reduces to:

$$R_T \Theta_T^4 + R_\Phi \Theta_\Phi^4 < \frac{2}{\widehat{G}^2}$$

$R_i$  are the scalar curvatures of the one dimensional submanifolds associated with each of the fields

$\Theta_i^2 \equiv G_{i\bar{i}} f^i f^{\bar{i}}$  parameterize SUSY breaking and satisfy  $\sum_i \Theta_i^2 = 1$

Volume modulus coupled to canonically normalized matter field:

$$K = -3 \ln(T + \bar{T}) + \Phi \bar{\Phi}$$

$R_\Phi = 0$  so the necessary condition for slow-roll inflation is:

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If the matter field dominates SUSY breaking during inflation ( $\Theta_T^2 \ll 1$ ) then  $F$ -term uplifted racetrack inflation is possible

## Superpotential

$$W = A + Ce^{-cT} + De^{-dT} - \mu^2 \Phi$$

is sufficient to uplift both racetrack inflation models!

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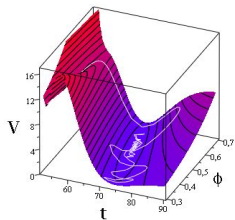
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# Polonyi Uplifting of Inflection Point Inflation



$\Theta_\Phi^2 \gg \Theta_T^2 \Rightarrow \Phi$  dominates SUSY breaking  
(during and after inflation)

$\phi$  is the main component of the inflaton

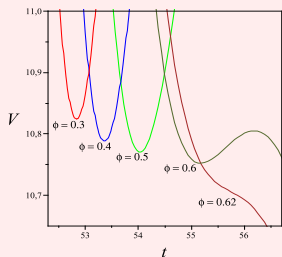
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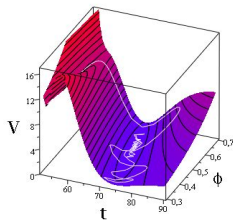
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5 orders of magnitude weaker than in the original model!

## CMB signatures

$n_s \gtrsim 0.93$  not altered by  $F$ -term uplifting  
but for some sets of parameters isocurvature perturbations may be produced



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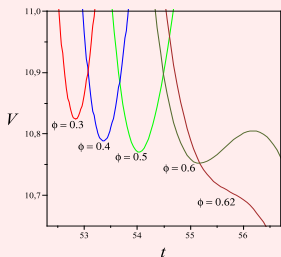
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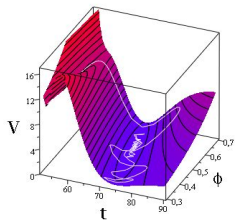
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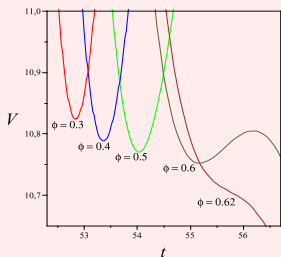
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# Polonyi Uplifting of Saddle Point Inflation

All 4 fields are involved in the inflationary dynamics

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## Summary of Polonyi uplifting

Volume modulus no longer the inflaton but fine-tuning reduced

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The volume modulus coupled to quantum corrected O'Raifeartaigh model:

Modified Kähler potential

$$K = -3 \ln(T + \bar{T}) + \Phi \bar{\Phi} - \frac{(\Phi \bar{\Phi})^2}{\Lambda^2}, \quad \Lambda \ll 1$$

$$R_{\Phi} = \frac{-4}{\Lambda^2(1-4|\Phi|^2/\Lambda^2)^3} < 0$$

Superpotential

$$W = A + Ce^{-cT} + De^{-dT} - \mu^2 \Phi$$

SUSY breaking minimum occurs at  $|\Phi| \sim \Lambda^2 \ll 1$

The mass matrix at  $\tau = \theta = 0$  in the limit  $\phi \ll \Lambda \ll 1$ :

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- the matter field is heavier than the volume modulus
- the mixing between the matter field and the volume modulus is strongly suppressed

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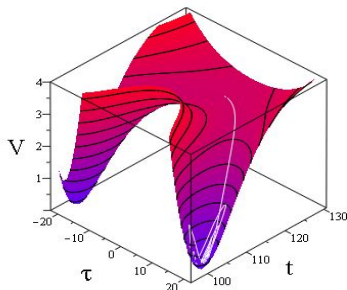
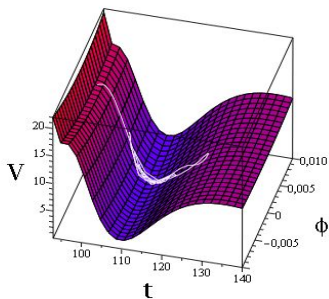
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# O'uplifting of Racetrack Inflation Models

- $\Phi$  is almost constant during inflation
- SUSY breaking dominated by the matter field ( $\Theta_\Phi > \Theta_T$ )
- matter field  $F$ -term provides effective uplifting term  
 $|F_\Phi|^2 \sim 1/t^3$
- O'uplifted racetrack models resemble the original ones
- Volume modulus is the inflaton but SUSY is broken spontaneously by the matter field





- Racetrack inflation can be realized in a fully supersymmetric framework with the matter field  $F$ -term as a source of SUSY breaking and uplifting
- Details of the inflationary scenario depend on the choice of the matter field sector
  - **Polonyi uplifting** - the volume modulus is no longer the inflaton but fine-tuning significantly reduced
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